

重力波観測の現状と

マルチメッセンジャーで探る重力波天体の物理

Status of Gravitational Wave Observations and Physics of GW Sources with Multi-messenger

Nobuyuki Kanda / Osaka City Univ.
KAGRA collaboration
3/2/2017, Chiba University

Basics of Gravitational Wave

Gravitational Wave (GW) is

- distortion of Space-Time
- predicted by General Relativity (GR) at 1915-1916
- directly measured at 2015

Detection / Observation of GWs

- by large base-length laser interferometer
- with **multi-detectors** : two LIGOs + Virgo, KAGRA in near future
- can extract information of source's dynamical motion.

GW sources are

- massive and compact objects : neutron star (NS), black-hole (BH)
- energetic motion : compact binary coalescence (CBC), supernova (SN)
==> These events inevitably lead to high-energy astronomical phenomena. Therefore, transient GWs may have multi-messenger counterpart.
- Pulsar
- Stochastic background (cosmological origin, astronomical origin, string, etc..)
- unknown

Space-time and its wave

Gravity distorts the space-time !

Einstein Eq.

$$R_{\mu\nu} - \frac{1}{2} g_{\mu\nu} R = -\kappa T_{\mu\nu}$$

metric tensor

“flat” space-time (Minkowski)

$$g_{\mu\nu} = \eta_{\mu\nu} = \begin{pmatrix} ct & x & y & z \\ -1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix} \begin{matrix} ct \\ x \\ y \\ z \end{matrix}$$

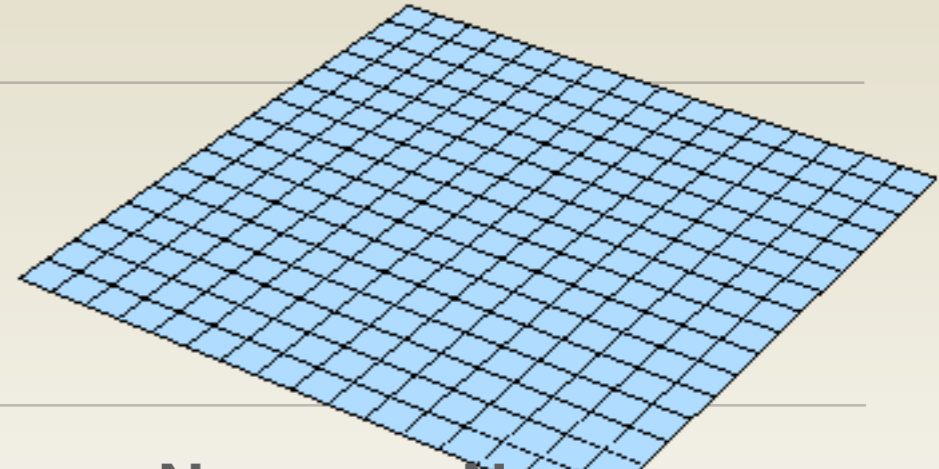
“curved (distorted)” space-time

$$g_{\mu\nu} \neq \eta_{\mu\nu}$$

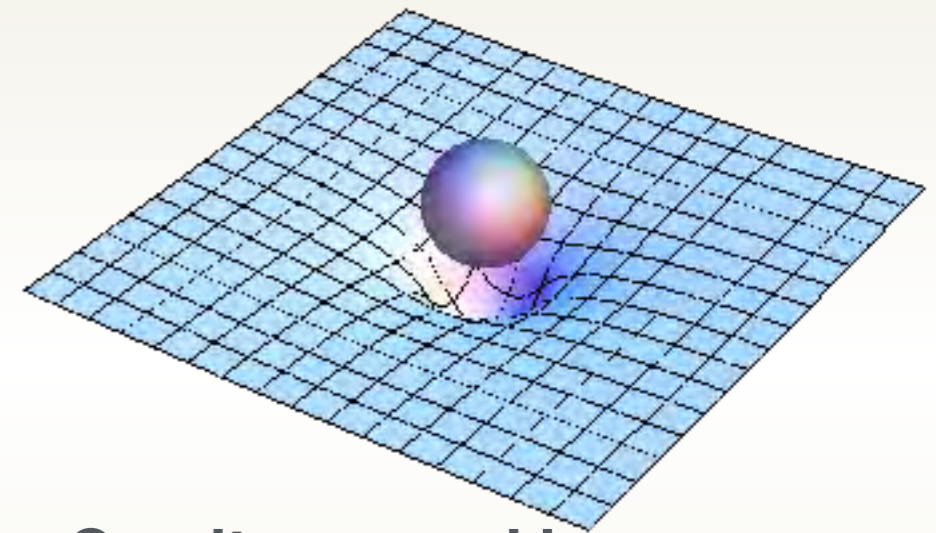
small perturbation ‘h’ --> Waves

$$g_{\mu\nu} = \eta_{\mu\nu} + h_{\mu\nu}$$

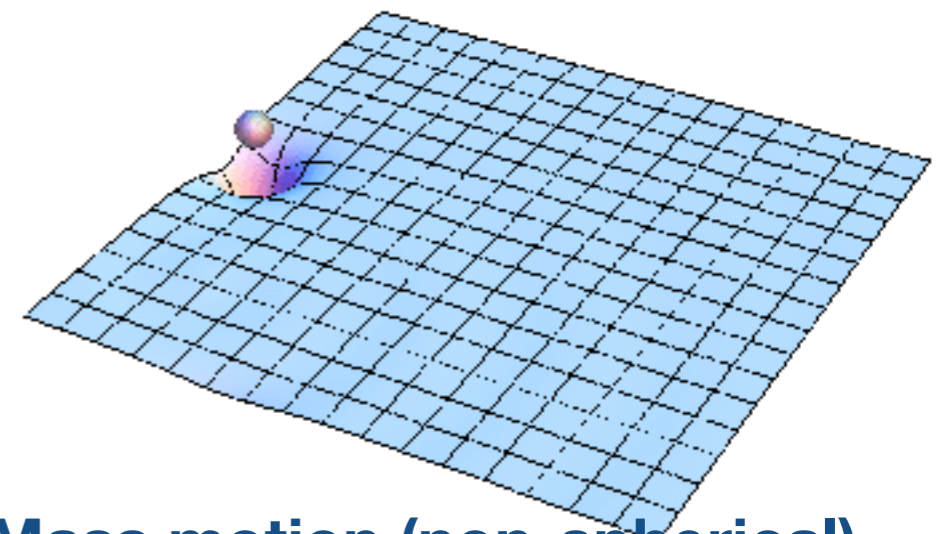
$$\left(\nabla^2 - \frac{1}{c^2} \frac{\partial^2}{\partial t^2} \right) h_{\mu\nu} = 0$$



No mass, No energy
=> Flat space-time



Gravity caused by mass
=> Distorted space-time



Mass motion (non-spherical)
=> Propagation of the distortion
“Gravitational Wave”

GW radiation

Source

- change (time derivative) of **quadrupole moment** of mass distribution $I_{\mu\nu} = \int dV (x_\mu x_\nu - \frac{1}{3} \delta_{\mu\nu} r^2) \rho(\vec{r})$

Amplitude

- inversely proportional to the distance between source and observer $h_{\mu\nu} = \frac{2G}{Rc^4} \ddot{I}_{\mu\nu}$

Energy

- total energy is given as : $E_{GW} \sim \frac{G}{5c^5} \langle \ddot{I}_{\mu\nu} \ddot{I}^{\mu\nu} \rangle$

Electromagnetic Wave

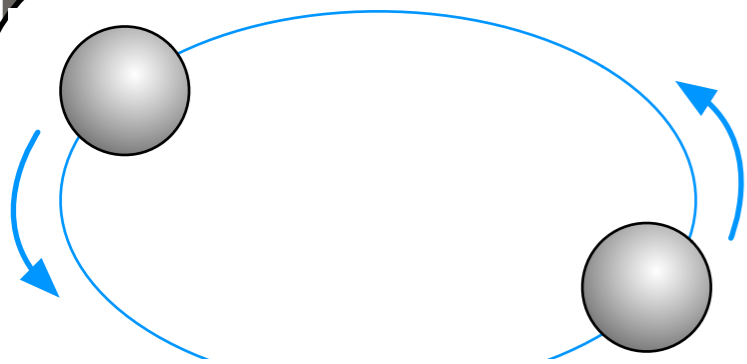
Gravitational Wave

Theory

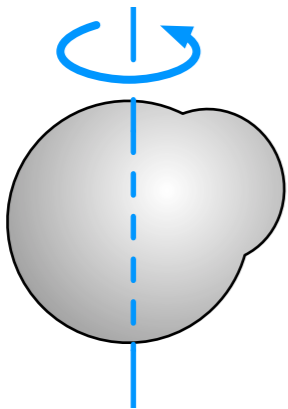
Electromagnetism

General Relativity

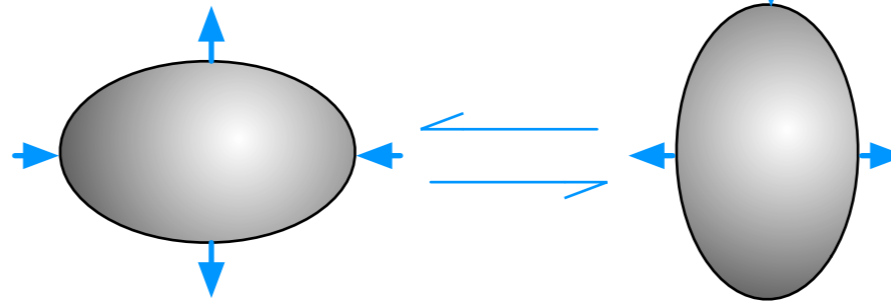
(solution of Einstein Equation)



binary
= rotating dumbbell



Rotation of non-axisymmetric object



Quadrupole deformation

→ 運動方向、變形方向

Metric of the space-time

$$\begin{pmatrix} 0 & 0 & 0 & 0 \\ 0 & h_+ & h_\times & 0 \\ 0 & h_\times & -h_+ & 0 \\ 0 & 0 & 0 & 0 \end{pmatrix}$$

quadrupole moment

$$(\ddot{I}_{\mu\nu})$$

10^{-39} for protons

Character

speed of light

speed of light

transverse

transverse

Note:

easily interact with materials,
can shield

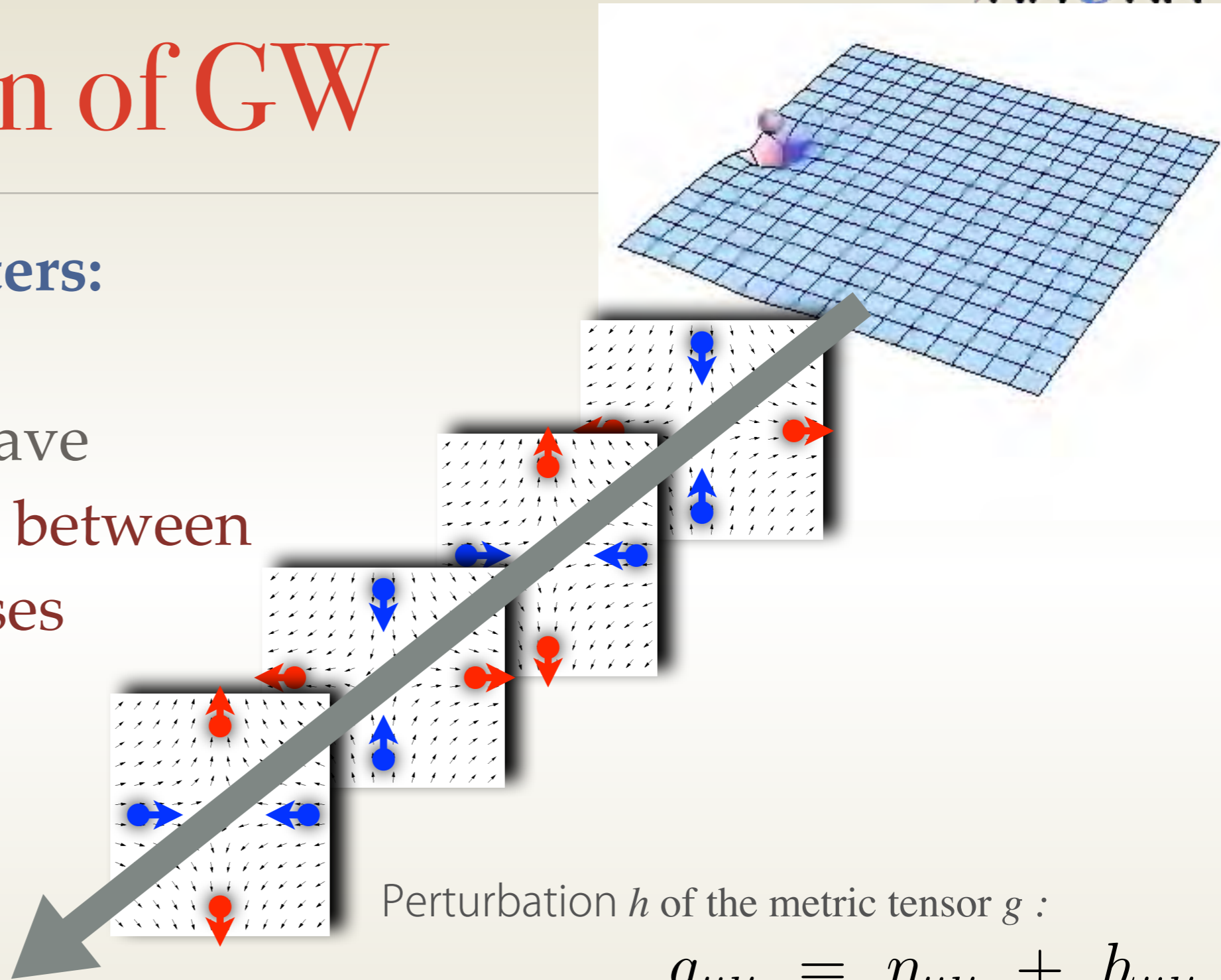
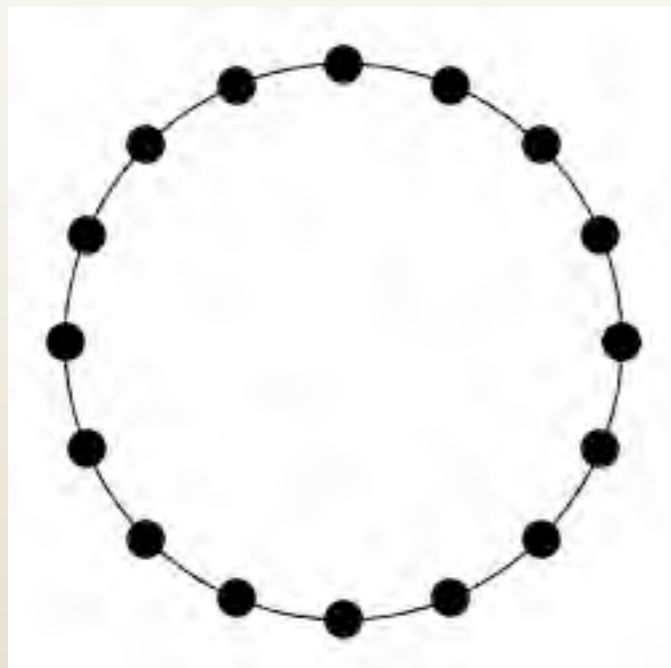
very small loss passing the
materials,
cannot shield

Propagation of GW

Important characters:

- Light speed
- Transverse wave

Tidal force between point masses



Perturbation h of the metric tensor g :

$$g_{\mu\nu} = \eta_{\mu\nu} + h_{\mu\nu}$$

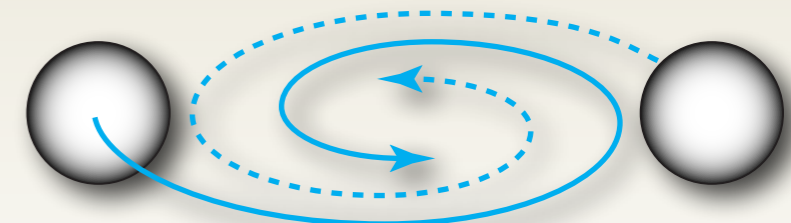
h is the strain of the spacetime.

$$\left(\nabla^2 - \frac{1}{c^2} \frac{\partial^2}{\partial t^2} \right) h_{\mu\nu} = 0$$

Typical Sources of GW

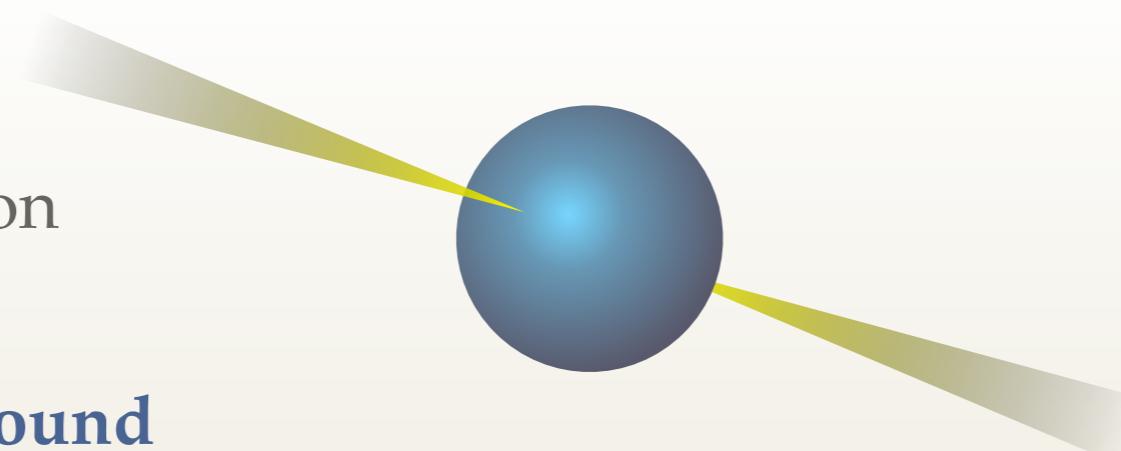
Occasionally events :

- Compact binary coalescence (CBC):
NS-NS, NS-BH, BH-BH
 Neutron star : NS, Blackhole : BH
- Supernovae
 BH Quasi-normal mode oscillation
- Pulsar glitch



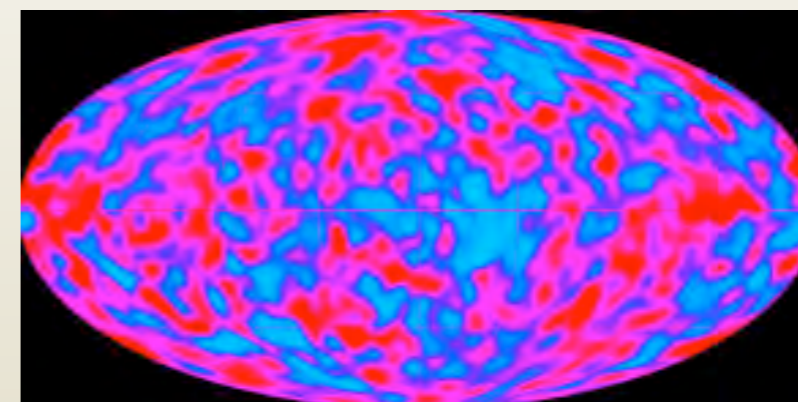
Continuous :

- Pulsar rotation
 Binary



Stochastic Background

- Early Universe
 Cosmic string
- Unresolvable astronomical origins



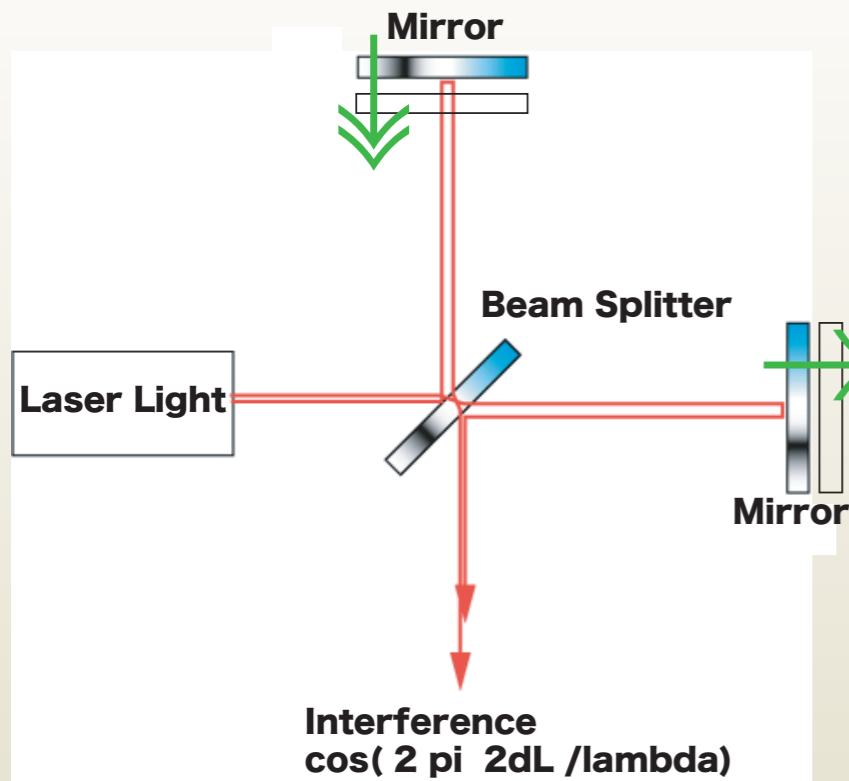
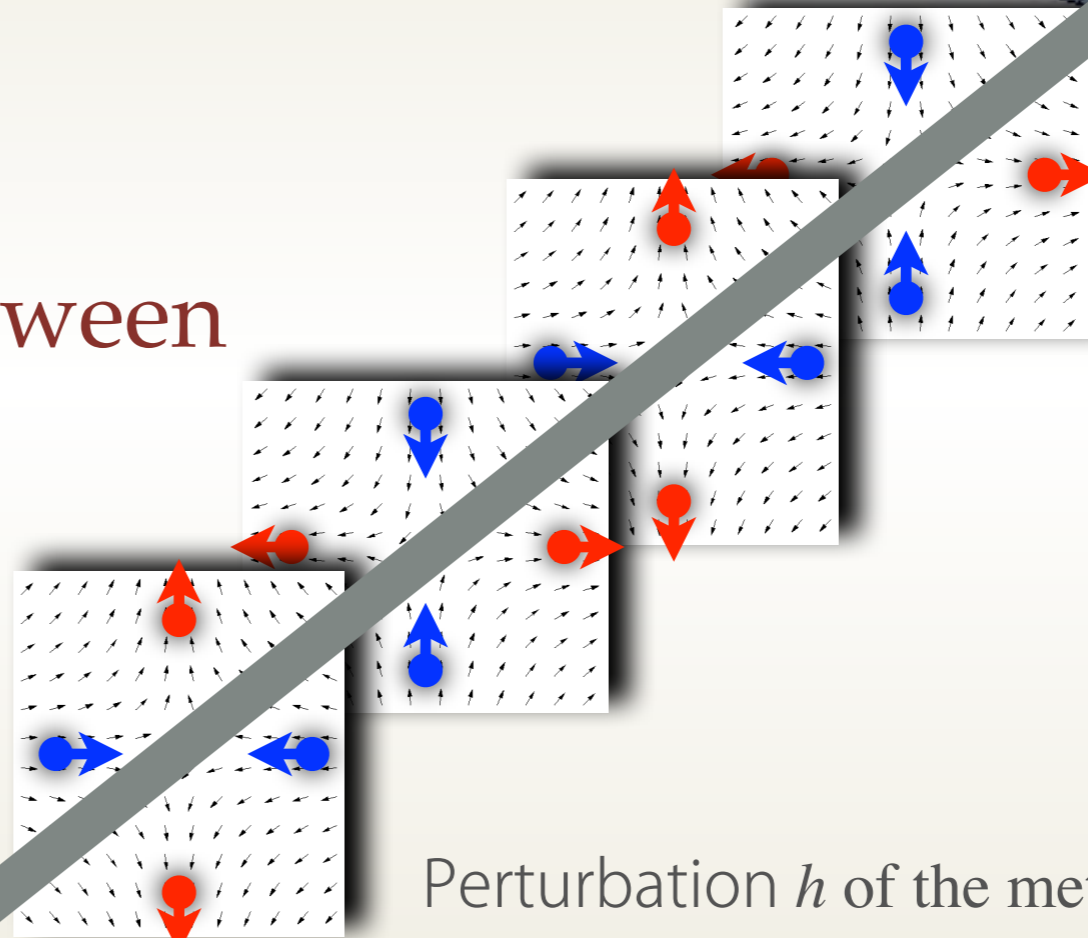
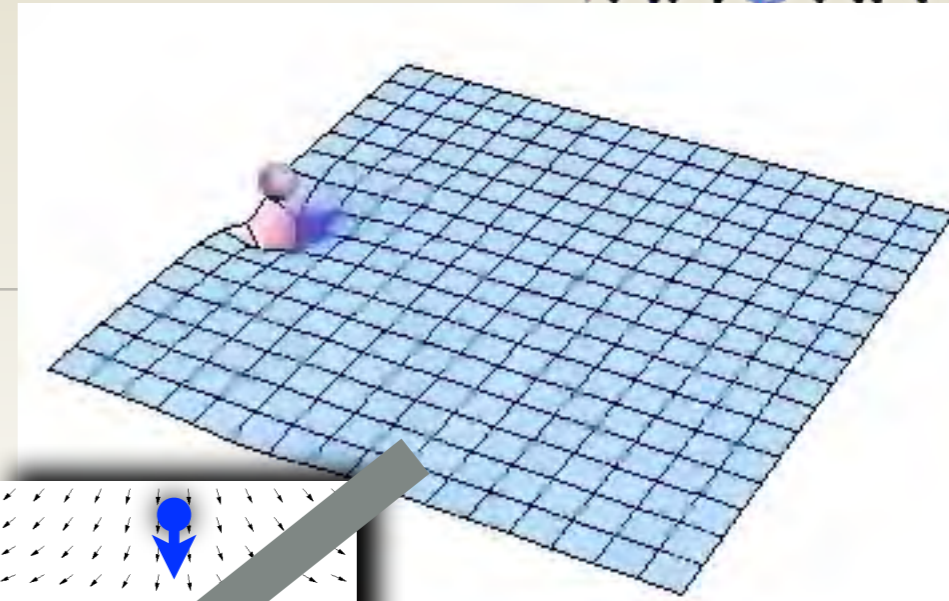
(& Unknown...)

How to detect GW

Important characters:

- Light speed
- Transverse wave

Tidal force between point masses



Perturbation h of the metric tensor g :

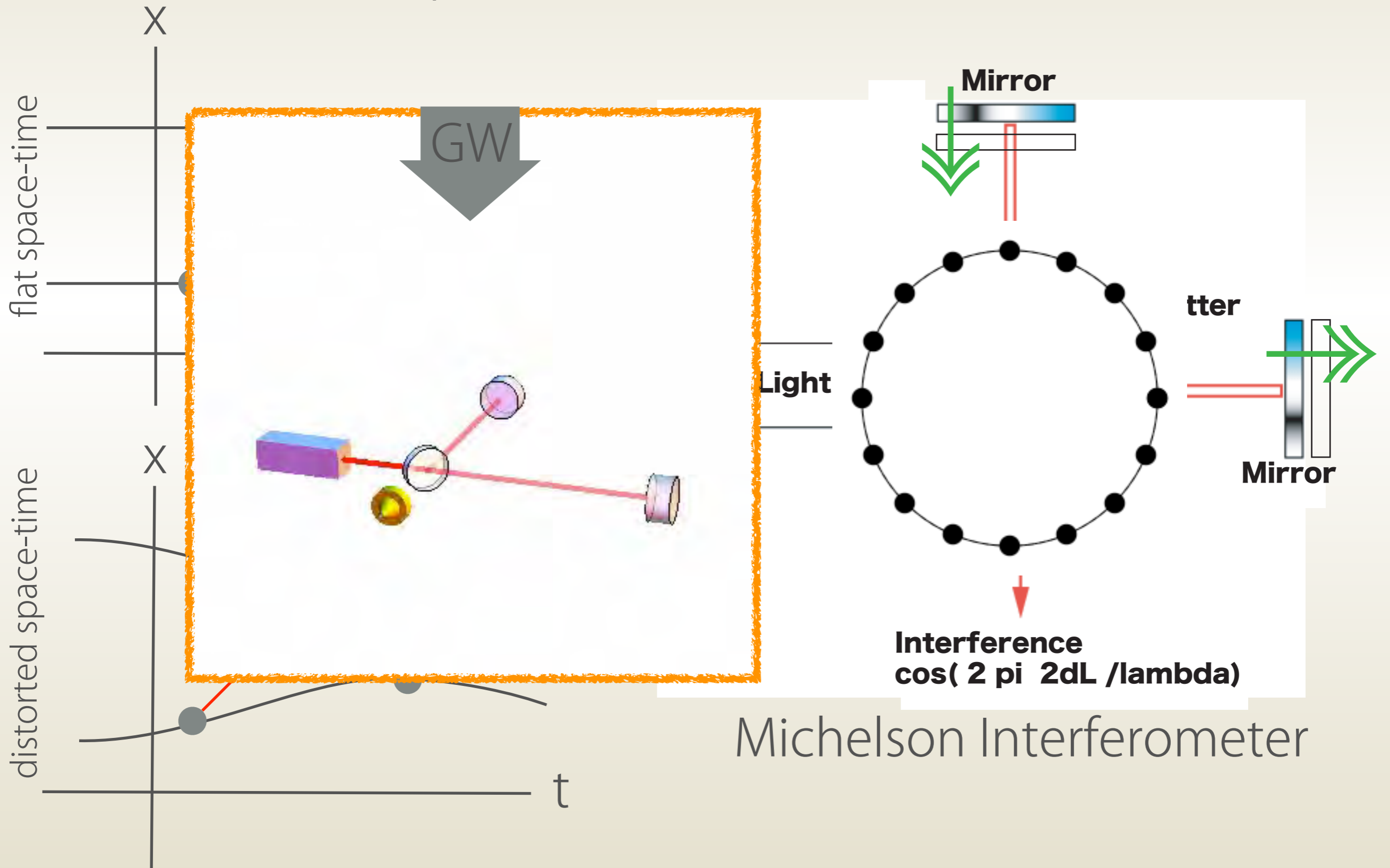
$$g_{\mu\nu} = \eta_{\mu\nu} + h_{\mu\nu}$$

h is the strain of the spacetime.

$$\left(\nabla^2 - \frac{1}{c^2} \frac{\partial^2}{\partial t^2} \right) h_{\mu\nu} = 0$$

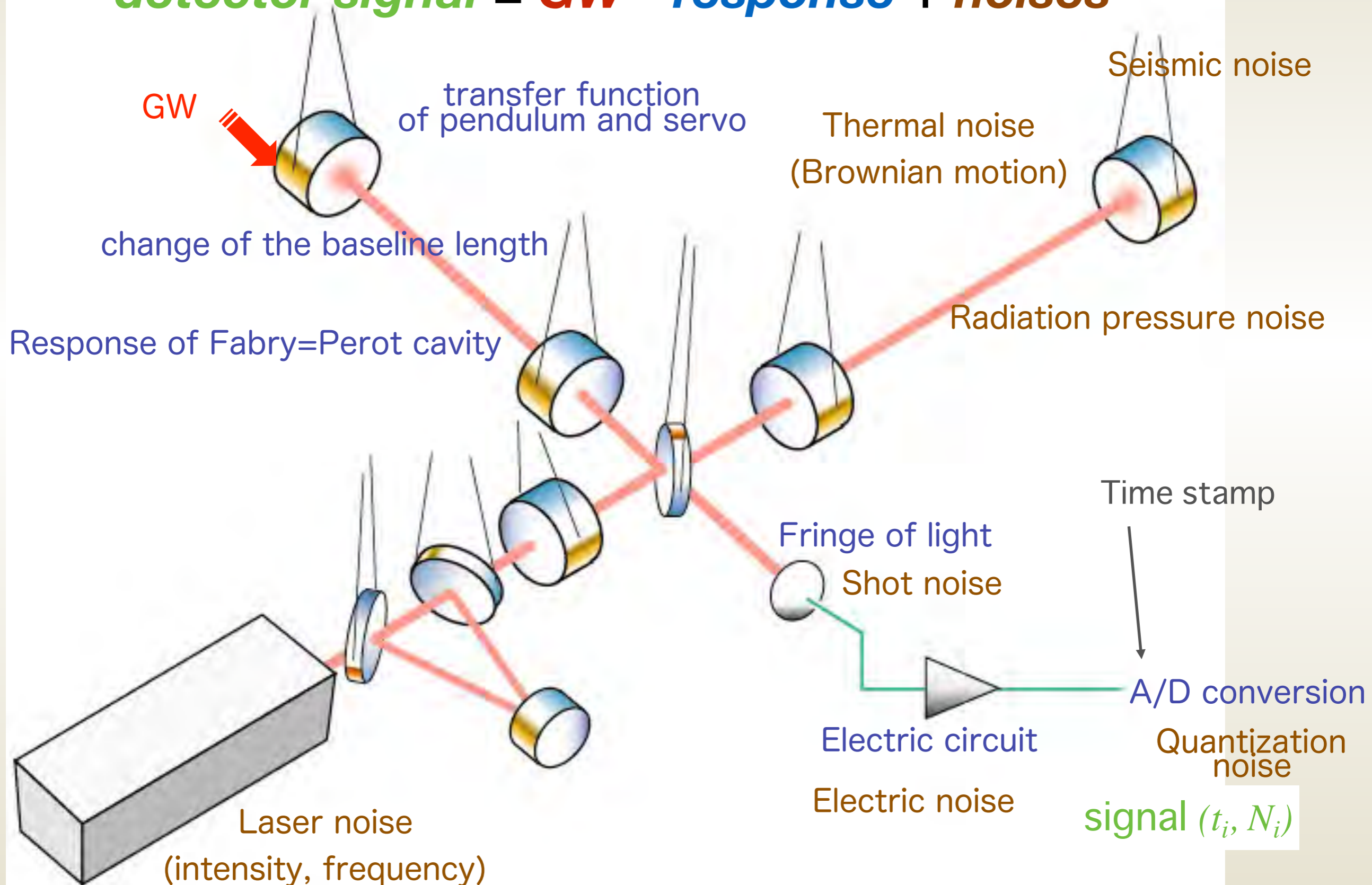
Fundamental of the detection

Free mass = suspended mirror



Schematics of Laser Interferometric Detector

$$\text{detector signal} = GW * \text{response} + \text{noises}$$



Global Network of GW detectors

GEO 600m



advanced LIGO
(Livingston) 4km



Virgo 3km
advanced Virgo



(Hanford) 4km



LIGO India

TAMA 300m
CLIO 100m

KAGRA 3km

Why we need many GW detectors ?

1. Localization of GW source direction

At least, Four or three detectors are necessary.

(depend on the relative direction and polarization of GW.)

We will use :

- - arrival time difference
- - amplitude ratio of detectors

GW150914 : $\sim 600 \text{ deg}^2$

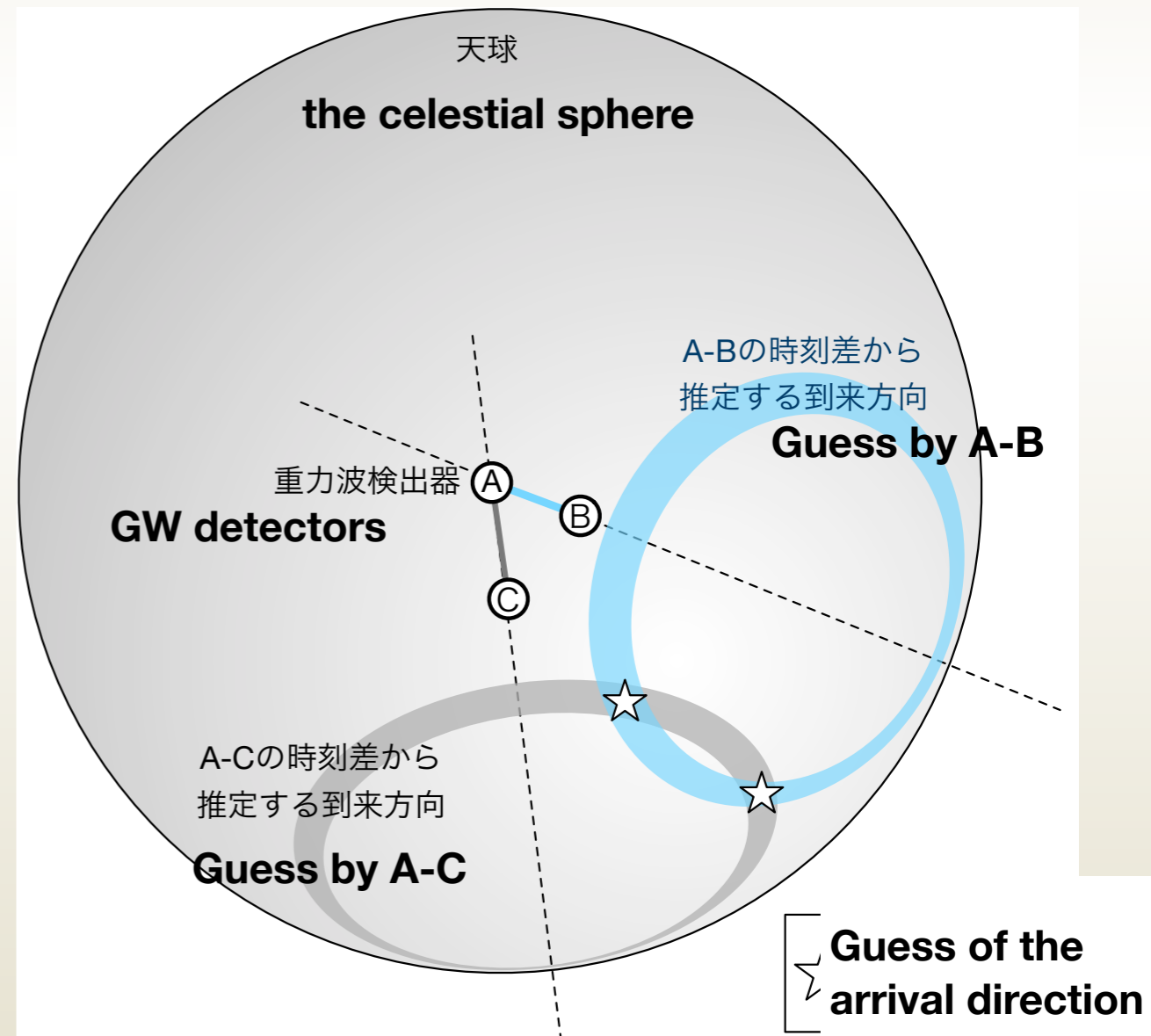
Average using

4 detectors : $\sim 5 \text{ deg}^2$

2. Sky coverage

3. Survey volume

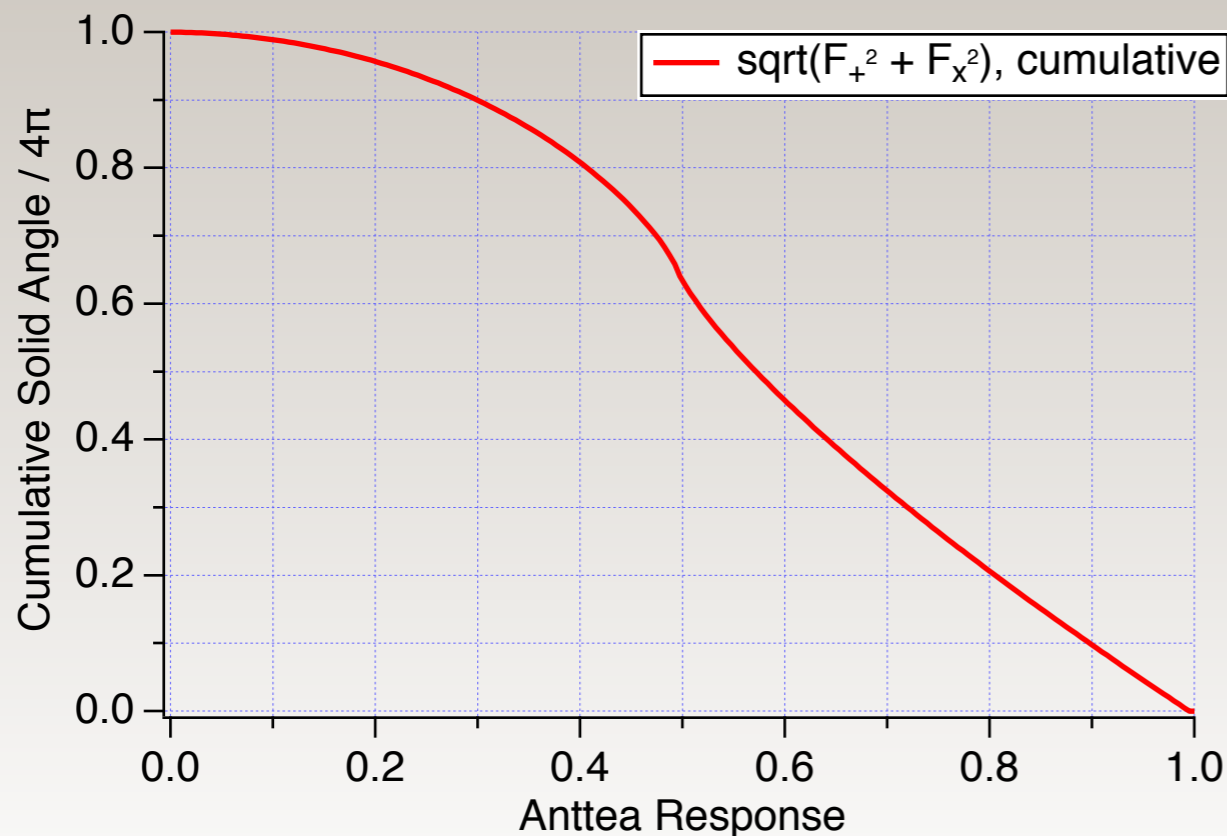
4. Duty time for operation



Antenna Pattern (Response for source direction and polarization)

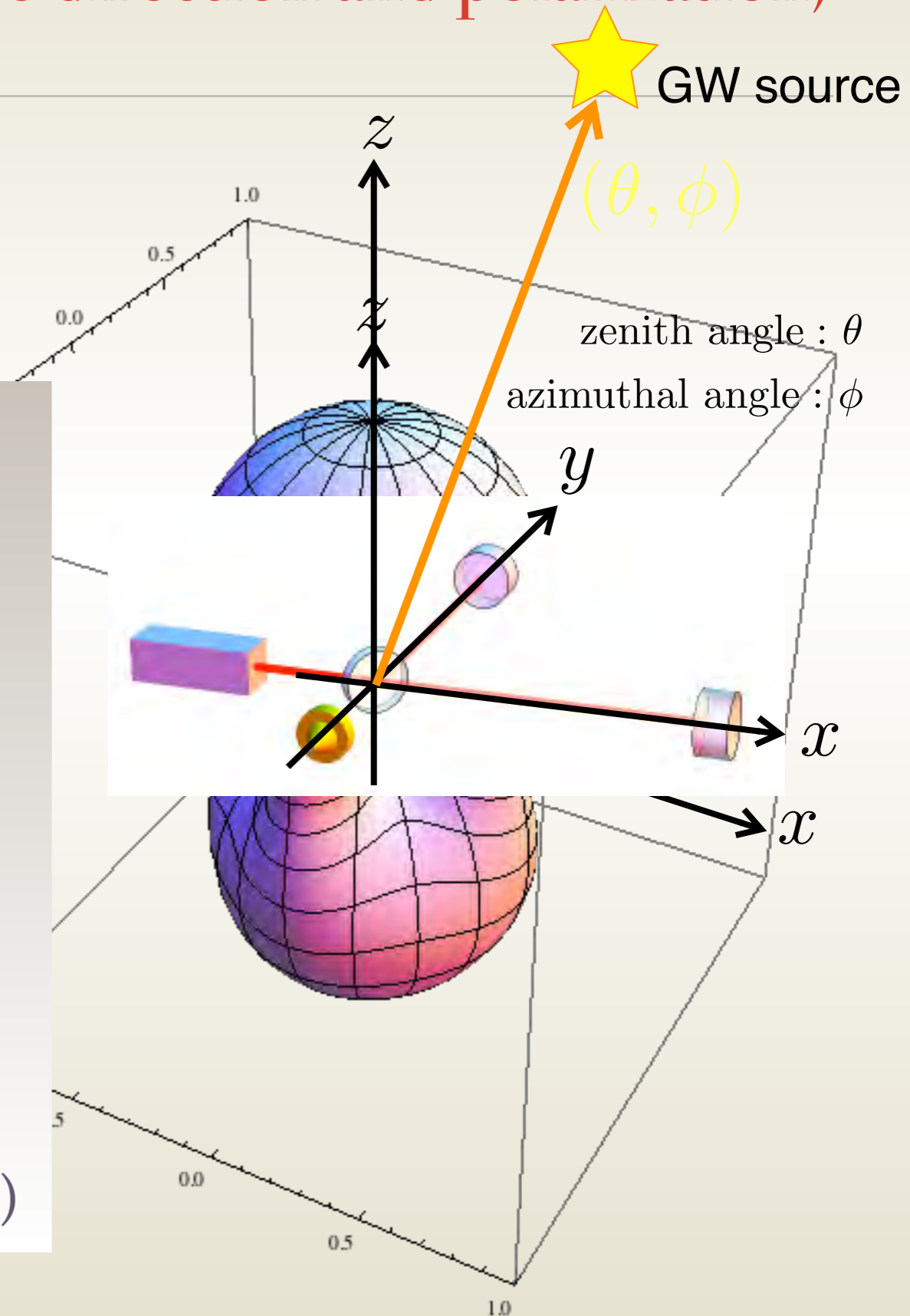
Interferometer's antenna pattern is widely spread as almost 'omni-directional'.

~70% sky coverage by response > 0.5



(目は悪いが、耳が悪いわけじゃ無い...^^;)

multi-detectors.



Sky coverage by detector network

LIGO (Hanford)

90

decl.[deg]

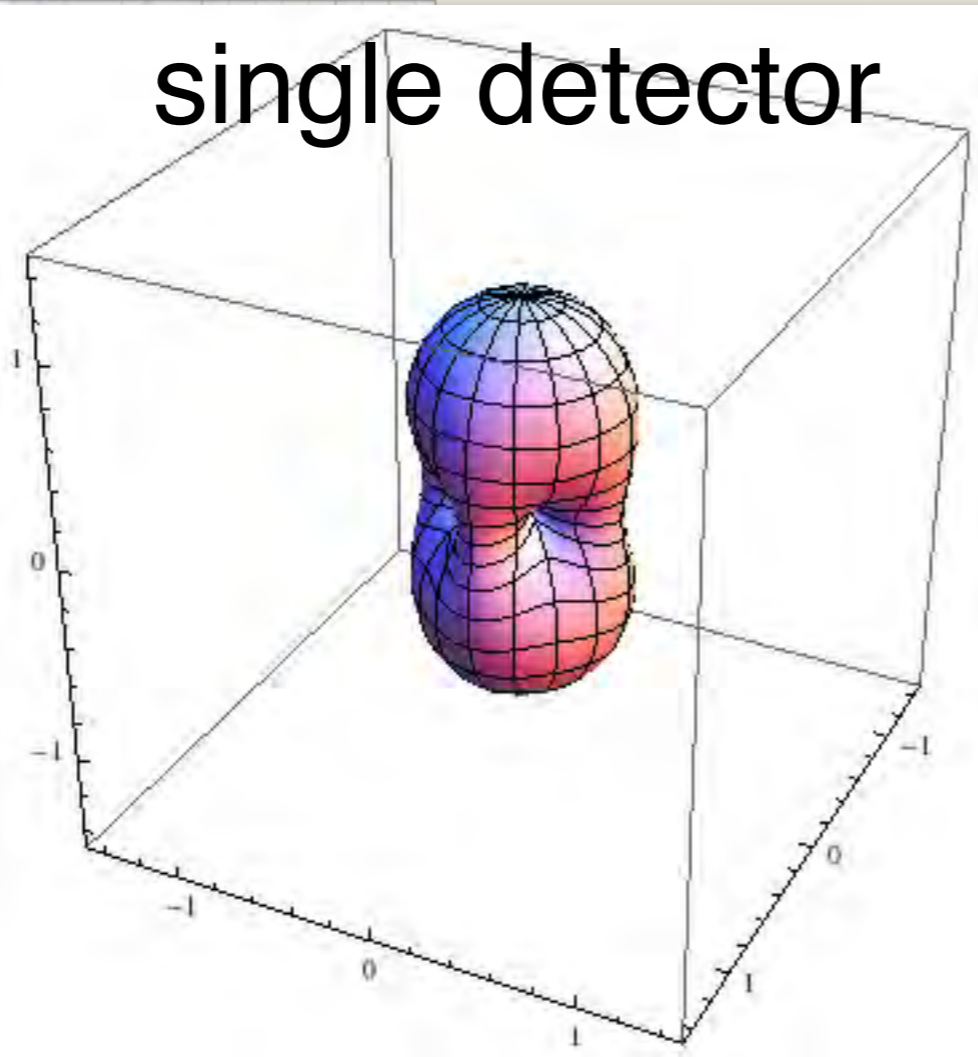
-90

-12

0

R.A.[hour]

single detector



ection of detectors
ford
ngston

: KAGRA+LIGO(Hanford)

90

decl.[deg]

-90

-12

0

12

R.A.[hour]

KAGRA

-12

0

12

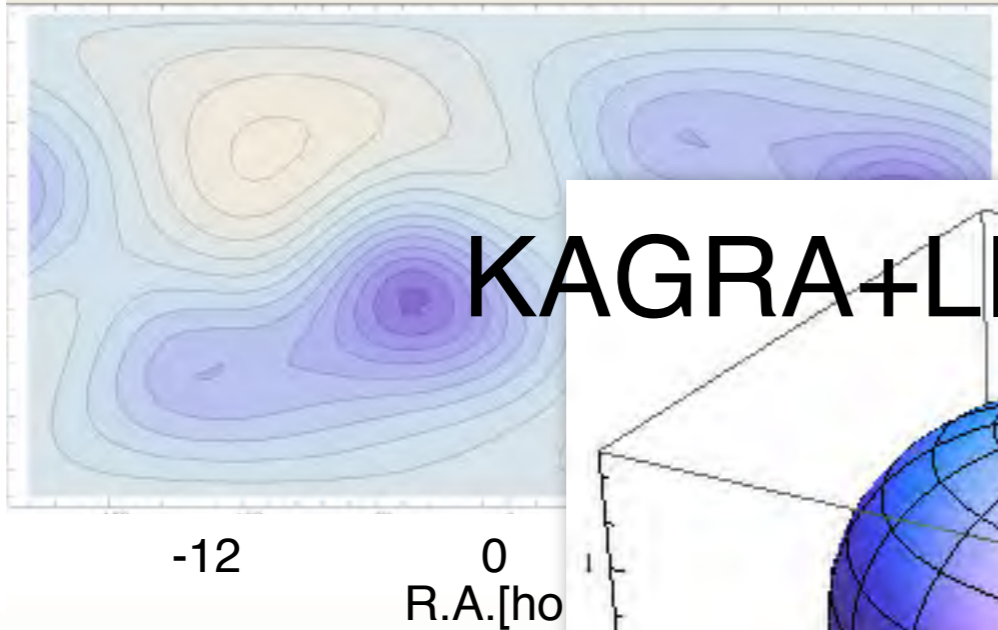
R.A.[hour]

KAGRA will make important role in the network,
with a complementary sensitivity map.

Sky coverage by detector network

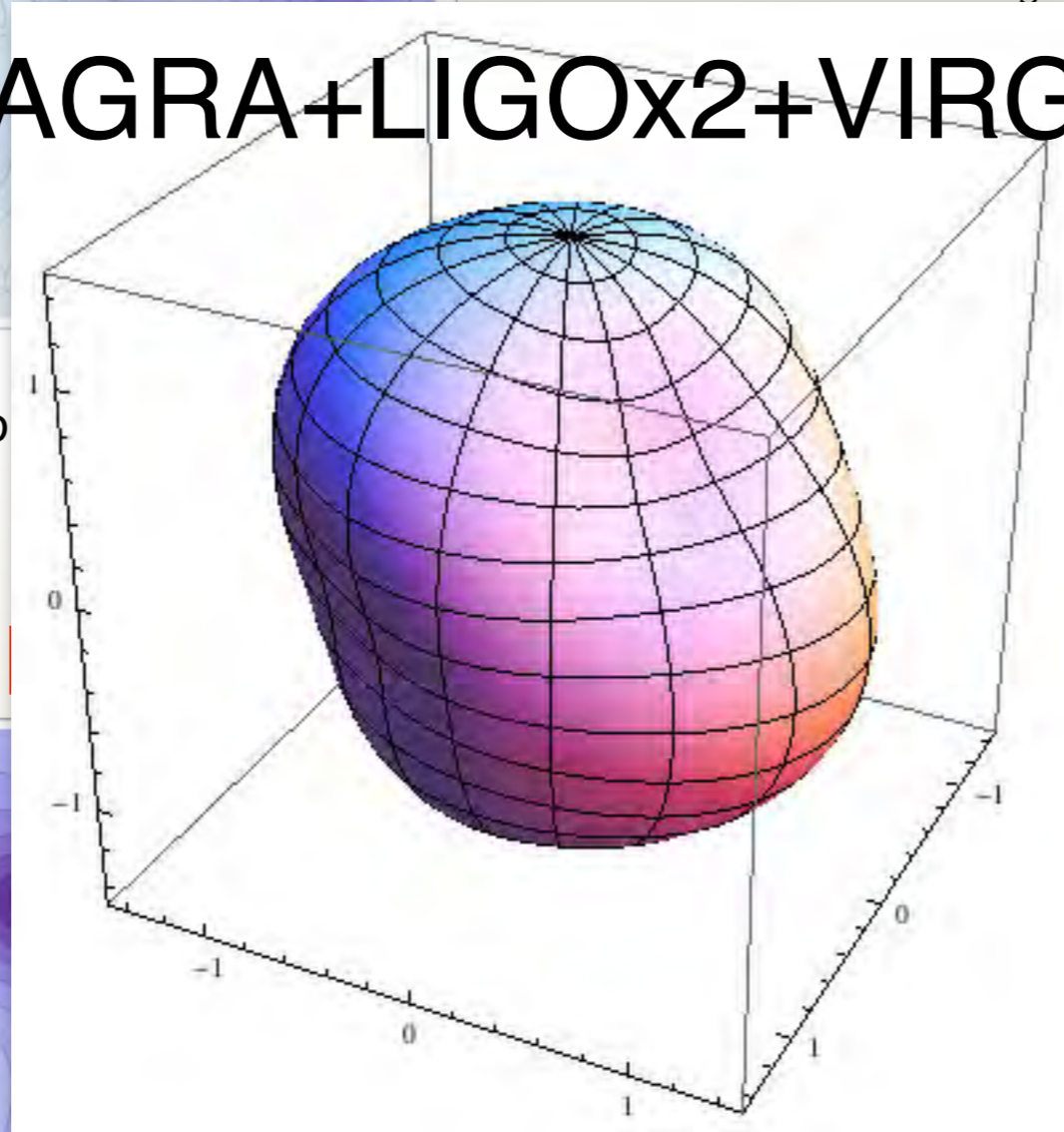
LIGO x2 + VIRGO

90
0
-90
decl.[deg]

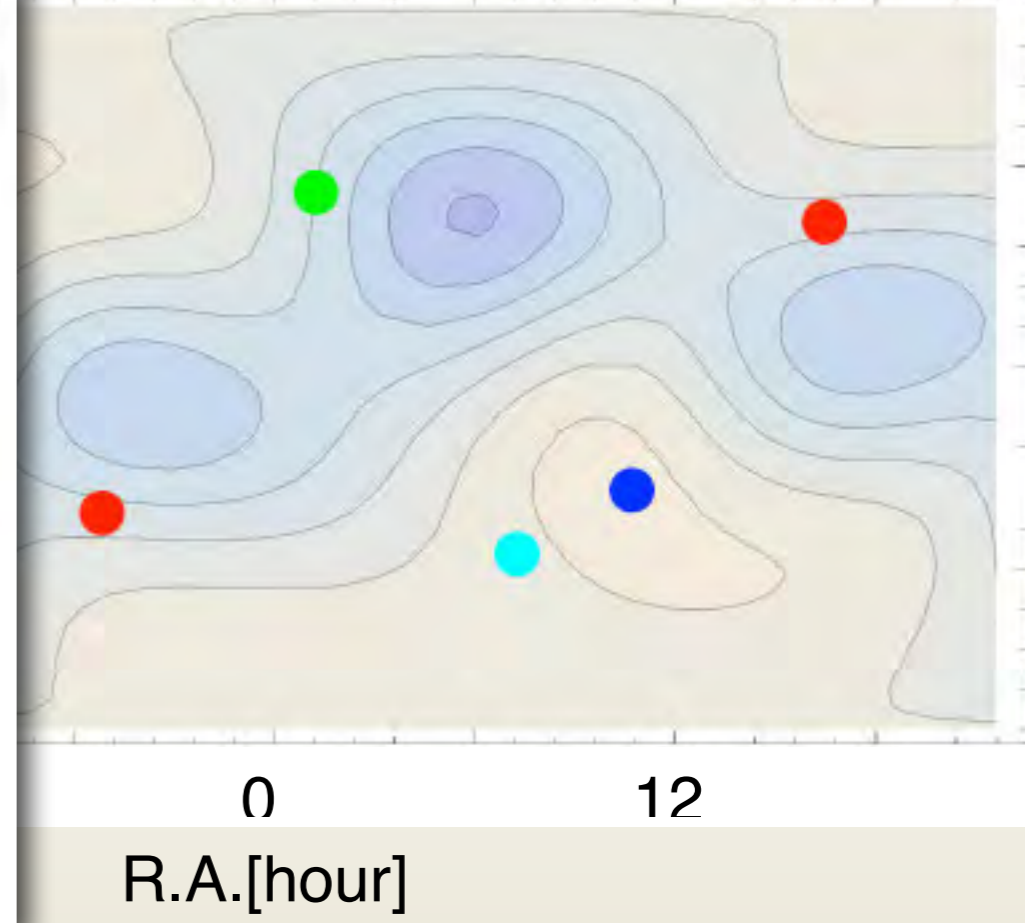


zenith direction of detectors
● LIGO Hanford
● LIGO Livingston

KAGRA+LIGOx2+VIRGO

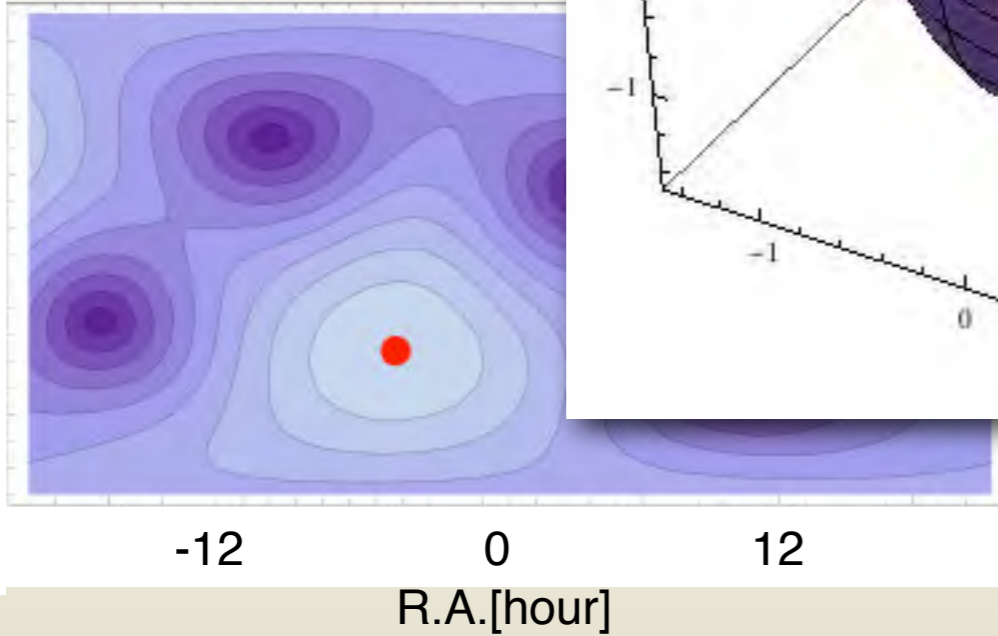


KAGRA+LIGOx2+VIRGO



KAGRA

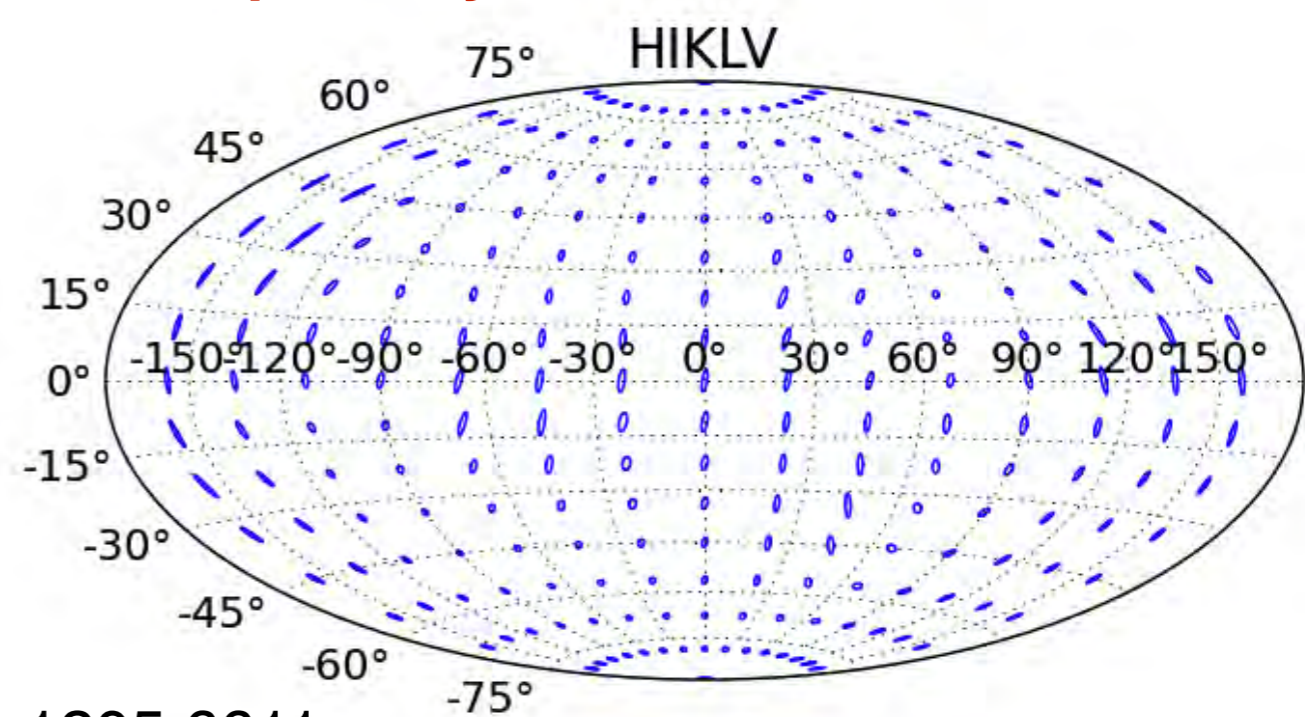
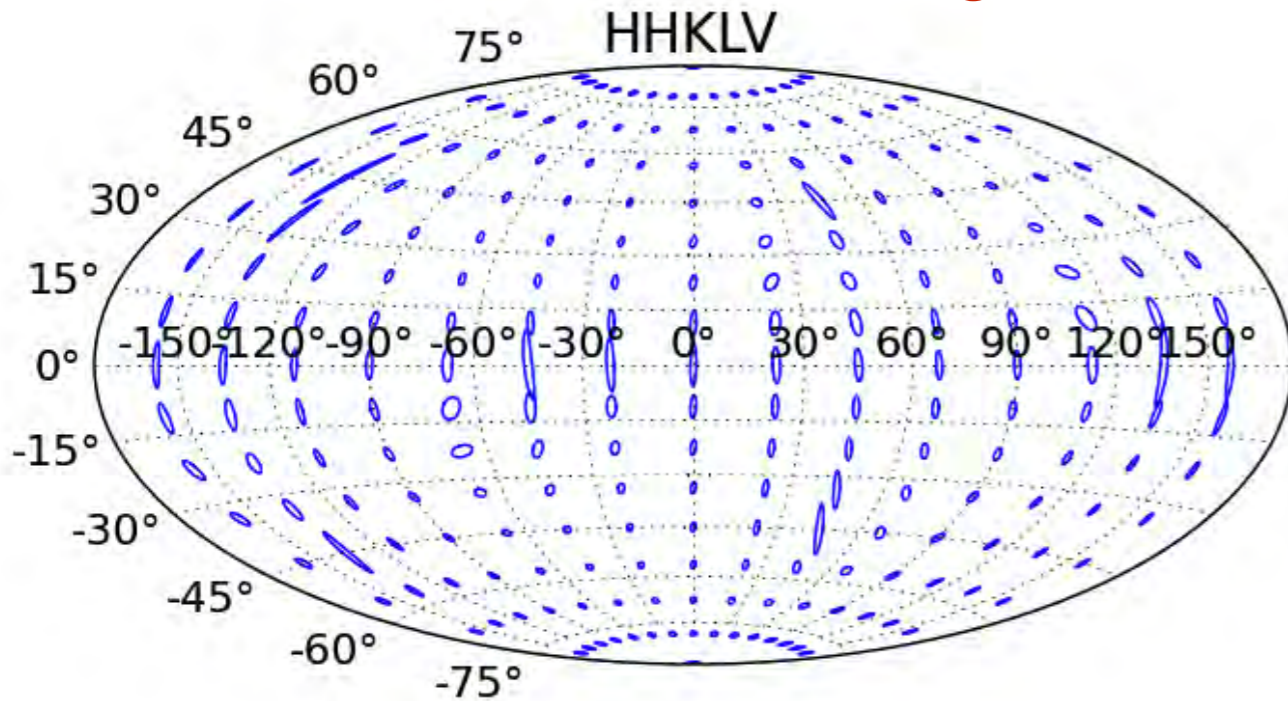
90
0
-90
decl.[deg]



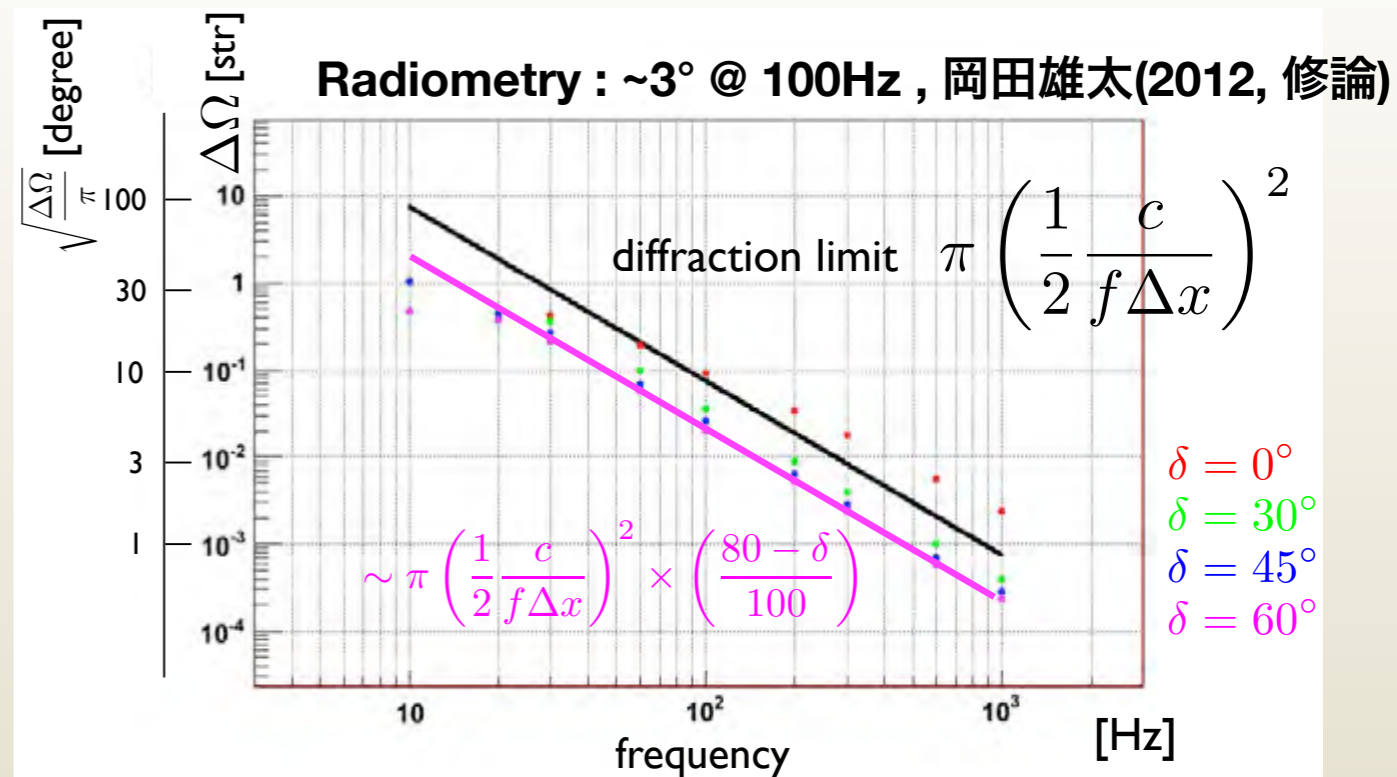
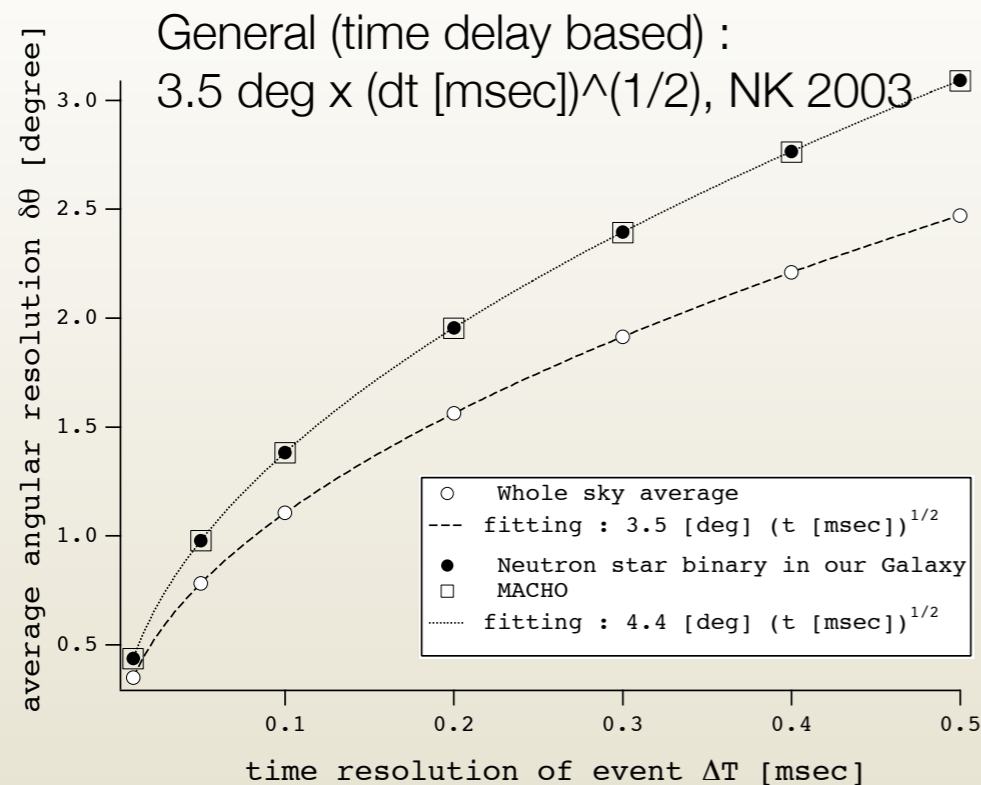
KAGRA will make important role in the network, with a complementary sensitivity map.

Arrival Direction

CBC : ~10 deg² resolution, at 160Mpc away, 5 detectors.

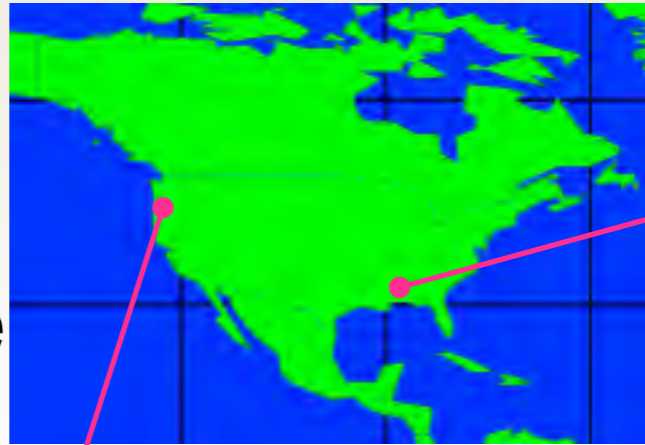


Fairhurst, arXivL1205.6611



LIGO and 1st GW observation

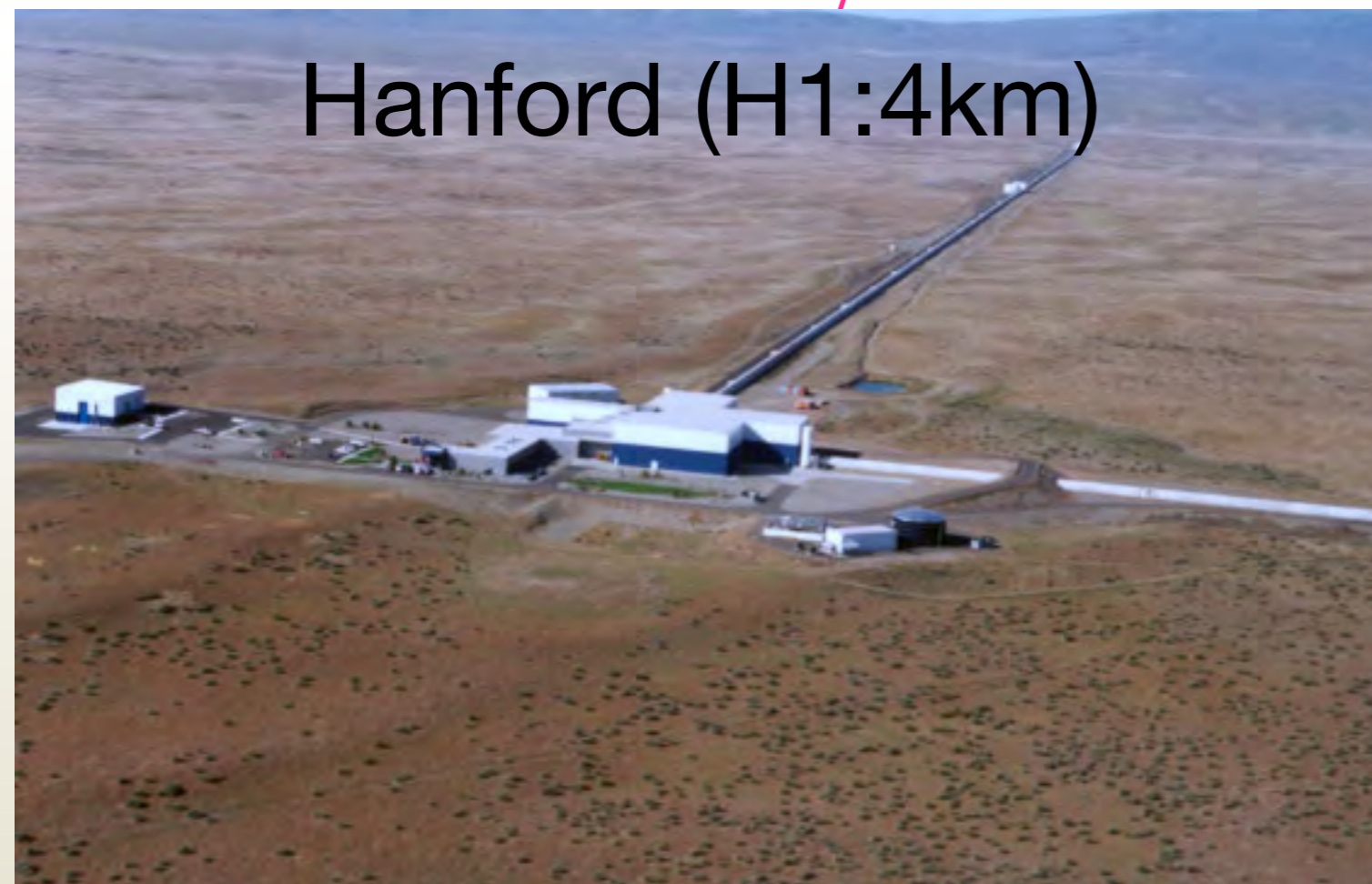
Laser
Interferometric
Gravitational-Wave
Observatory



Livingston (L1:4km)



Hanford (H1:4km)



O1 (Observation 1)
2015/9/18 - 2016/1/12
1100 hours

<http://www.ligo.org/>

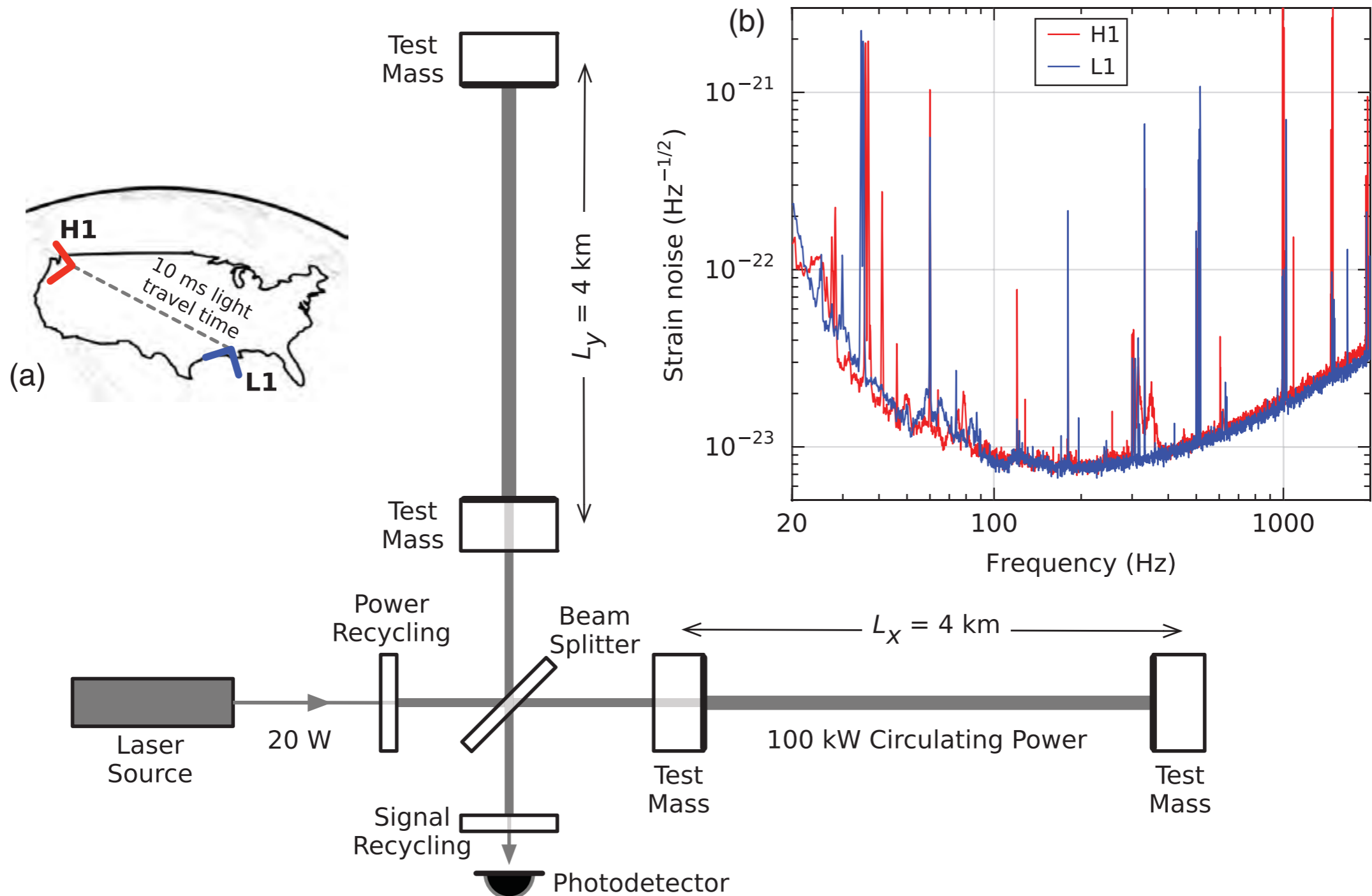


FIG. 3. Simplified diagram of an Advanced LIGO detector (not to scale). A gravitational wave propagating orthogonally to the detector plane and linearly polarized parallel to the 4-km optical cavities will have the effect of lengthening one 4-km arm and shortening the other during one half-cycle of the wave; these length changes are reversed during the other half-cycle. The output photodetector records these differential cavity length variations. While a detector's directional response is maximal for this case, it is still significant for most other angles of incidence or polarizations (gravitational waves propagate freely through the Earth). *Inset (a)*: Location and orientation of the LIGO detectors at Hanford, WA (H1) and Livingston, LA (L1). *Inset (b)*: The instrument noise for each detector near the time of the signal detection; this is an amplitude spectral density, expressed in terms of equivalent gravitational-wave strain

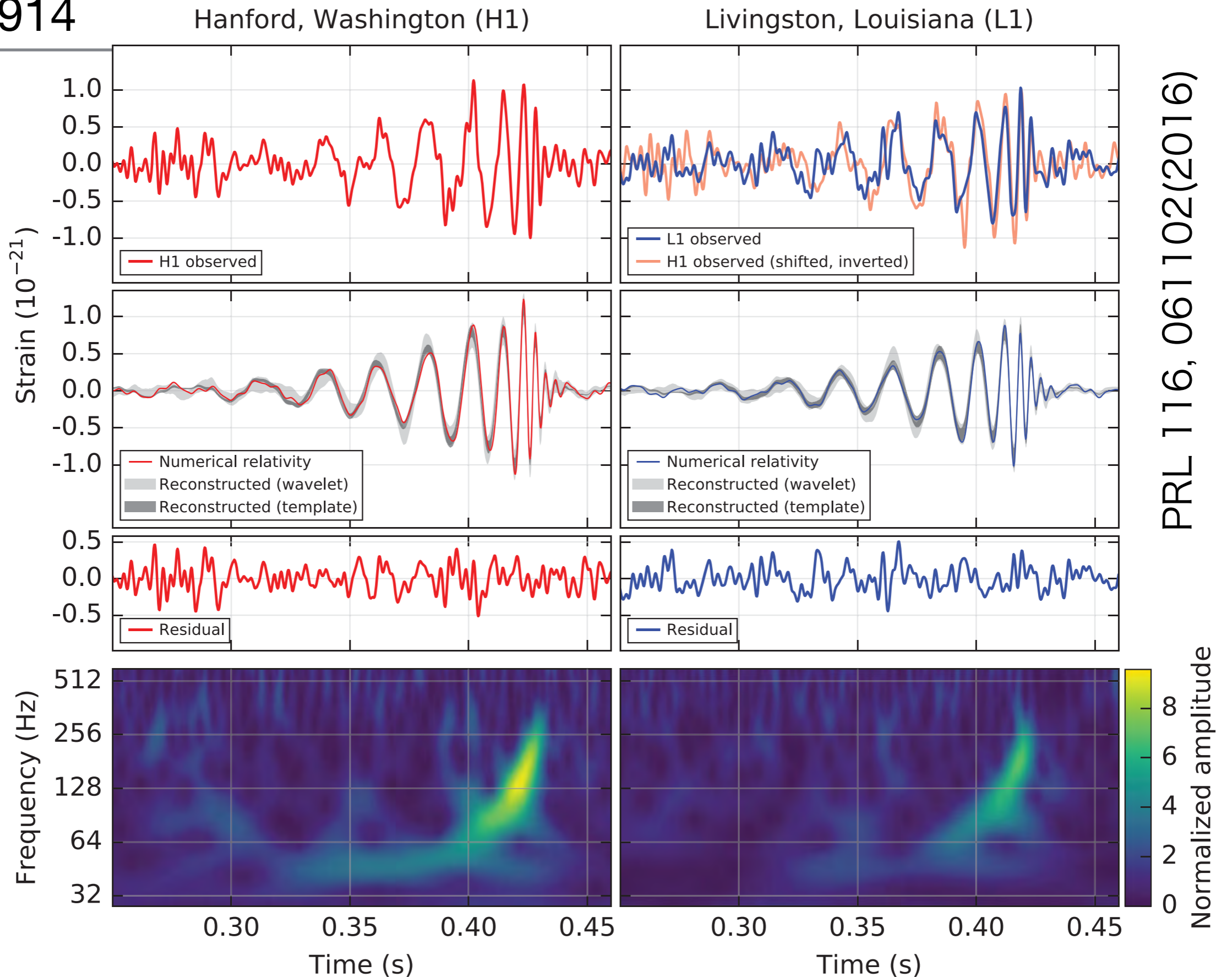


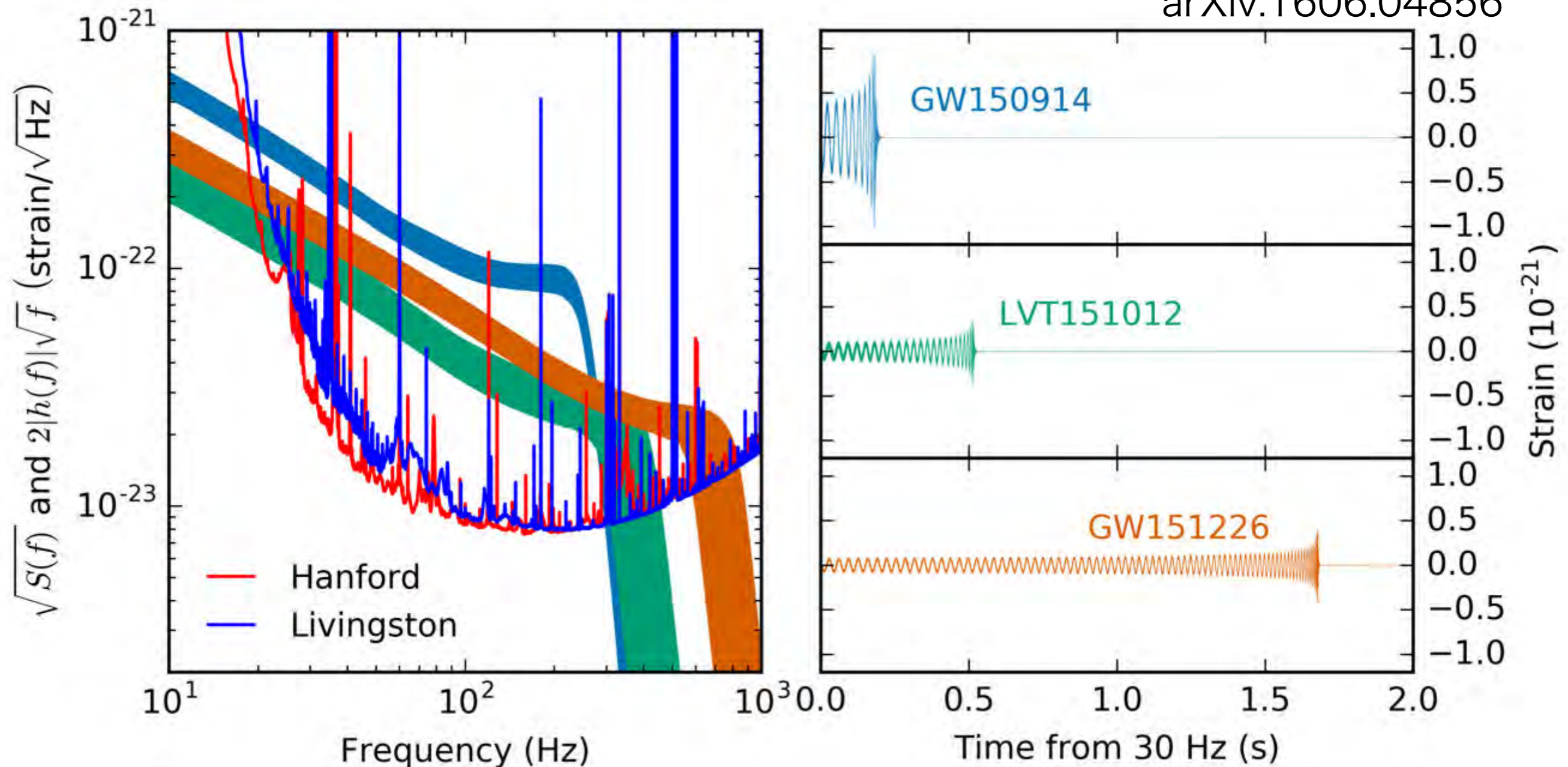
FIG. 1. The gravitational-wave event GW150914 observed by the LIGO Hanford (H1, left column panels) and Livingston (L1, right column panels) detectors. Times are shown relative to September 14, 2015 at 09:50:45 UTC. For visualization, all time series are filtered with a 35–350 Hz bandpass filter to suppress large fluctuations outside the detectors’ most sensitive frequency band, and band-reject

BH-BH in LIGO O1

- O1 (Observational run 1) : Sep.18, 2015 - Jan. 12, 2016

GW150914, GW151226 : BBH (Binary Black Hole) mergers

arXiv:1606.04856



Remarks : the observed GW events in LIGO O1

GW150914

GW151226

LVT150120

Event	GW150914	GW151226	LVT151012
Signal-to-noise ratio ρ	23.7	13.0	9.7
False alarm rate FAR/yr ⁻¹	$< 6.0 \times 10^{-7}$	$< 6.0 \times 10^{-7}$	0.37
p-value	7.5×10^{-8}	7.5×10^{-8}	0.045
Significance	$> 5.3 \sigma$	$> 5.3 \sigma$	1.7σ
Primary mass $m_1^{\text{source}} / M_\odot$	$36.2^{+5.2}_{-3.8}$	$14.2^{+8.3}_{-3.7}$	23^{+18}_{-6}
Secondary mass $m_2^{\text{source}} / M_\odot$	$29.1^{+3.7}_{-4.4}$	$7.5^{+2.3}_{-2.3}$	13^{+4}_{-5}
Chirp mass $\mathcal{M}^{\text{source}} / M_\odot$	$28.1^{+1.8}_{-1.5}$	$8.9^{+0.3}_{-0.3}$	$15.1^{+1.4}_{-1.1}$
Total mass $M^{\text{source}} / M_\odot$	$65.3^{+4.1}_{-3.4}$	$21.8^{+5.9}_{-1.7}$	37^{+13}_{-4}
Effective inspiral spin χ_{eff}	$-0.06^{+0.14}_{-0.14}$	$0.21^{+0.20}_{-0.10}$	$0.0^{+0.3}_{-0.2}$
Final mass $M_f^{\text{source}} / M_\odot$	$62.3^{+3.7}_{-3.1}$	$20.8^{+6.1}_{-1.7}$	35^{+14}_{-4}
Final spin a_f	$0.68^{+0.05}_{-0.06}$	$0.74^{+0.06}_{-0.06}$	$0.66^{+0.09}_{-0.10}$
Radiated energy $E_{\text{rad}} / (M_\odot c^2)$	$3.0^{+0.5}_{-0.4}$	$1.0^{+0.1}_{-0.2}$	$1.5^{+0.3}_{-0.4}$
Peak luminosity $\ell_{\text{peak}} / (\text{erg s}^{-1})$	$3.6^{+0.5}_{-0.4} \times 10^{56}$	$3.3^{+0.8}_{-1.6} \times 10^{56}$	$3.1^{+0.8}_{-1.8} \times 10^{56}$
Luminosity distance D_L / Mpc	420^{+150}_{-180}	440^{+180}_{-190}	1000^{+500}_{-500}
Source redshift z	$0.09^{+0.03}_{-0.04}$	$0.09^{+0.03}_{-0.04}$	$0.20^{+0.09}_{-0.09}$
Sky localization $\Delta\Omega / \text{deg}^2$	230	850	1600

Note : GW150914 in [Jy]

Using the fits to numerical simulations of binary black hole mergers in [92,93], we provide estimates of the mass and spin of the final black hole, the total energy radiated in gravitational waves, and the peak gravitational-wave luminosity [39]. The estimated total energy radiated in gravitational waves is $3.0_{-0.5}^{+0.5} M_{\odot} c^2$. The system reached a peak gravitational-wave luminosity of $3.6_{-0.4}^{+0.5} \times 10^{56}$ erg/s, equivalent to $200_{-20}^{+30} M_{\odot} c^2 / s$.

PRL.116.061102

energy flux : 3.6×10^{56} erg / s

(cf: total energy : ~ 3 Msolar $\sim 5.4 \times 10^{54}$ erg)

luminosity distance : 420 Mpc = 1.3×10^{27} cm

bandwidth : ~ 300 Hz

$\sim 5.7 \times 10^{21}$ Jy

LIGO O2 run started

<https://www.ligo.caltech.edu/news/2016-11-30>

from Nov.30,
2016.

Scheduled as
6 months



LIGO Hanford and LIGO Livingston Observatories. Credit: Caltech/MIT/LIGO Lab.

LIGO Resumes Search for Gravitational Waves

News Release • November 30, 2016

After a series of upgrades, the twin detectors of LIGO, the Laser Interferometer Gravitational-wave Observatory, have turned back on and resumed their search for ripples in the fabric of space and time known as gravitational waves. LIGO transitioned from engineering test runs to science observations at 8 a.m. Pacific Standard Time on November 30.



KAGRA



Mine Work Style

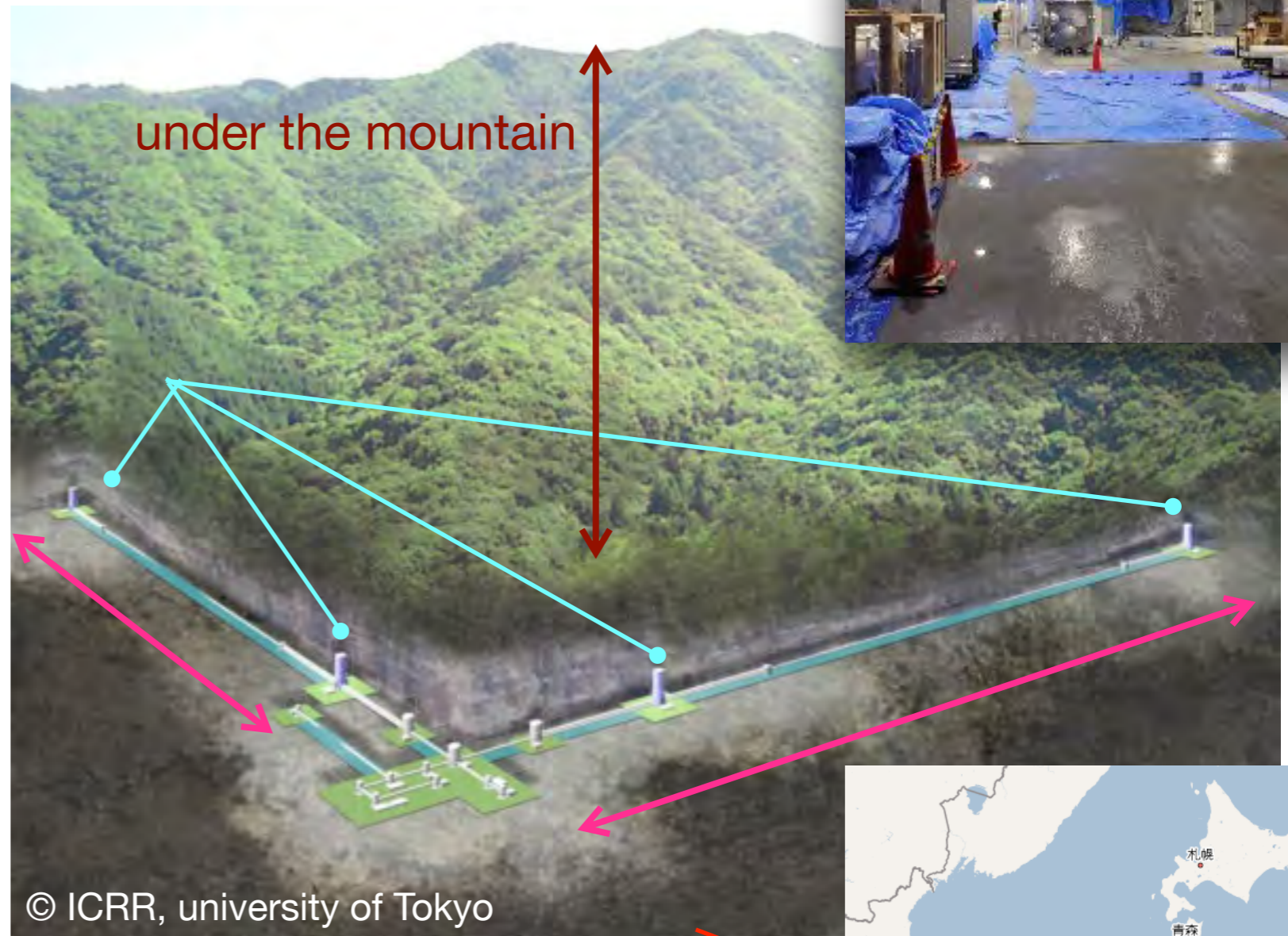
- Work cloths, work gloves, work boots
- Helmets
- Head ligts
- Reflect vests
- Oxygen sensors
- Electric bicycles

KAGRA



~280 persons (>80 affiliations)

- ▶ Underground
 - ▶ Kamioka mine
 - ▶ **Silent and Stable**
- ▶ Cryogenic mirror
 - ▶ 20K
 - ▶ **Sapphire substrate**
- ▶ 3km baseline



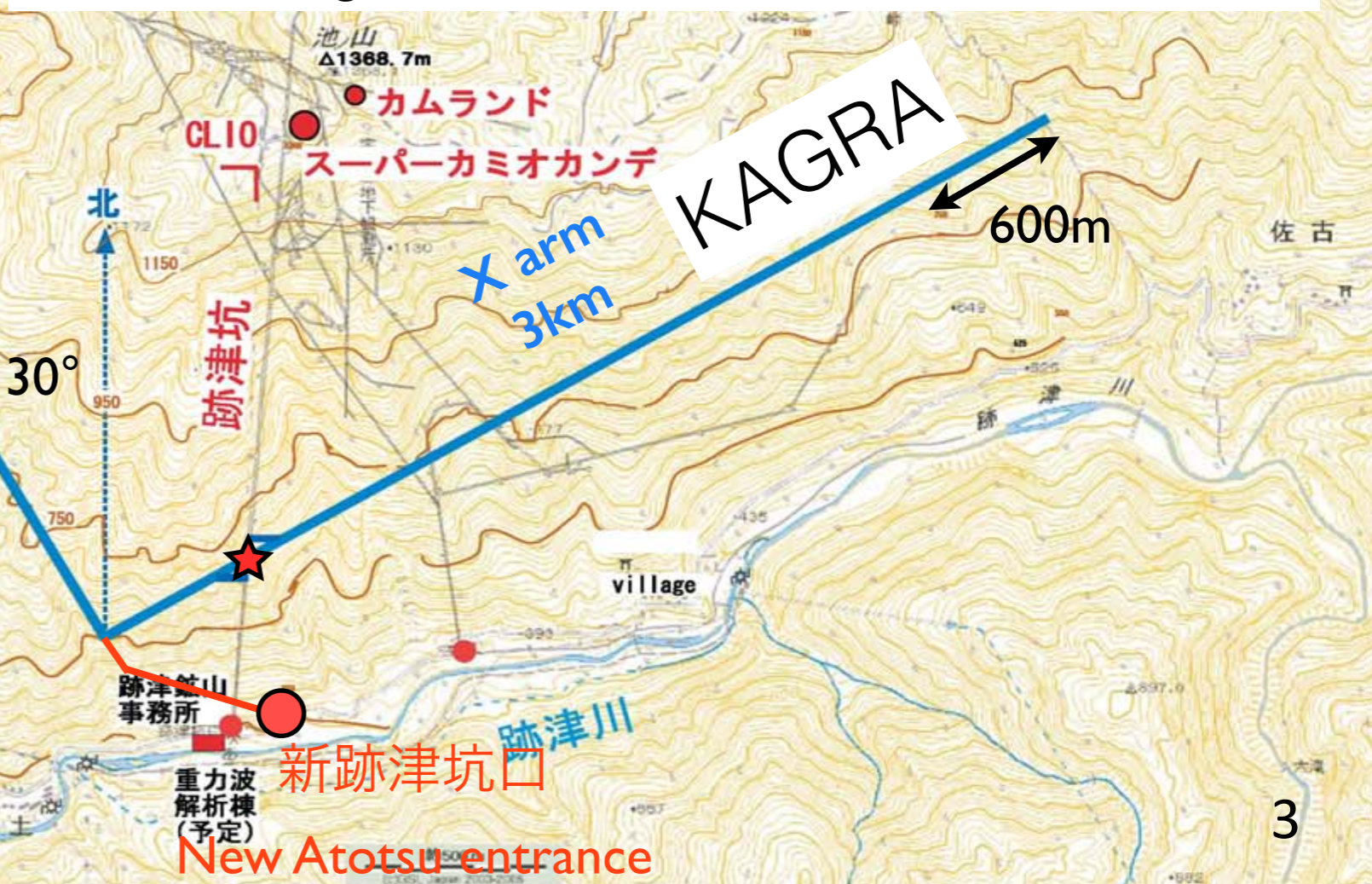
© ICRR, university of Tokyo

- ▶ Schedule
 - ▶ 2010 : Construction start
 - ▶ early 2016 : 1st operation in normal temperature
 - ▶ early 2018 : cryogenic operation



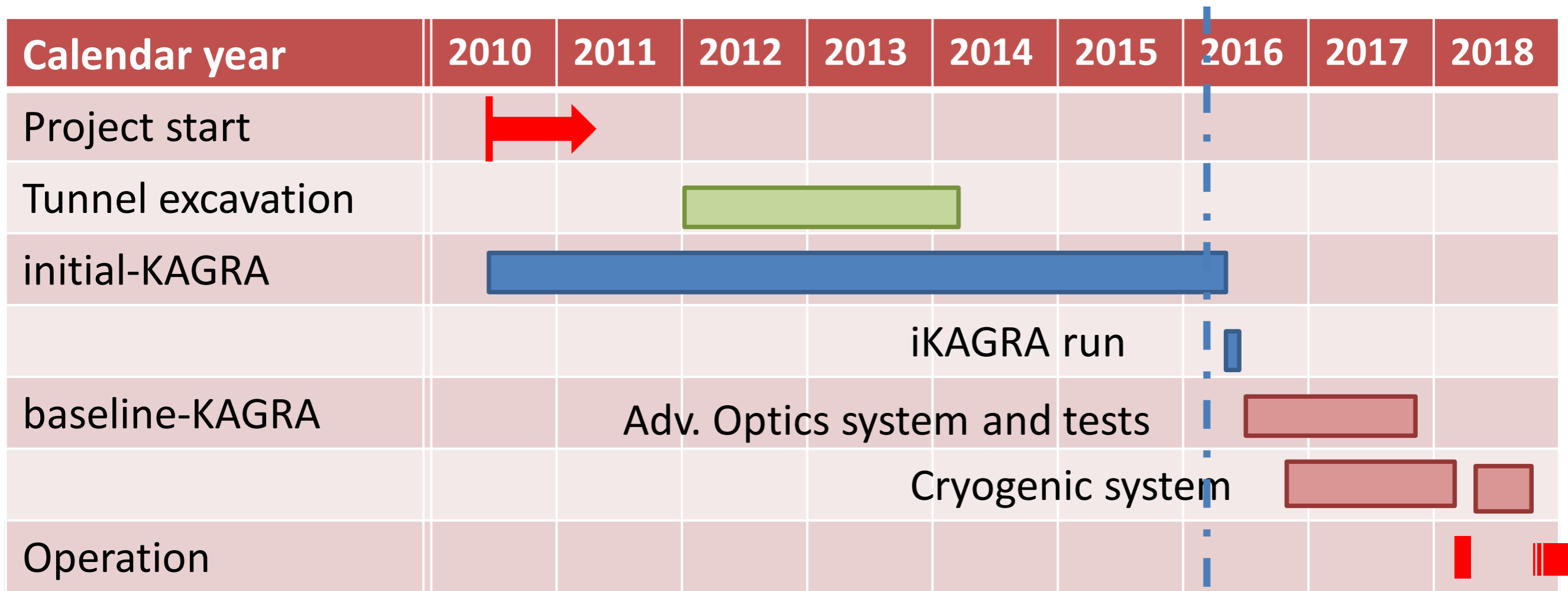
Location of Center (BS)

- latitude: 36.41°N , longitude: 137.31° .
- Y arm direction: 28.31 deg. from the North.
- Height from the sea level : about 372m.
- 2 entrances for the experiment room.
- Center, Xend, Yend are inside more than 200m from the surface of the mountain.
- Tunnel floor is tilted by $1/300$ for natural water drainage.
- Height of the Xend: 382.095m.
- Height of the Yend: 362.928m.



Tilt: $1/300$

★ Water drain point



iKAGRA

- We had test run at March and April 2016.

bKAGRA

- Advanced optics and cryogenic system are in progress.
- Cryogenic operation ~end of FY2017



Shin-Atotsu entrance
(2017.1.7)

Tunnel excavation completed at March, 2014.



Photo : KAGRA tunnel, center corner



at July 6, 2015

(from almost same viewpoint of Oct.2014)

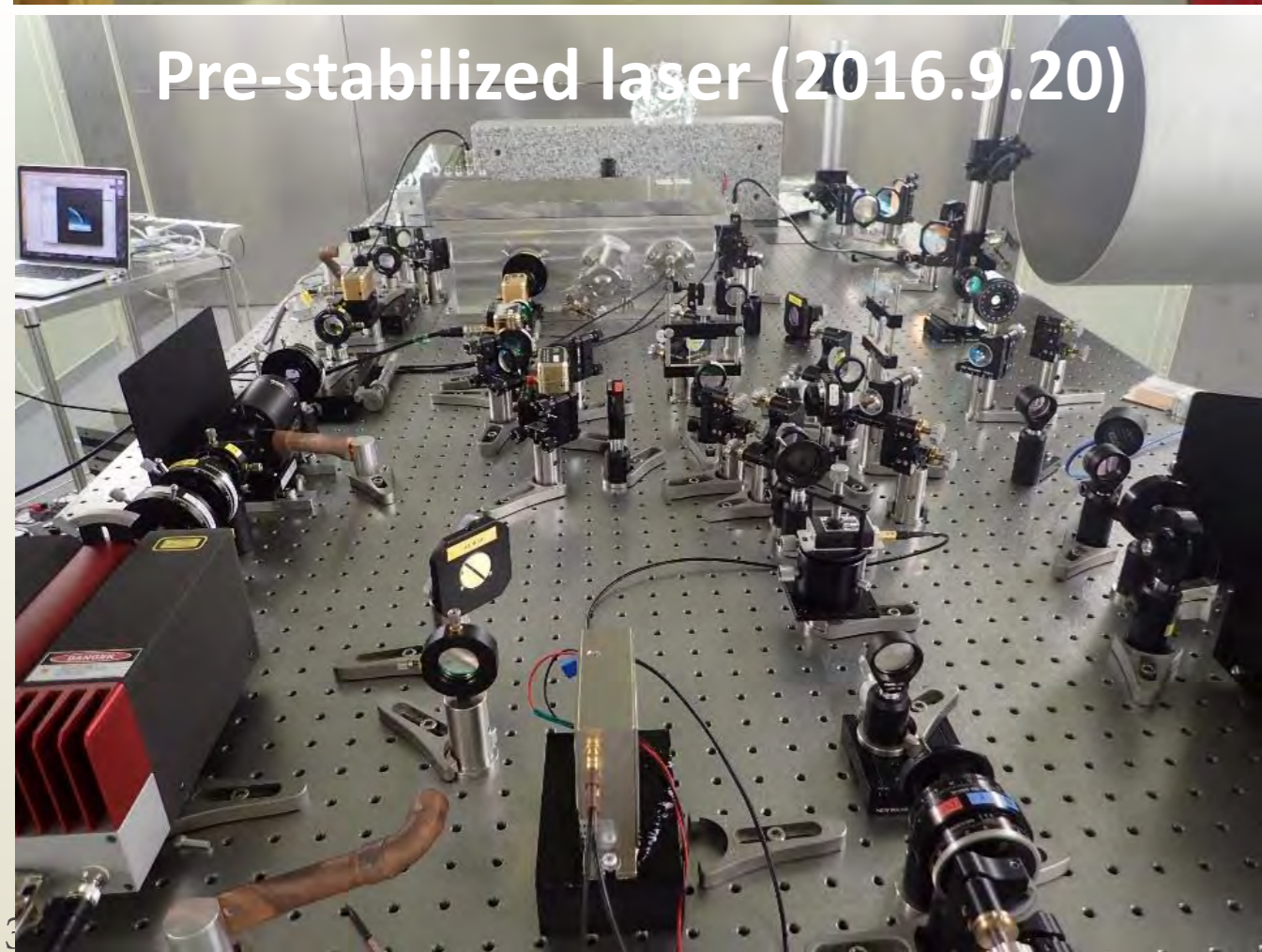
Central area (2017.1.7)



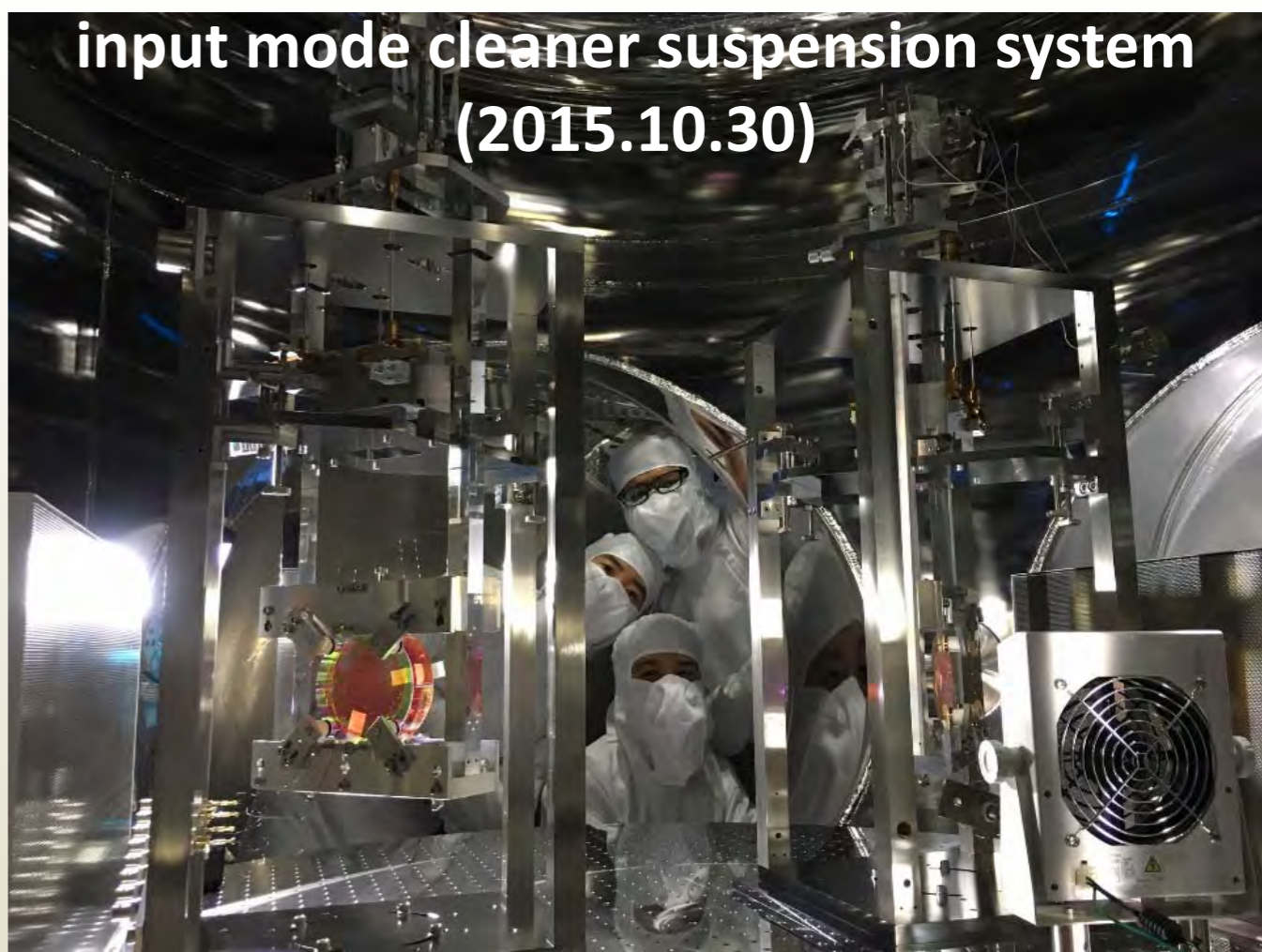
Cryostat for input test mass (2016.9.20)



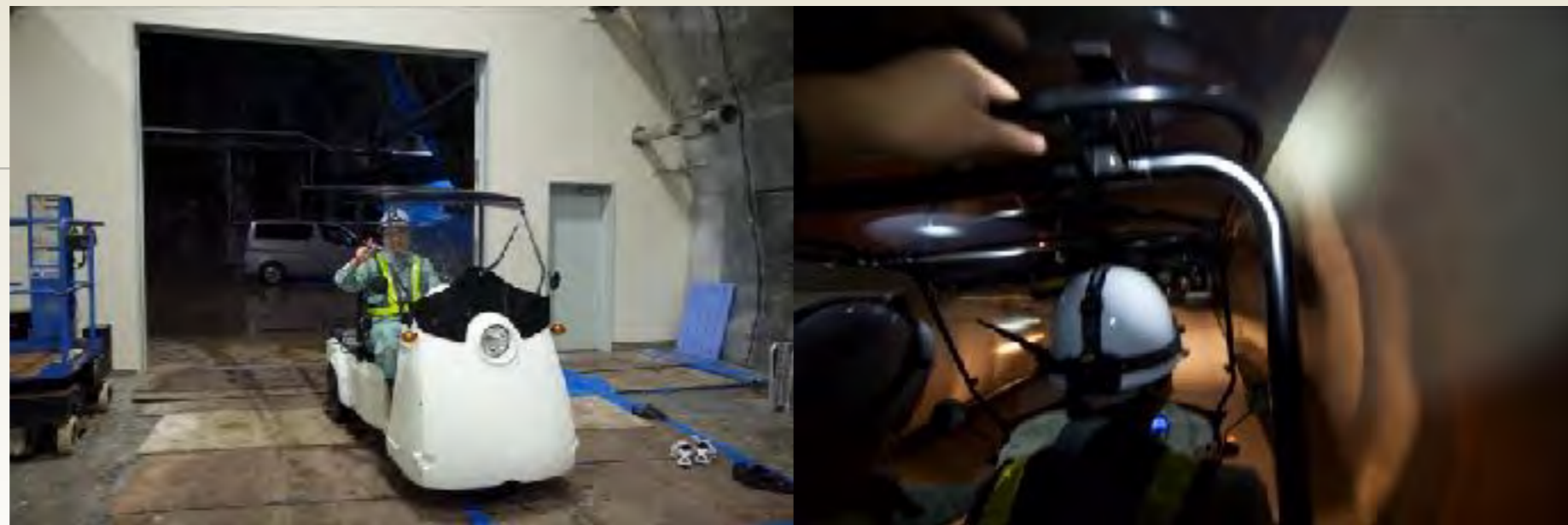
Pre-stabilized laser (2016.9.20)



input mode cleaner suspension system (2015.10.30)



Tunnel



Drive by Electric car



mid of the X-arm



Upper floor
End room

(almost) end of X-arm

Electronics hut



The electronics and computer hut inside the KAGRA tunnel



DC power supply



frame writer -> transfer



I/O interface



Fiber connection from/to the surface

Control room

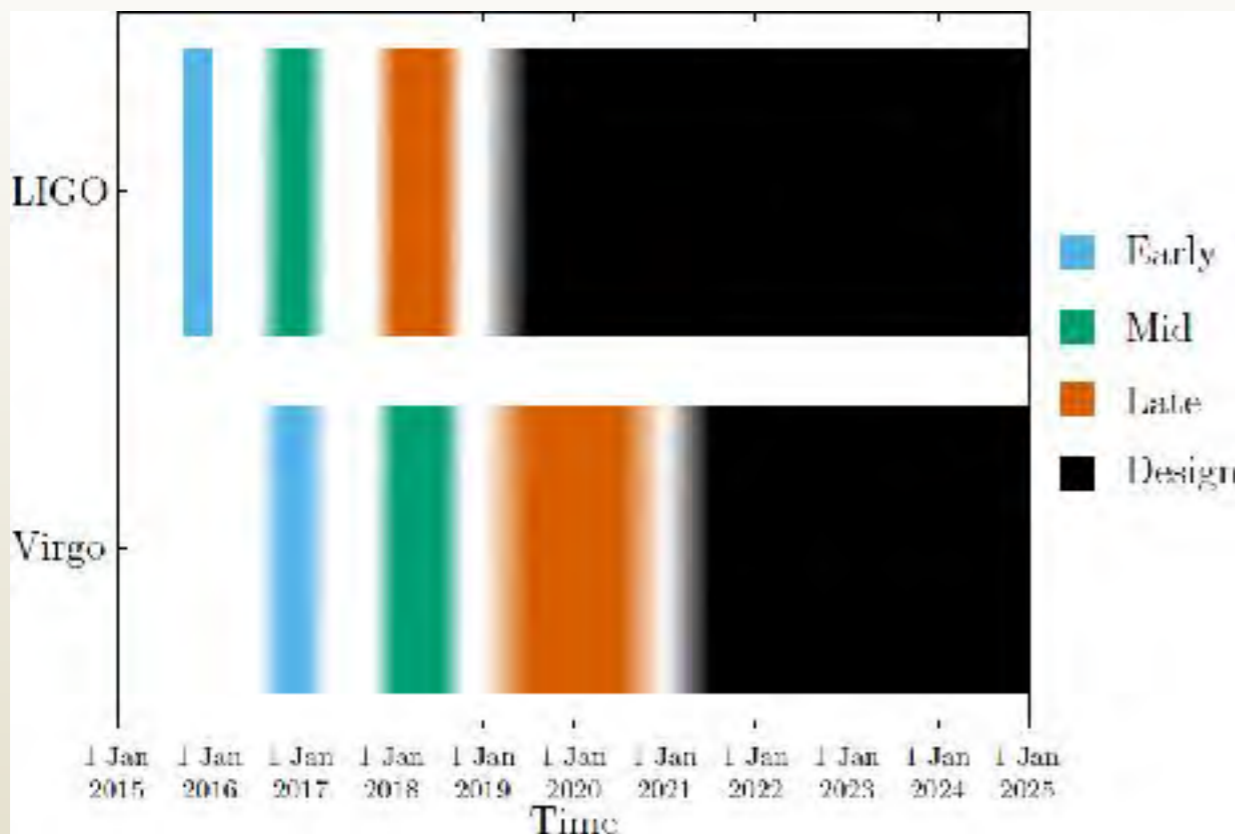
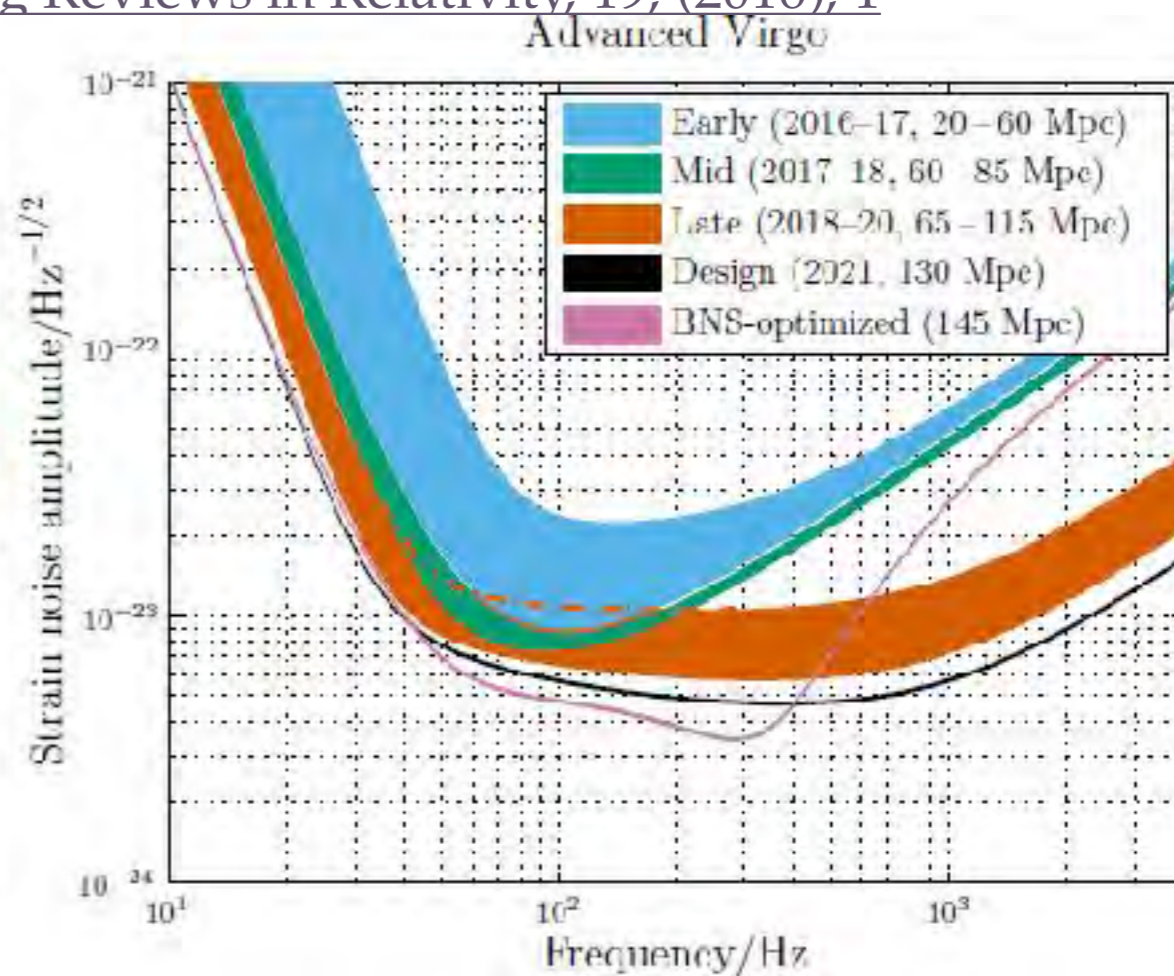
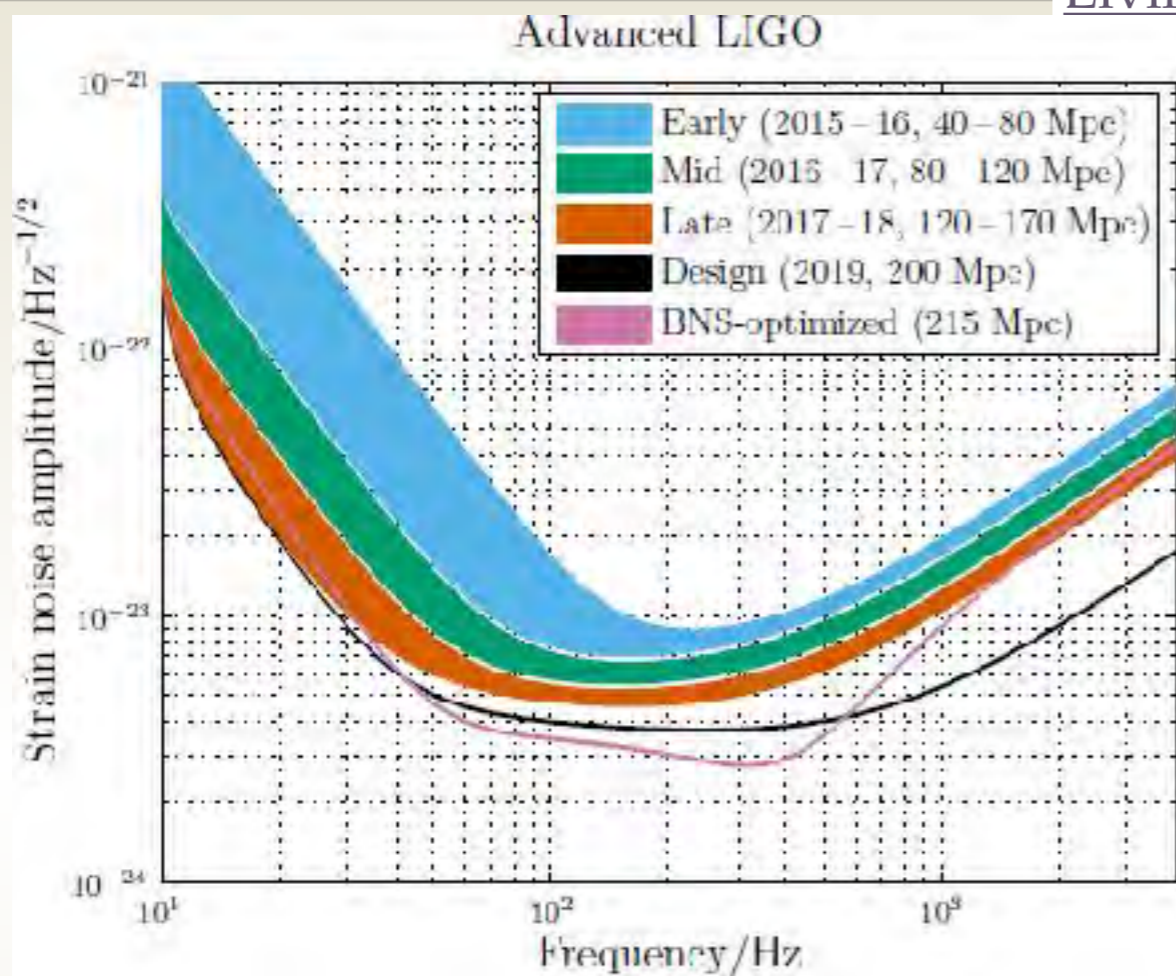
Control room, surface building at Kamioka



Spool data system
in next room

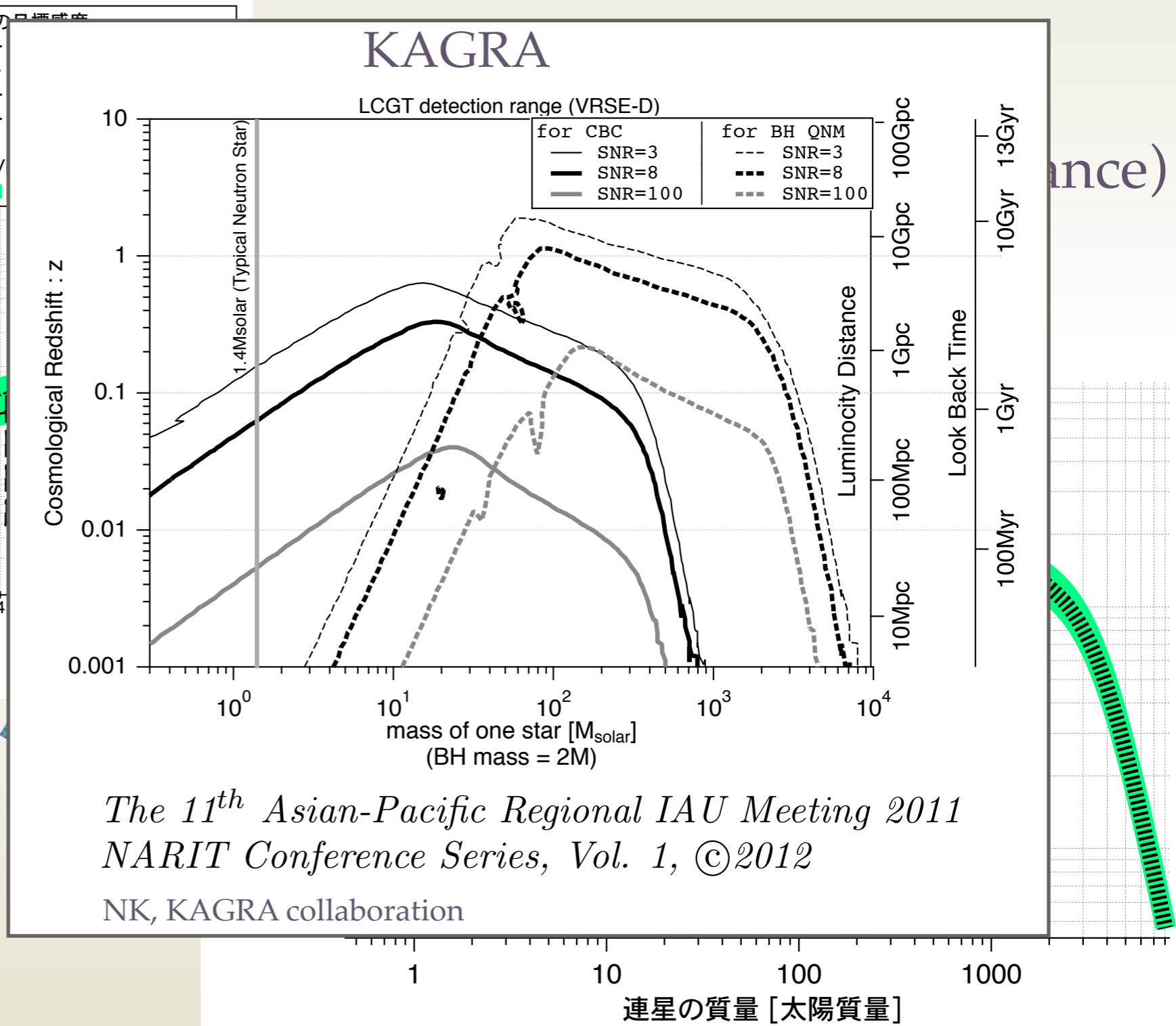
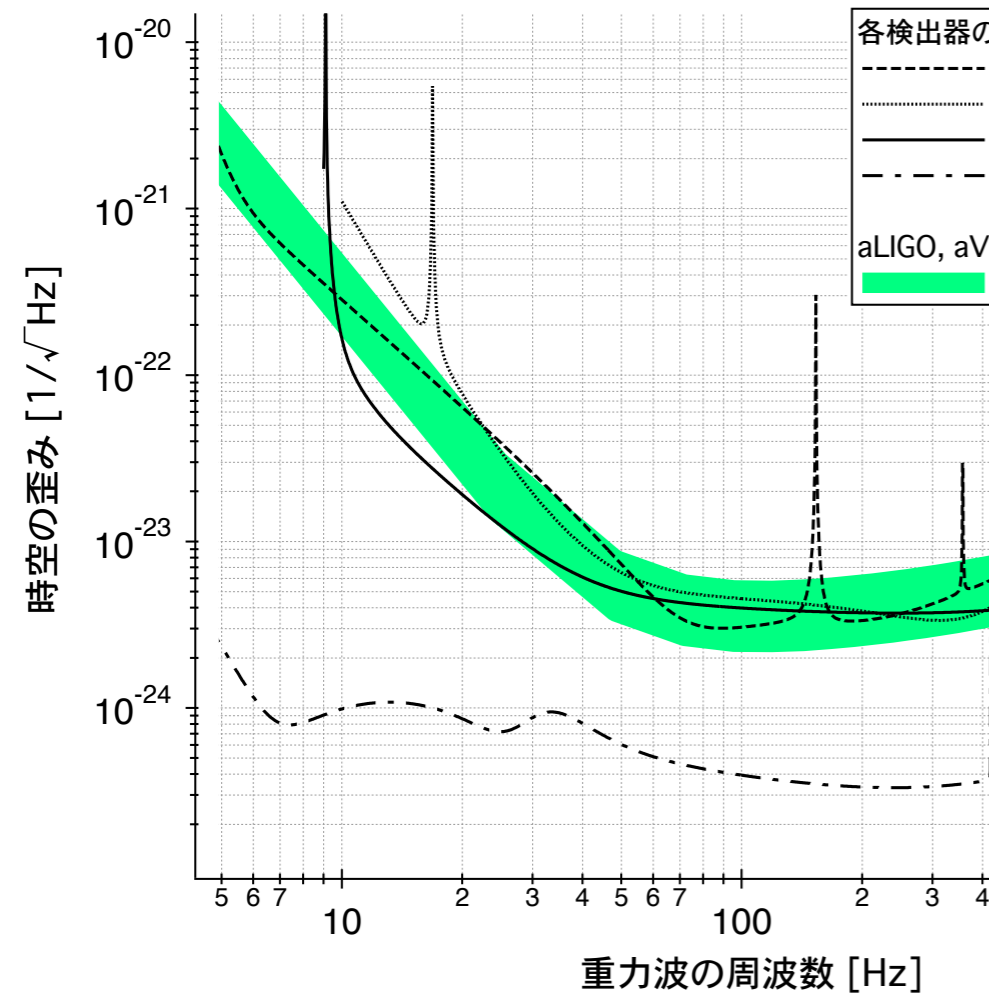
Observation Scenario

Prospects for Observing and Localizing Gravitational-Wave Transients with Advanced LIGO and Advanced Virgo
 Living Reviews in Relativity, 19, (2016), 1



(In next update of this documents. KAGRA will appear in these figures.)

Sensitivity → Range



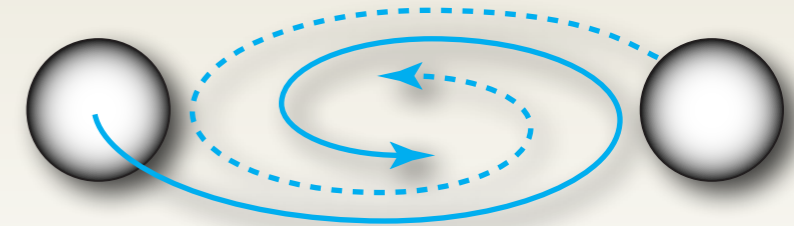
The 11th Asian-Pacific Regional IAU Meeting 2011
 NARIT Conference Series, Vol. 1, ©2012

NK, KAGRA collaboration

Remark : GW sources

Occasionally events :

- Compact binary coalescence (CBC):
NS-NS, NS-BH, BH-BH
Neutron star : NS, Blackhole : BH
- Supernovae
BH Quasi-normal mode oscillation
- Pulsar glitch



Continuous :

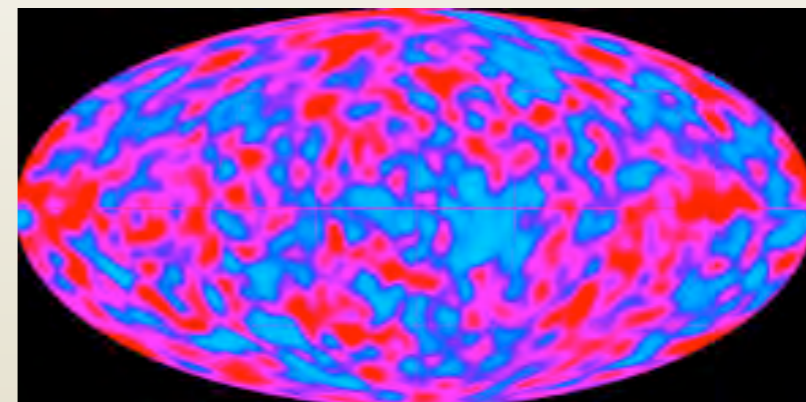
- Pulsar rotation
Binary



Stochastic Background

- Early Universe
Cosmic string
- Unresolvable astronomical origins

(& Unknown...)



Supernova (SN)

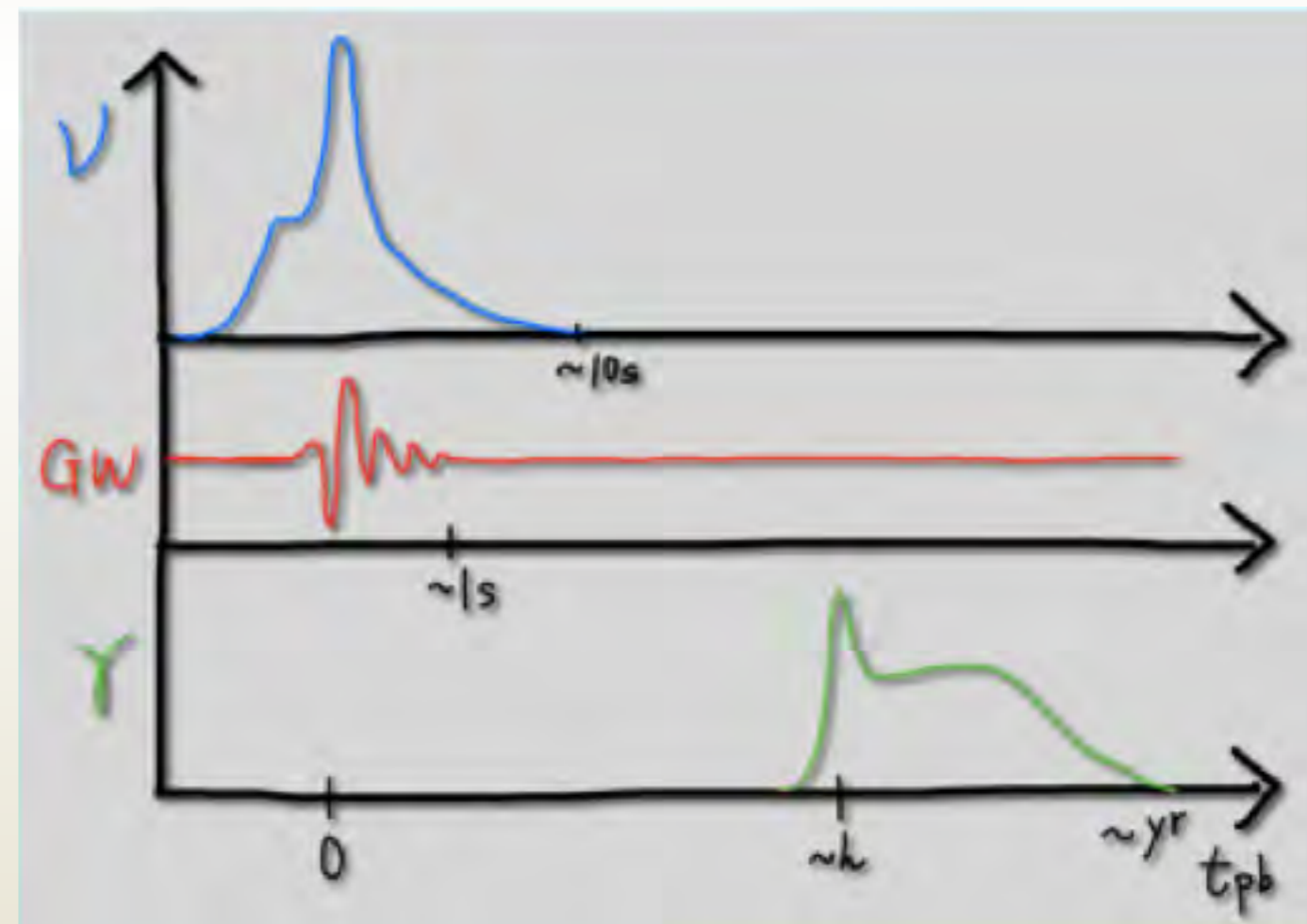


Many process of SN possibly radiate GWs

- core bounce
- convection
- SASI
- Jet

Neutrino, GW, EM will be emitted.

- Fruitful scenario of 'coincidence detection'
- Multi-probes make it possible to get newer knowledge and deep understand of SN mechanism.



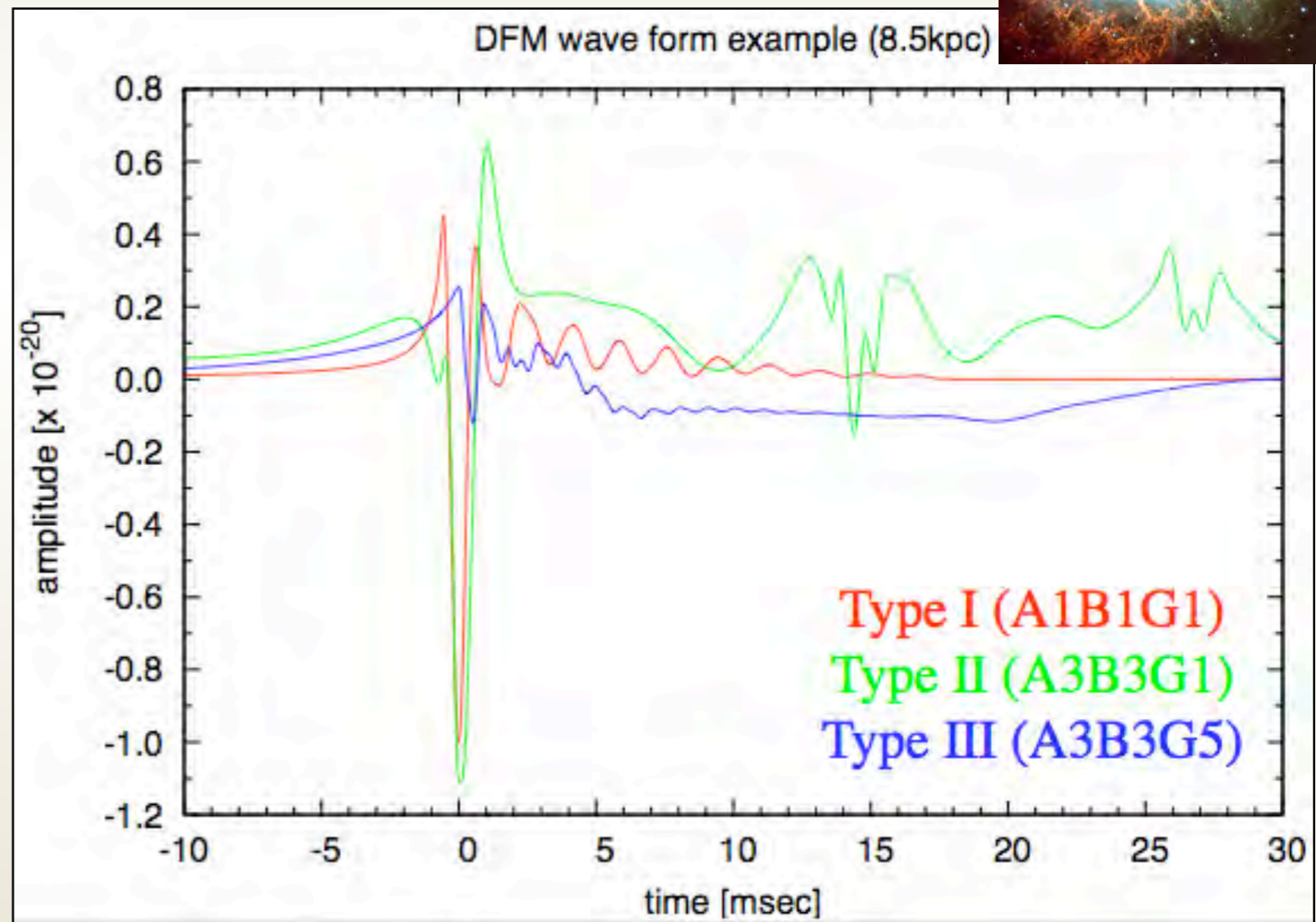
Drawn by Y.Suwa

GW signal (example : Supernova)

Supernova (type II) will emit short duration GW (Burst wave) according to various processes in it.

- Rotational Core collapse (Bounce)
- Convection
- Proto-neutron star formation and g-mode instability
- Standing-Accretion-Shock Instability

...



Dimmermeier at al.

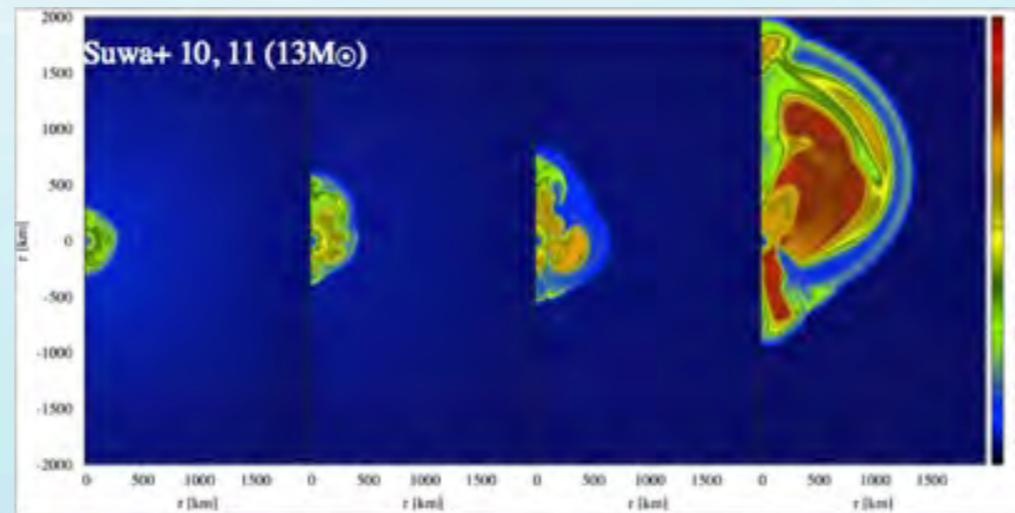
Team SKE

at Kakenhi New innovative area
「重力波天体」

SNe Theory(A05)

Y. Suwa

- Provide time correlated data, GW and neutrino
- Suggest signature signals physical phenomenon



Neutrino analysis(A03)

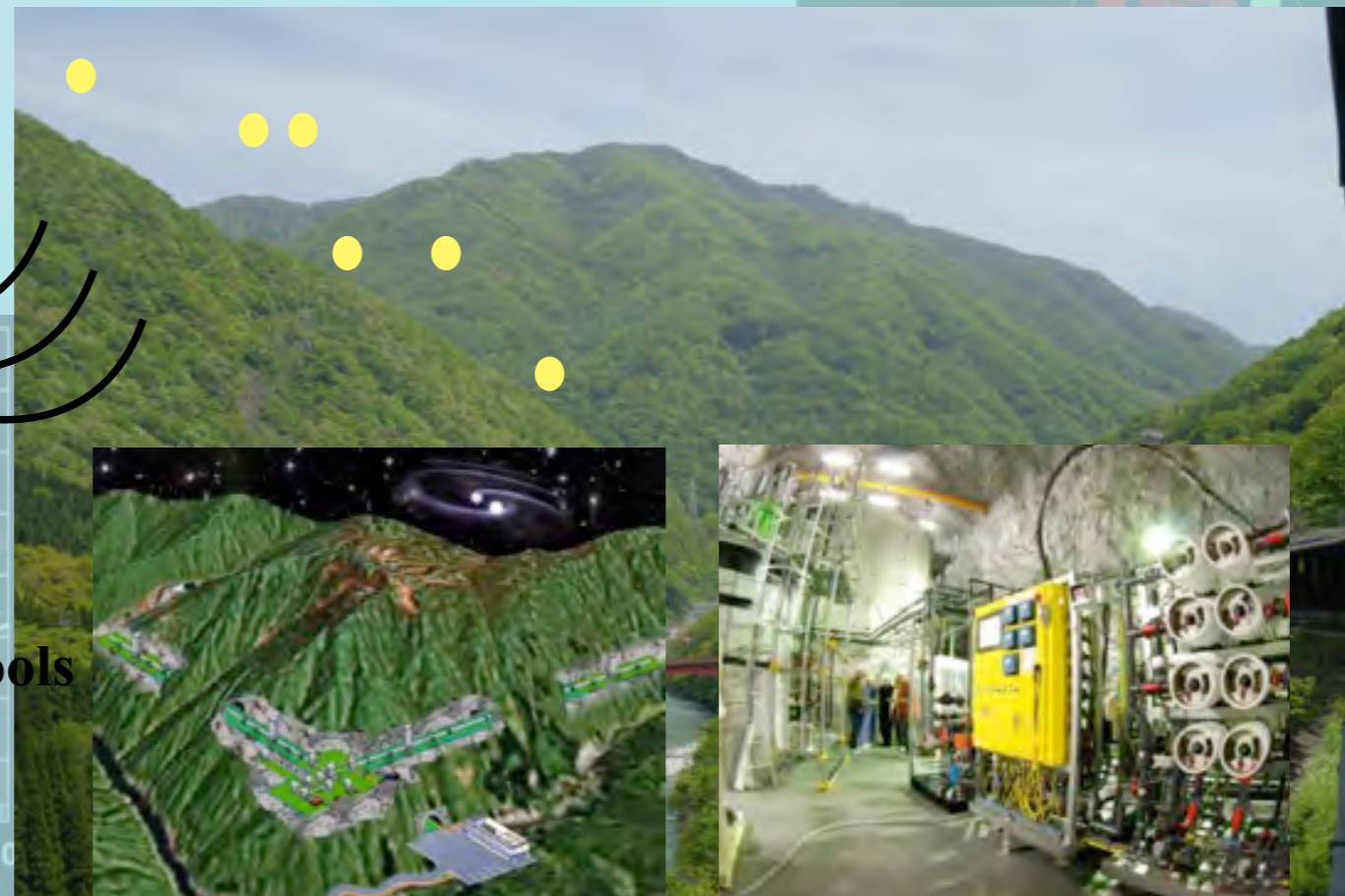
T. Kayano, Y. Koshio
M. Vagins

- R&D of EGADS detector
- Signal simulations with EGADS and SK

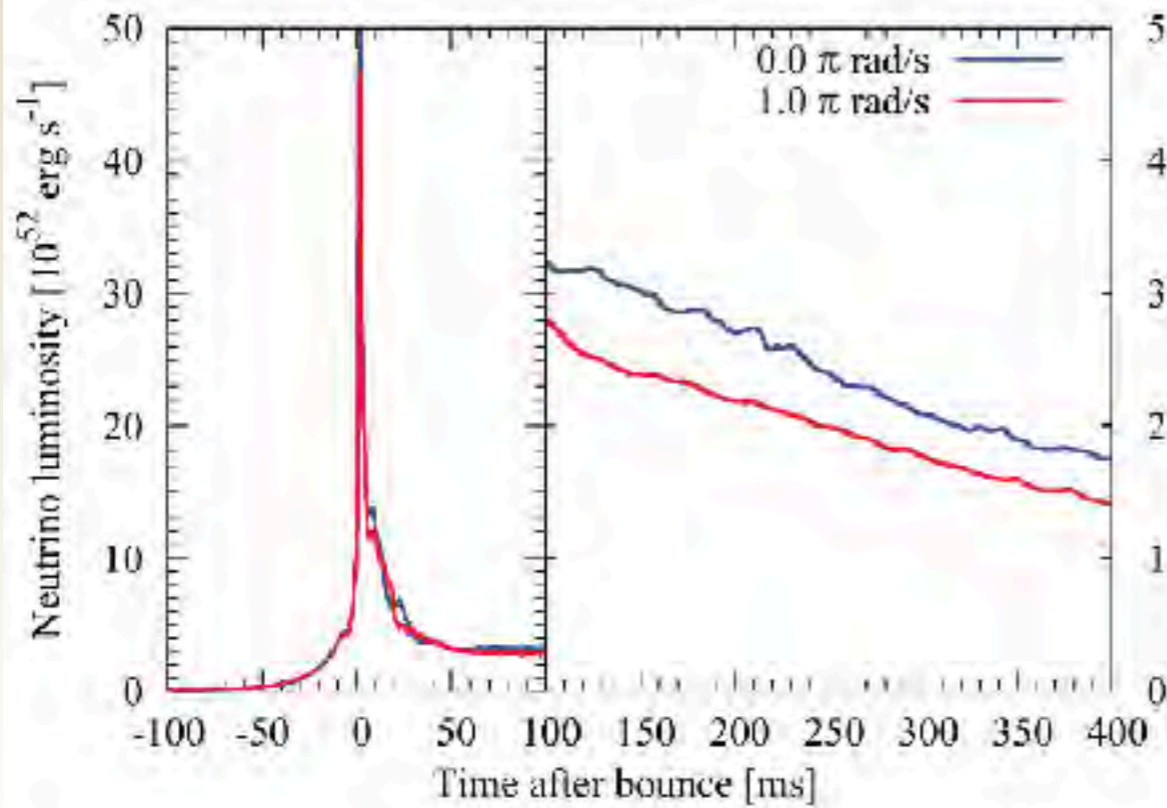
GW analysis(A04)

T. Yokozawa, M. Asano
N. Kanda

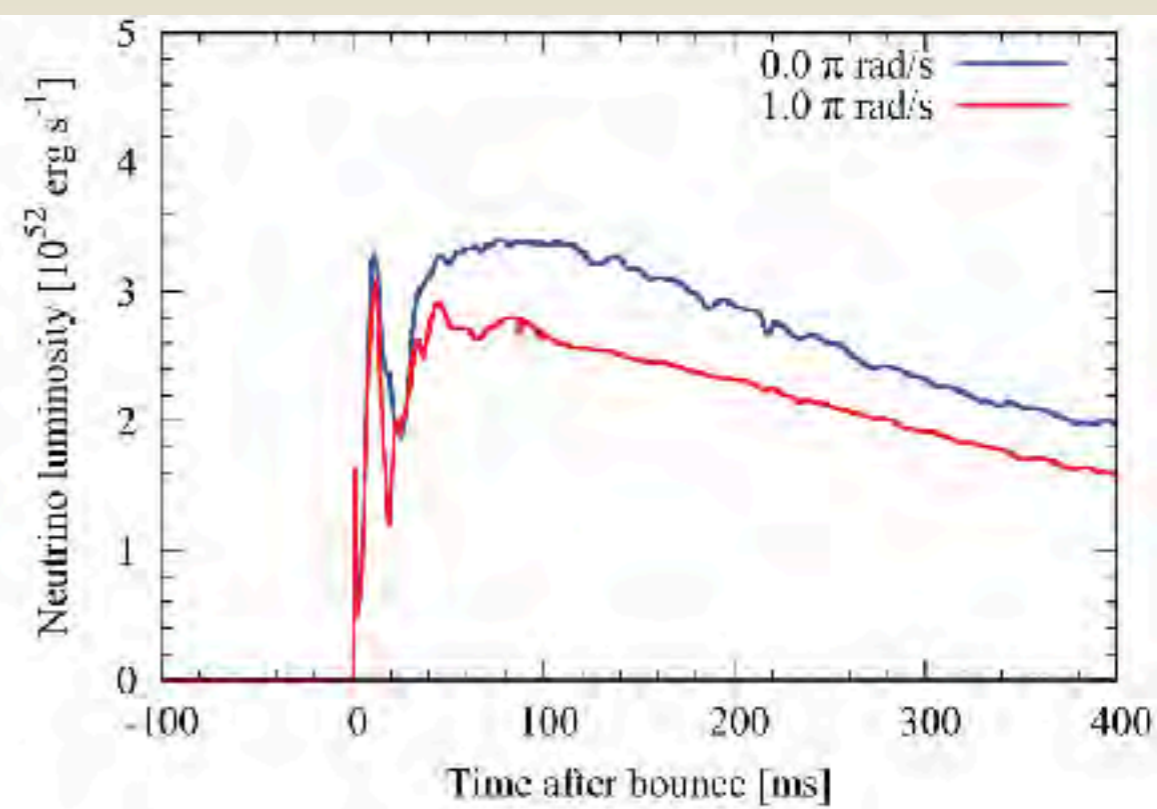
- KAGRA detector simulations
- Develop/Optimize GW analysis tools
- Prepare for realtime observation



neutrino



(a) L_{ν_e}



(b) L_{ν_e}

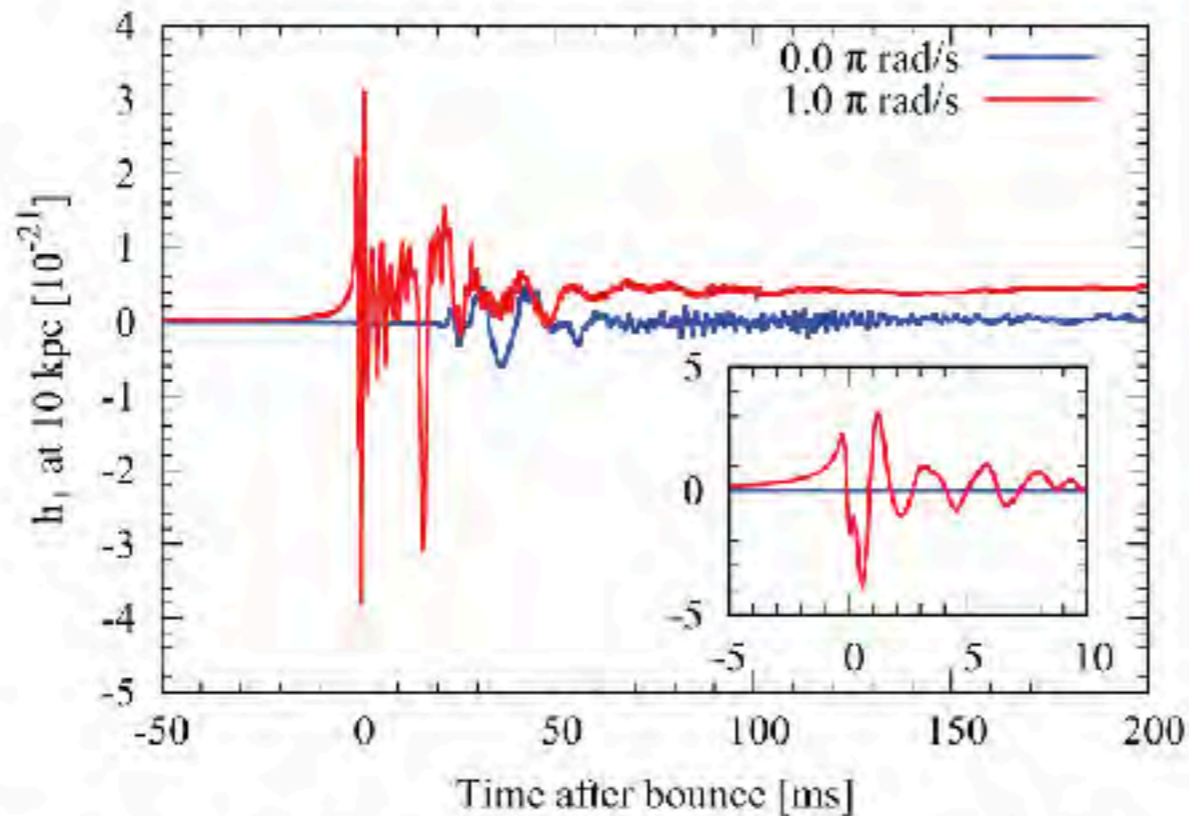


Figure 2. GW amplitude as a function of time for a core-collapse supernova occurring 10 kpc from the observer. Each line represents models with different initial rotation rates, i.e., no rotation ($\Omega_0 = 0.0\pi$) (blue) and strong rotation $\Omega_0 = 1.0\pi \text{ rad s}^{-1}$ (red). The small panel shows features around the bounce time. The fast rotation model exhibits a large amplitude GW at the

T.Yokozawa et al.,
ApJ., 811, 86 (12pp) 2015

GW

GW and neutrino analysis for the dynamics of SNe timing analysis could suggest that the core is strongly rotating or not.

Table 2

The Various Scenarios' GW Detection Efficiencies (GW eff.), Neutronization Neutrino Detection Efficiencies (Neutrino Eff.) for (1) EGADS or (2) GADZOOKS!, Their Product, and the P_r Value for the $0.0\pi \text{ rad s}^{-1}$ Model

Scenario	GW Eff.(%)	Neutrino Eff.(%)	Detection Eff.(%)	P_r (%)
0.2 kpc, uniform	74.8	100.0(1)	74.8	0.0
1.0 kpc, uniform	46.5	46.8(1)	21.9	20.8
Galactic Center	0.0	97.5(2)	0.0	...
Galaxy Dist.	1.5	84.6(2)	1.5	0.2

Table 3

The Various Scenarios' GW Detection Efficiencies(GW eff.), Neutronization Neutrino Detection Efficiencies (Neutrino Eff.) for (1) EGADS or (2) GADZOOKS!, Their Product, and the P_r Value for the $1.0\pi \text{ rad s}^{-1}$ Model

Scenario	GW Eff.(%)	Neutrino Eff.(%)	Detection Eff.(%)	P_r (%)
0.2 kpc, uniform	88.0	100.0(1)	88.0	98.4
1.0 kpc, uniform	73.6	40.2(1)	29.5	80.0
Galactic Center	21.5	94.8(2)	20.4	75.3
Galaxy Dist.	26.7	81.7(2)	24.7	76.2

Observational Strategy for GW and Neutrino

Problems/Concerns:

- Event must be near !
Typical range of GW and Neutrino detector for SN is a few-several 100Mpc.
- Our galaxy might be optical thick.

Therefore, ...

- Keep duty time!
GW detectors may be key.
Never lose the chance of golden event !
- Inference of the direction by each detection is essential.
- We must develop the data analysis that can be done with a single event.

Advantages

- omni-directional
- 'time machine' like
In both detector cases, we can analyze past records of event triggers / signals.
- (In Japan) SK and KAGRA has less uncertainty of arrival time difference.

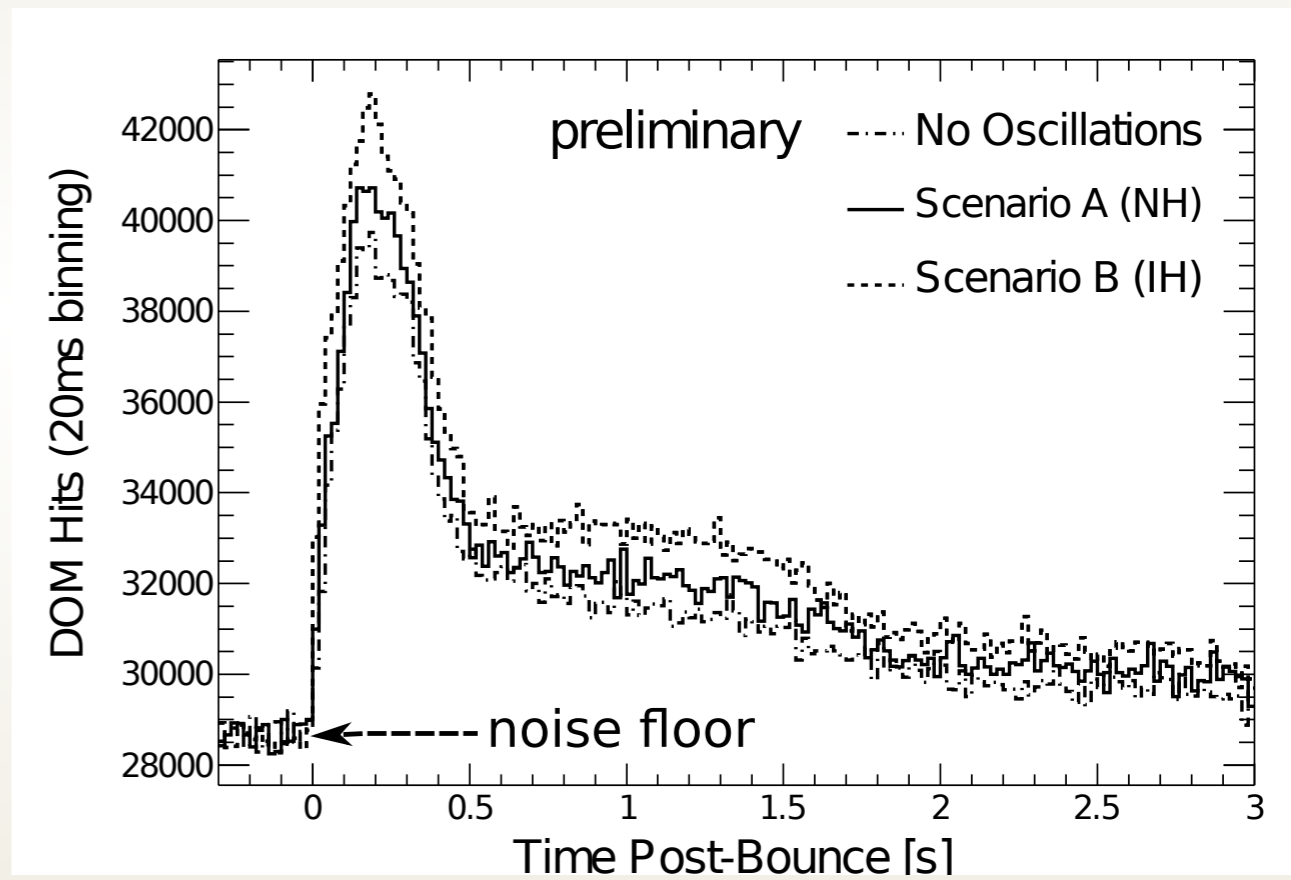
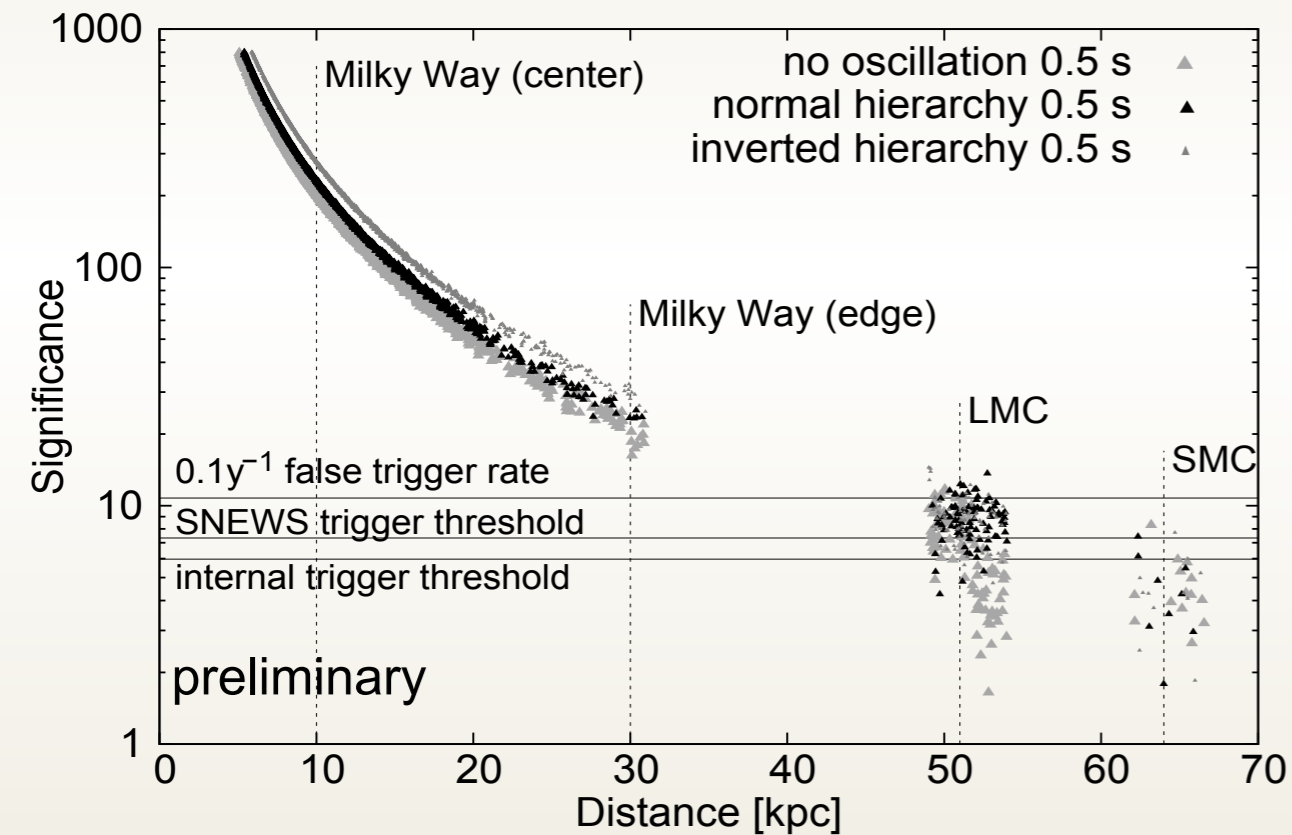
Key issues

- time series (time profile) of both GW and neutrino flux
- infer the SN direction

一期一会

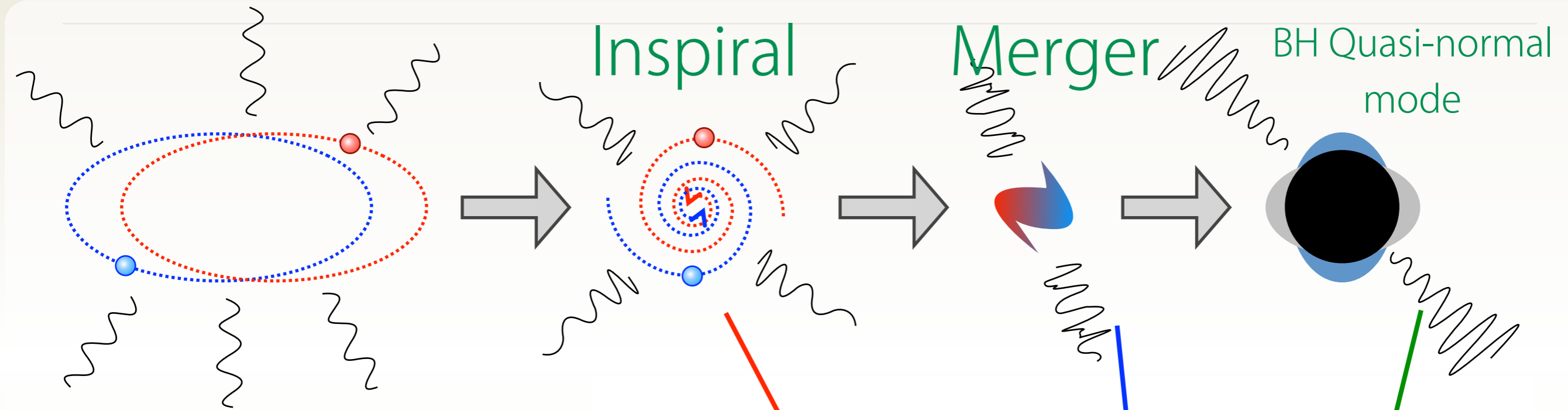
Personal question : How about IceCube for SN?

SN @10kpc away



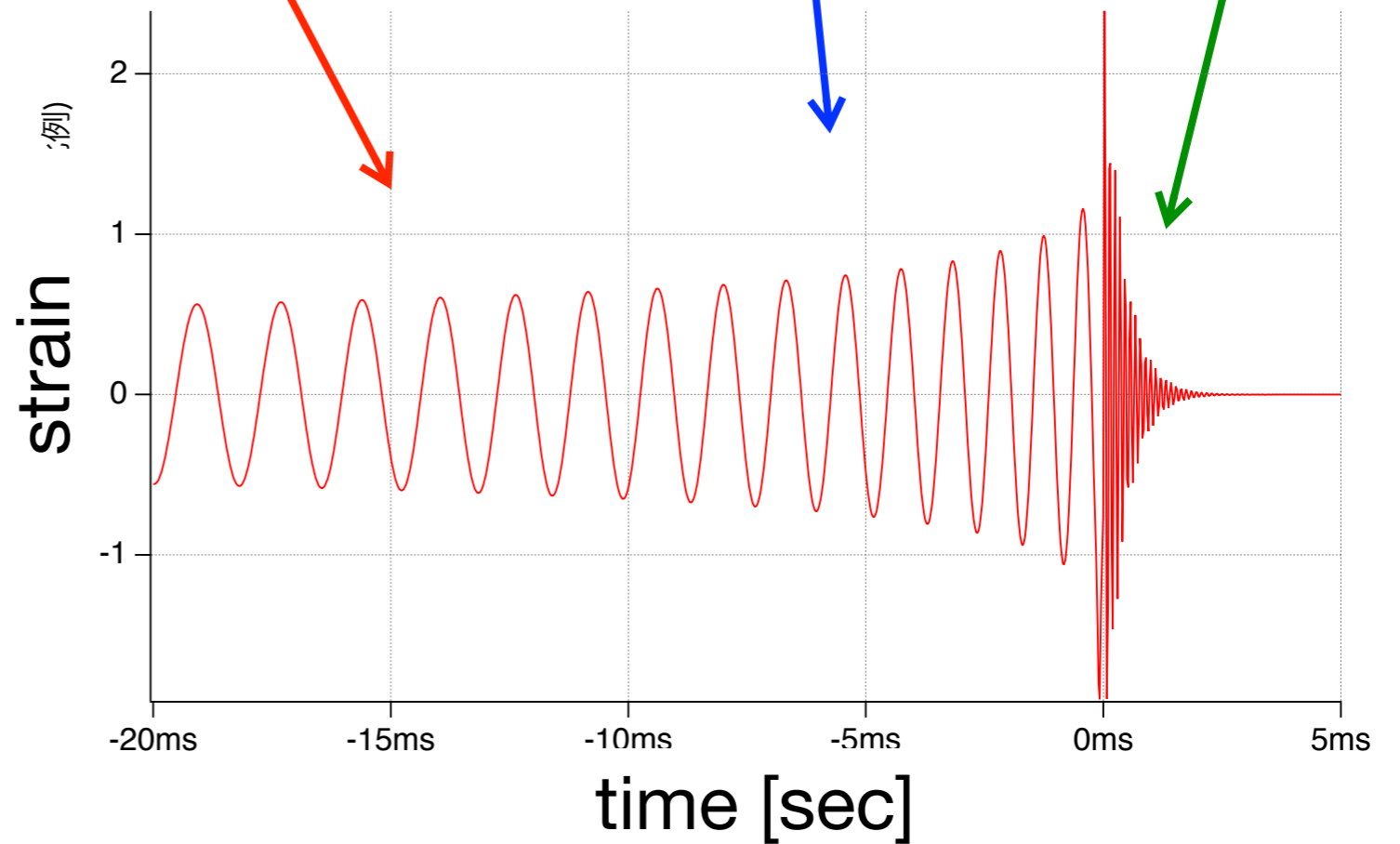
arXiv:1111.2731 (Proceedings of ICRC2011)

CBC (Compact Binary Coalescence)



Compact Stars :

- Black-holes
- Neutron Stars



CBC Waveform and Physics

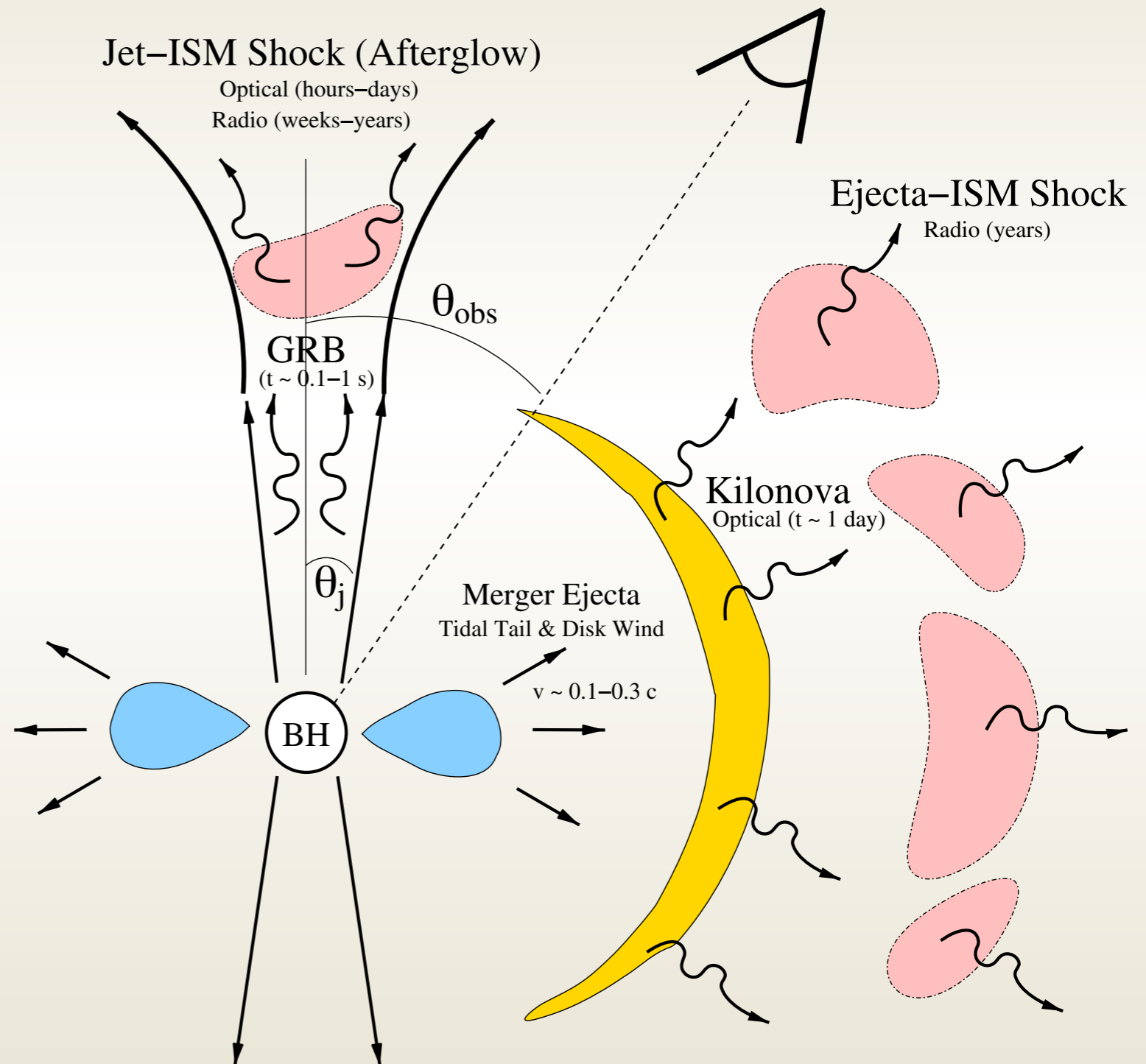


phase	Inspiral (a few ~1000sec, depend on mass)	merger (~10msec)	ringdown (~100msec)	
waveform	Post-Newton approx. analytic waveform	Numerical relativity	Perturbation theory of BH space-time	
frequency	(10Hz) ~ 1.5 kHz	a few kHz	several kHz	
Physics	mass of stars, luminosity, arrival time (with multi-detectors, direction, polarization, phase, orbit inclination, distance)	Tidal effects, Viscosity, ... -> NS's E.O.S.	(In case of Hyper-massive NS is formed, EOS, hyperon, ...)	BH mass BH spin Testing GR

After merger of NS-NS, NS-BH

EM follow-ups

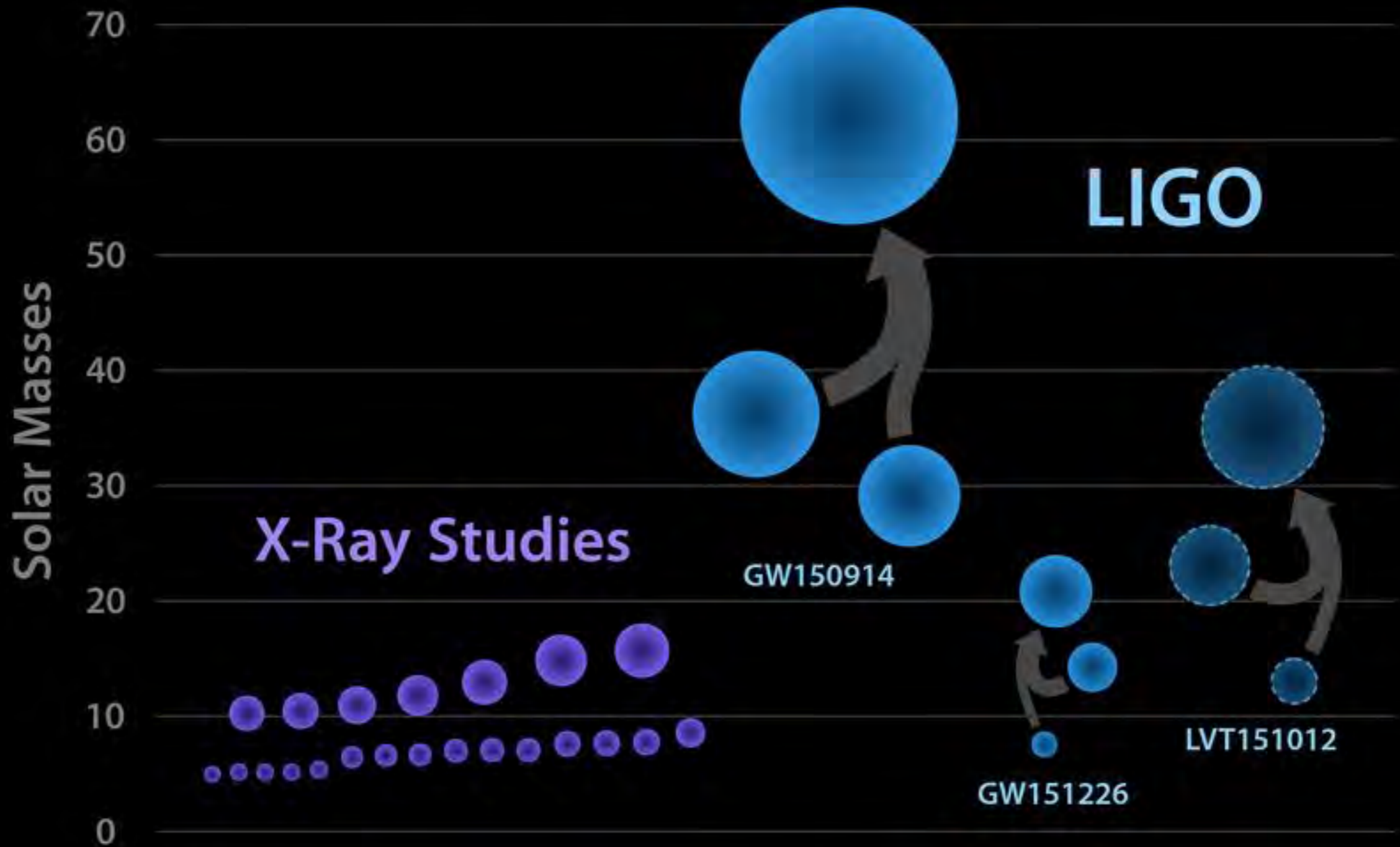
In cases of NS-NS and NS-BH, Electro-magnetic radiation can be expected.



Metzger & Berger, ApJ 746:48(2012)

BH-BH

Black Holes of Known Mass



Origin of Massive Black-holes ?

Stars as like our sun cannot form such heavy BH...

- Population III stars ?

Metal less stars that may be the 'first stars' of the universe

- Dynamical formation ?

runaway merger of BHs

- Primordial BH?

BH formed directly at early universe



30 + 30 solar mass BHs

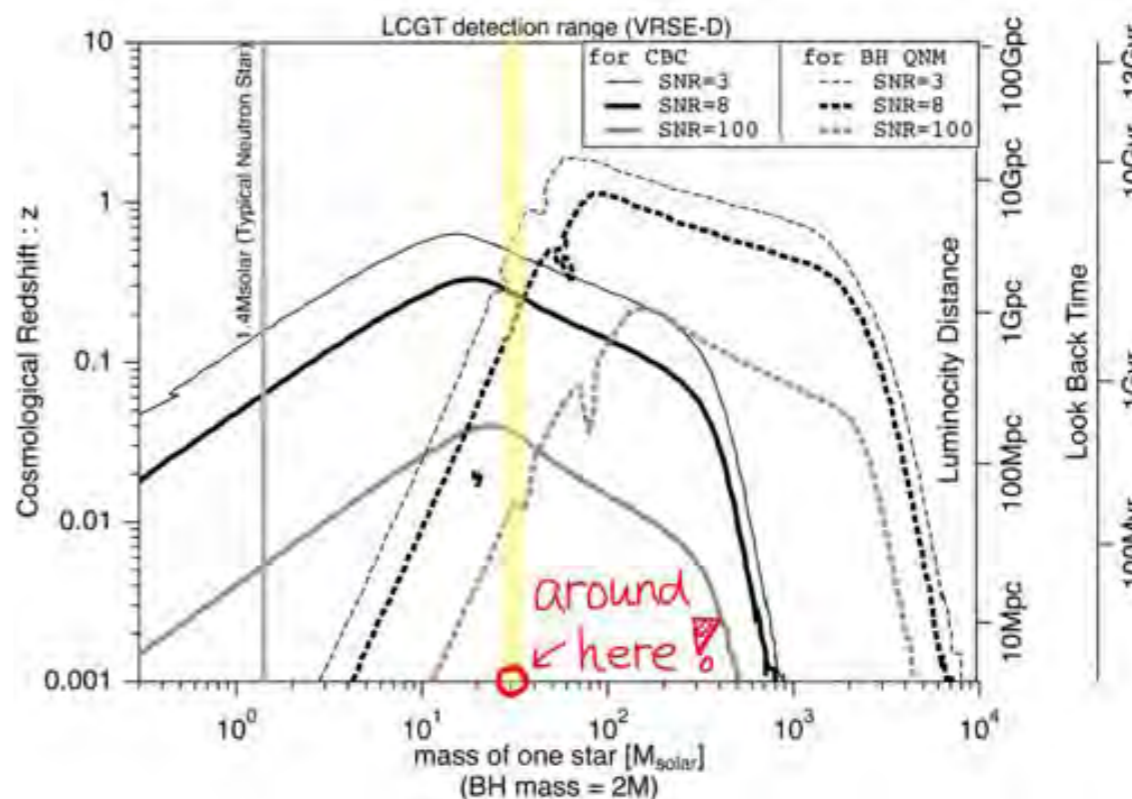
Interesting target for three reasons:

Nakano Talk

Inspiral and ringdown phases have roughly equal SNRs, so provides good test of GR

If population III stars (formed at redshifts 5-10) exist, these might be a substantial fraction.

Perhaps we will detect several of them in the first aLIGO data run O1, this September!



The detection rate of inspiral and quasi-normal modes of Population III binary black holes which can confirm or refute the general relativity in the strong gravity region

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²*Department of Physics, Graduate School of Science, Osaka City University, Osaka 558-8585, Japan*

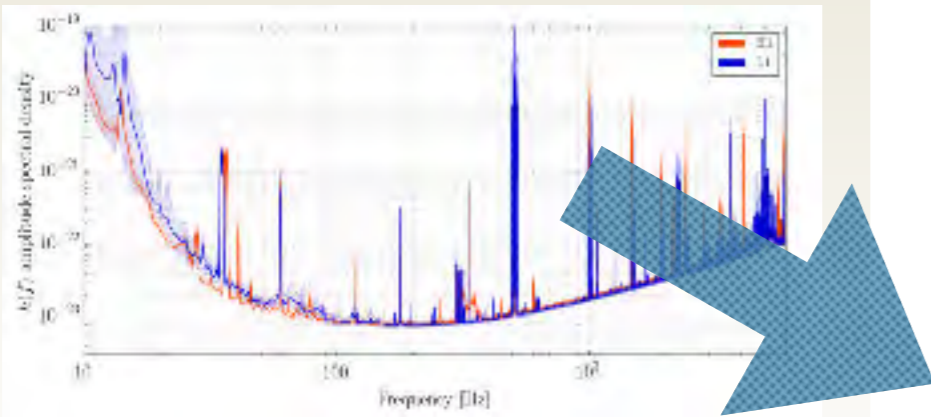
Accepted 2015 November 5. Received 2015 October 17; in original form 2015 May 26

ABSTRACT

Using our population synthesis code, we found that the typical chirp mass defined by $(m_1 m_2)^{3/5} / (m_1 + m_2)^{1/5}$ of Population III (Pop III) binary black holes (BH–BHs) is $\sim 30 M_\odot$ with the total mass of $\sim 60 M_\odot$ so that the inspiral chirp signal as well as quasi-normal mode (QNM) of the merging black hole (BH) are interesting targets of KAGRA. The detection rate of the coalescing Pop III BH–BHs is $\sim 180 \text{ events yr}^{-1} (SFR_p / (10^{-2.5} M_\odot \text{ yr}^{-1} \text{ Mpc}^{-3})) ([f_b / (1 + f_b)] / 0.33) Err_{\text{sys}}$ in our standard model, where SFR_p , f_b and Err_{sys} are the peak value of the Pop III star formation rate, the binary fraction and the systematic error with $Err_{\text{sys}} = 1$ for our standard model, respectively. To evaluate the robustness of chirp mass distribution and the range of Err_{sys} , we examine the dependence of the results on the unknown parameters and the distribution functions in the population synthesis code. We found that the chirp mass has a peak at $\sim 30 M_\odot$ in most of parameters and distribution functions as well as Err_{sys} ranges from 0.046 to 4. Therefore, the detection rate of the coalescing Pop III BH–BHs ranges about $8.3\text{--}720 \text{ events yr}^{-1} (SFR_p / (10^{-2.5} M_\odot \text{ yr}^{-1} \text{ Mpc}^{-3})) ([f_b / (1 + f_b)] / 0.33)$. The minimum rate corresponds to the worst model which we think unlikely so that unless $(SFR_p / (10^{-2.5} M_\odot \text{ yr}^{-1} \text{ Mpc}^{-3})) ([f_b / (1 + f_b)] / 0.33) \ll 0.1$, we expect the Pop III BH–BHs merger rate of at least one event per year by KAGRA. Nakano, Tanaka & Nakamura show that if signal-to-noise ratio (S/N) of QNM is larger than 35, we can confirm or refute the general relativity (GR) more than 5σ level. In our standard model, the detection rate of Pop III BH–BHs whose S/N is larger than 35 is $3.2 \text{ events yr}^{-1} (SFR_p / (10^{-2.5} M_\odot \text{ yr}^{-1} \text{ Mpc}^{-3})) ([f_b / (1 + f_b)] / 0.33)$.

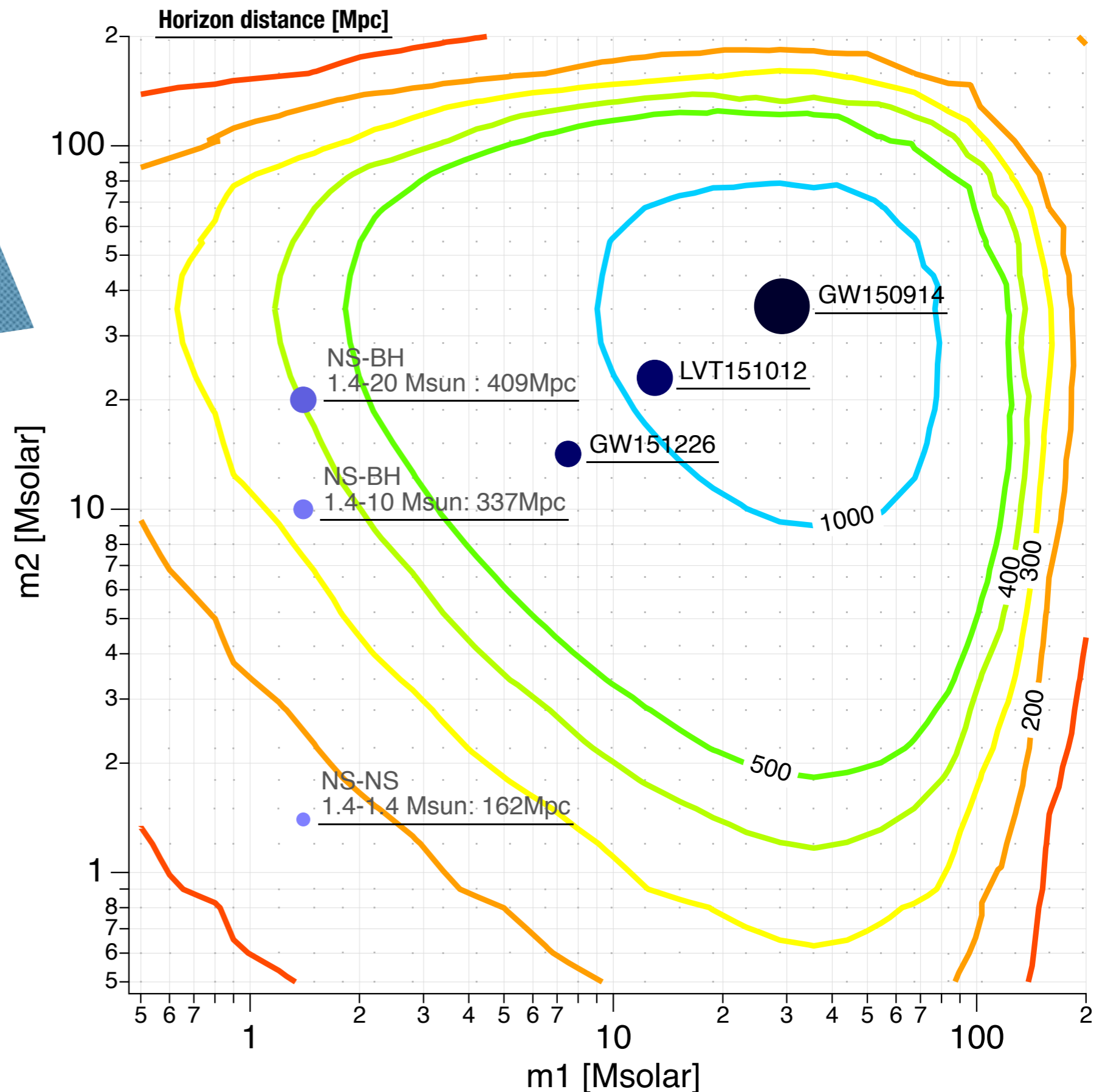
Window as a function of binary masses

Example : LIGO O1



Detector opens window for particular mass ranges.

(In another word, this might be a 'bias'...)



Summary

Welcome to the observational era!

We need more more more events !!!

Multi-messenger observation

for deep understanding of GW sources.

i.e. dynamical motion and mechanism, origin, etc.

GW observation itself still attractive for the study of fundamental physics.