

# The Spin Evolution of Binary Black Holes Progenitors in open cluster

arXiv:2102.09323

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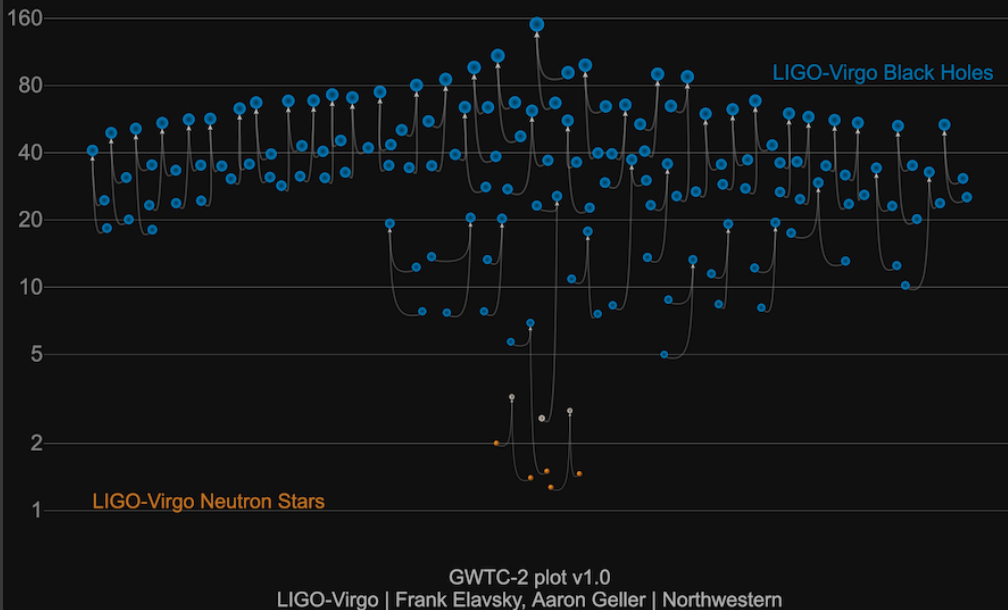
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Challenging and Innovation in Computational Astrophysics 2021

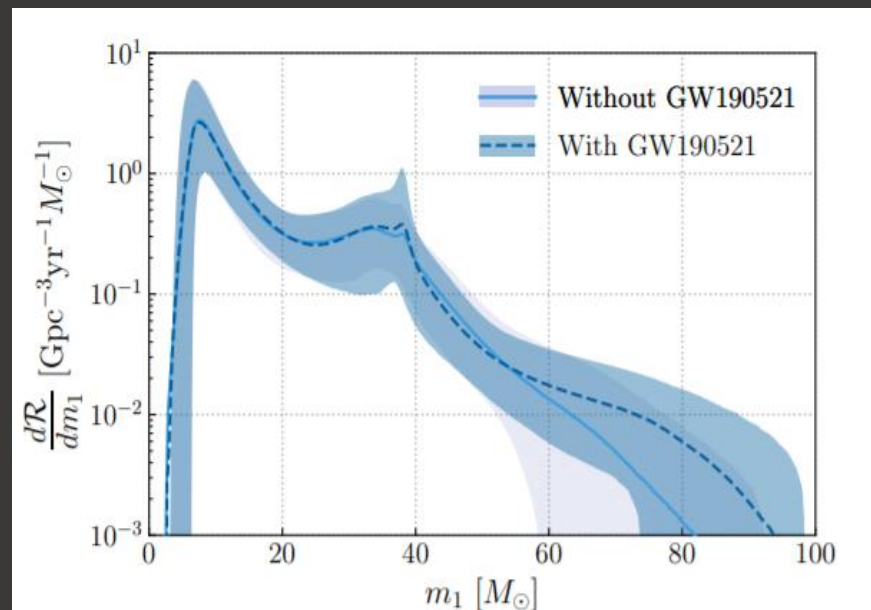
@Zoom meeting

# INTRODUCTION

## Masses in the Stellar Graveyard *in Solar Masses*



differential merger rate density for  $m_1$



LIGO/Virgo O1-O3a  
(arXiv 2010.14533)

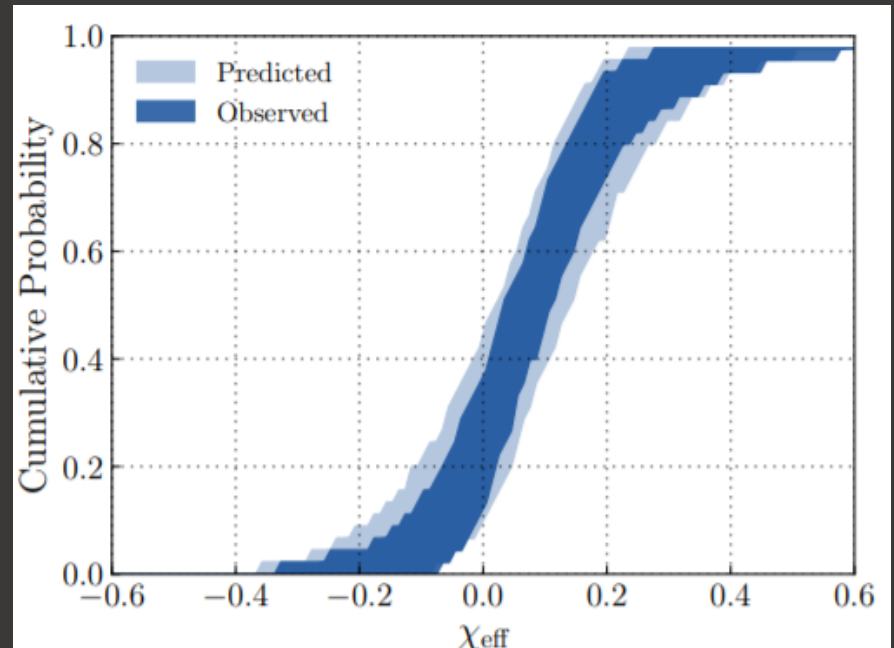
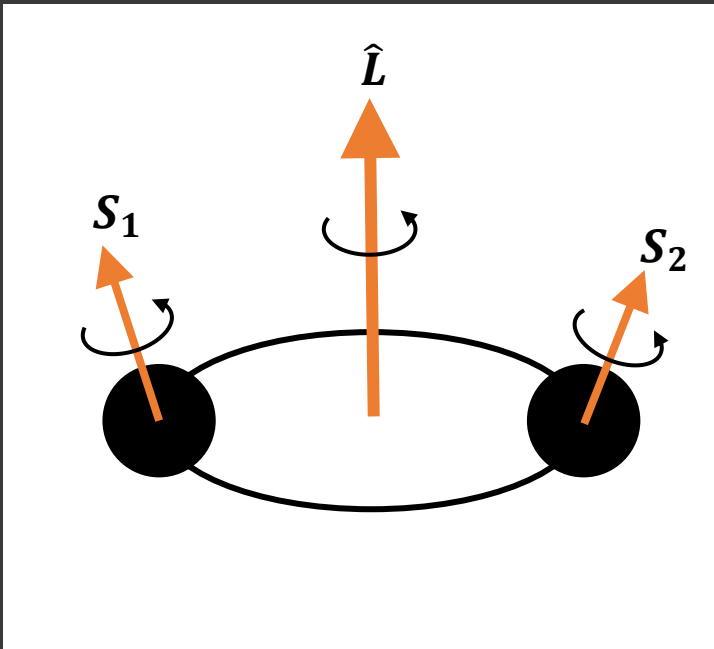
Formation scenarios for these binary black holes

1. isolated field binary (common envelope, mass transfer)
2. dynamical formation in the dens star region

# Spin parameter : $\chi_{\text{eff}}$

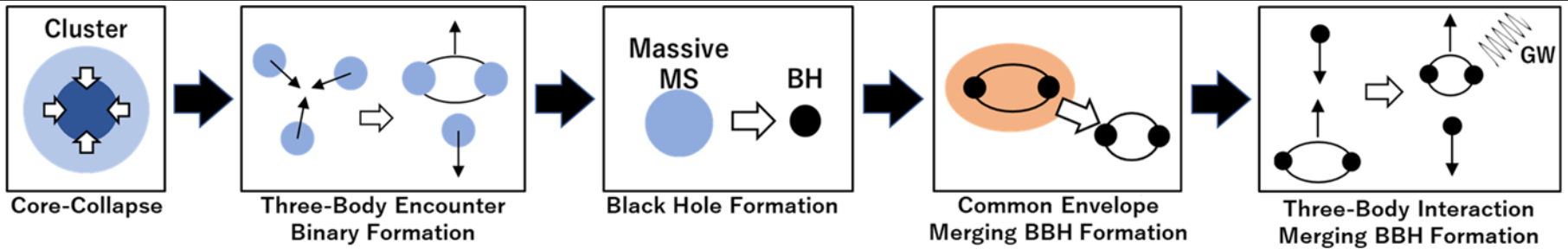
$$\chi_{1,2} = \frac{c}{Gm_{1,2}^2} S_{1,2} \cdot \hat{L}, \quad \chi_{\text{eff}} = \frac{m_1 \chi_1 + m_2 \chi_2}{M},$$

O1-O3a (arXiv 2010.14533)



# previous our results

## 1) BBH formation in open cluster (Kumamoto+2019)

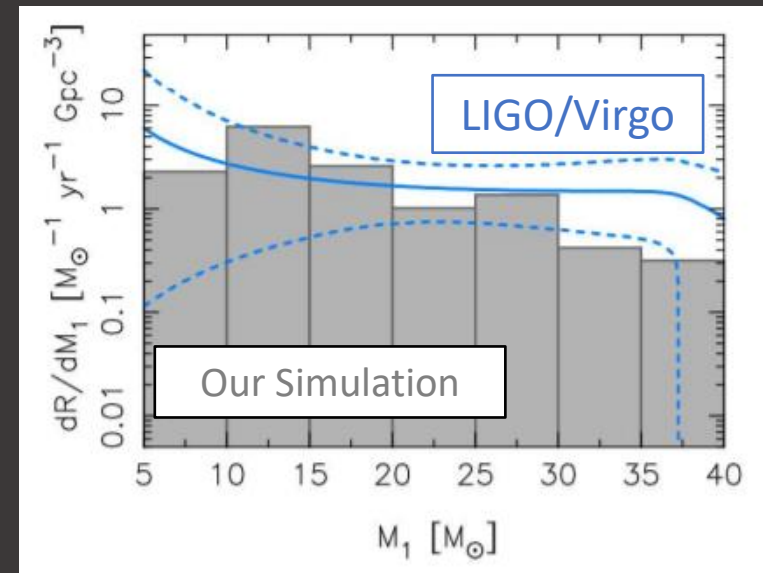


## 2) merger rate density of BBHs formation in open cluster (Kumamoto+2020)

$$R_{OC} \sim 70 \text{ yr}^{-1} \text{Gpc}^{-3}$$

c.f. BBH merger rate density estimated from 10 BBHs observed O1 and O2;

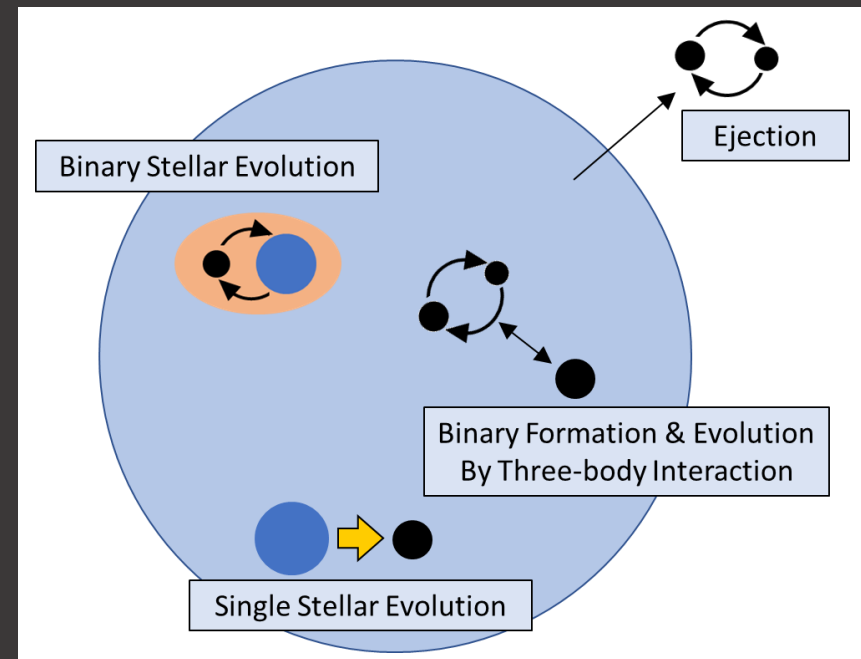
$$R = 53.2_{-28.8}^{+58.5} \text{ yr}^{-1} \text{Gpc}^{-3} \quad (\text{Abbott} + 2019)$$



# N-body simulation – Methods and Models

We performed N-body simulations of open clusters with four different metallicities to estimate a local merger rate density of BBHs from **open clusters**.

- code : NBODY6++GPU
- Cluster Mass :  $\sim 2500M_{\odot}$
- Number of Particles : 4266
- Initial Mass Function : Kroupa 2001  
 $0.08M_{\odot} < M_{star} < 150M_{\odot}$
- Density Profile : Plummer Model
- Half Mass Density :  
 $\rho_{hm,ini} = 10^4 M_{\odot}pc^{-3}$
- No primordial binary
- No natal kick
- Metallicity :  $Z/Z_{\odot} = 0.1, 0.25, 0.5, 1$
- Stellar Evolution (Hurley+2000)
  - Evolution of stellar mass, radius and luminosity
  - Common envelope
  - Mass transfer



Kumamoto et.al. 2019  
Kumamoto et.al. 2020

# RESULTS – ejected BBHs from cluster

Number of binaries black holes formed in cluster

| Model | metallicity Z | $N_{\text{cluster}}$ | $N_{\text{BBH}}$ | $N_{\text{BBH}}(t_{\text{GW}} < 14\text{Gyr})$ |
|-------|---------------|----------------------|------------------|--|
| Z0002 | 0.002         | 360                  | 338              | 37   |
| Z0005 | 0.005         | 500                  | 487              | 17   |
| Z001  | 0.01          | 1000                 | 988              | 32   |
| Z002  | 0.02          | 1000                 | 877              | 7  |

We calculate the merger time of binary black holes escaped from the cluster.

$$\text{merger time : } t_{\text{GW}} \sim 1.2 \left[ \frac{M_1}{30M_{\odot}} \right]^{-3} \left[ \frac{a}{0.1\text{AU}} \right]^4 \frac{g(e)}{q(1+q)} \text{Gyr},$$

$$g(e) \equiv \frac{(1 - e^2)^{3.5}}{1 + \frac{73}{24}e^2 + \frac{37}{96}e^4}$$

# Spin-up by tidal locking

Time scale of synchronization by tidal locking:

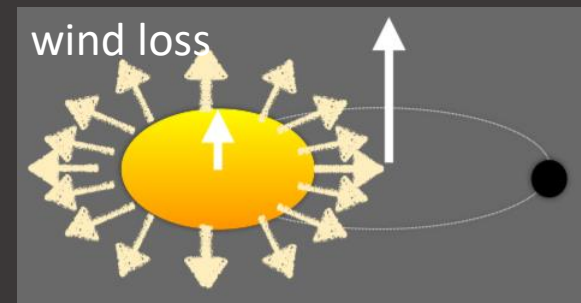
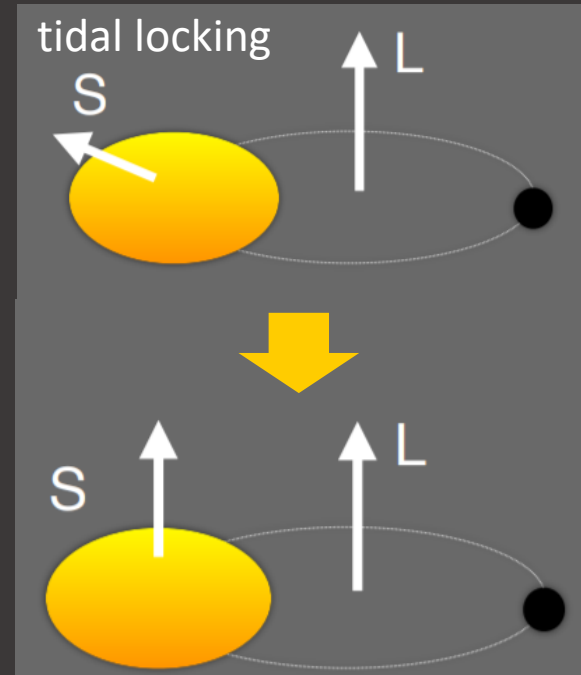
$$t_{syn} \approx 10 \text{ Myr } q^{-1/8} \left( \frac{1+q}{2q} \right)^{31/24} \left( \frac{t_c}{1\text{Gyr}} \right)^{17/8}$$

Fully synchronized spin parameter:

$$\chi_{syn} \approx 0.5 q^{1/4} \left( \frac{1+q}{2} \right)^{1/8} \left( \frac{\epsilon}{0.075} \right) \left( \frac{R_2}{2R_\odot} \right)^2 \left( \frac{m_2}{30M_\odot} \right)^{-13/8} \left( \frac{t_c}{1\text{Gyr}} \right)^{-3/8},$$

Time scale of spin-loss by wind mass loss:

$$t_w = \frac{\chi_*(t)}{\dot{\chi}_*(t)} = \frac{M(t)}{\dot{M}(t)} \propto Z^{-0.86}$$



# Spin Evolution

Time evolution of stellar spin parameter  
(Piran & Piran 2020):

$$\frac{d\chi_*}{dt} = \frac{(\chi_{syn} - \chi_*)^{8/3}}{t_{syn}(t_c)} - \frac{\chi_*}{t_w},$$


  
 tidal locking      wind

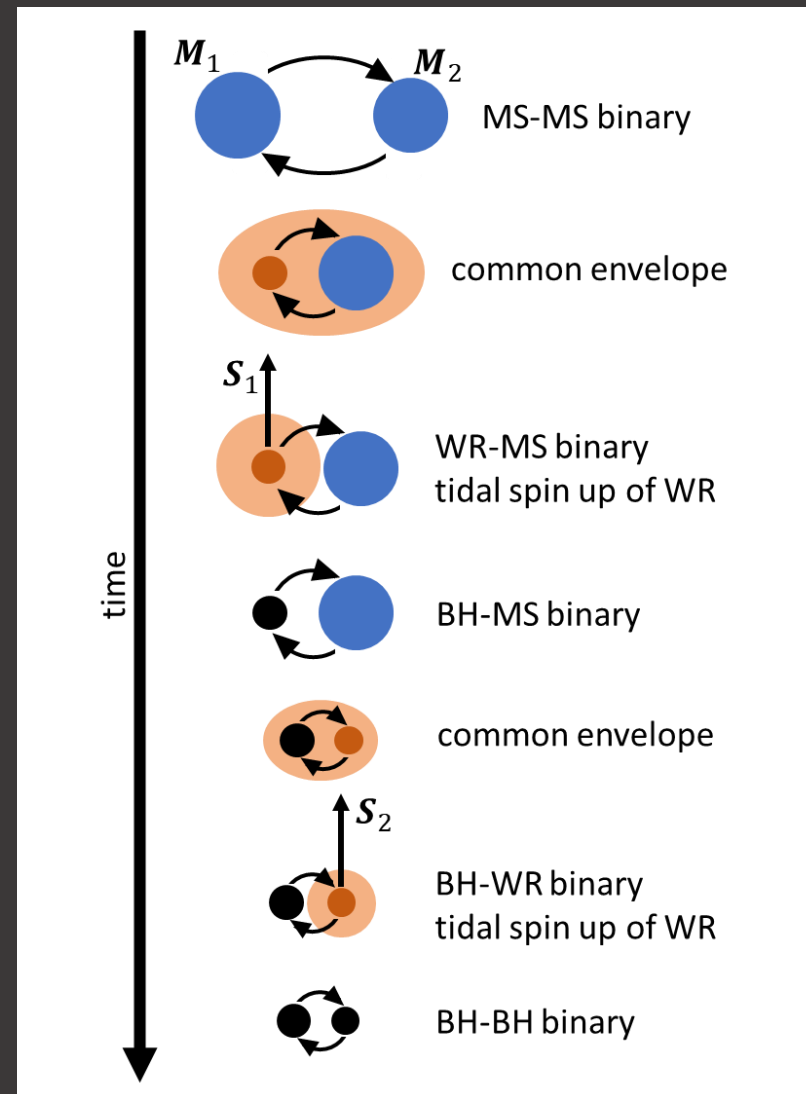
We assumed the initial spin distribution just after the common envelope  $S_{1,2}(0)$ .

Modal 1:

$$S_{1,2}(0) = 0$$

Model 2:

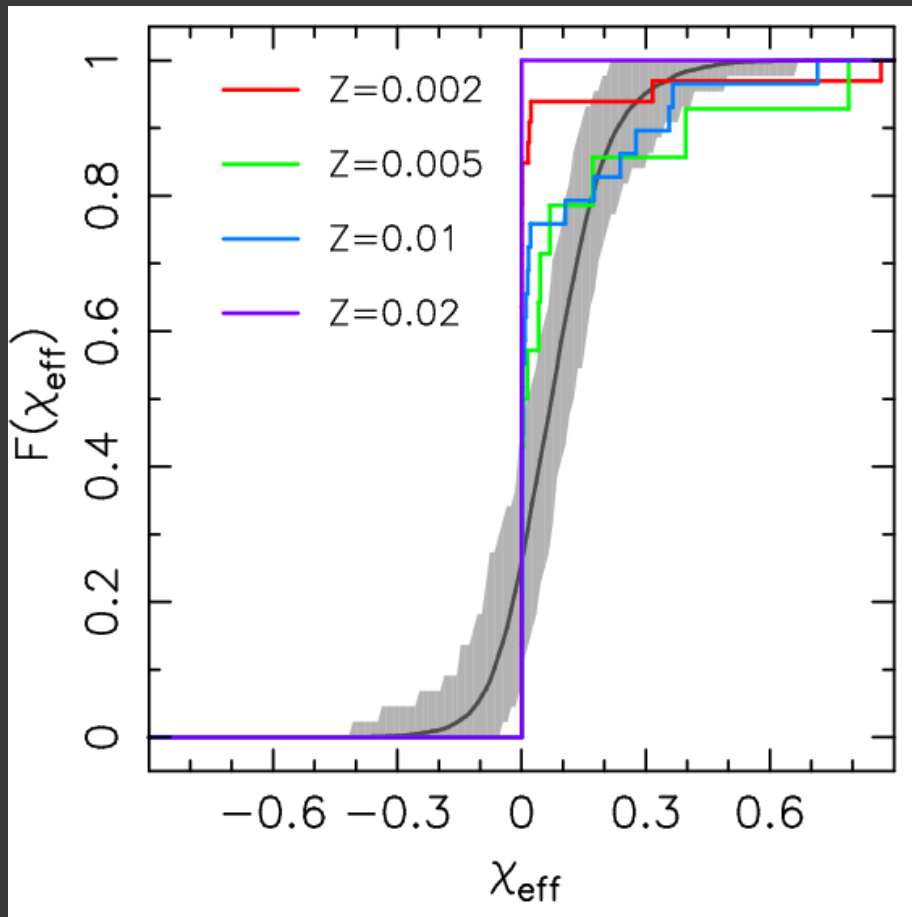
$0 \leq S_{1,2}(0) \leq 1$  randomly flat distribution,  
direction of  $S_{1,2}$  is isotropic



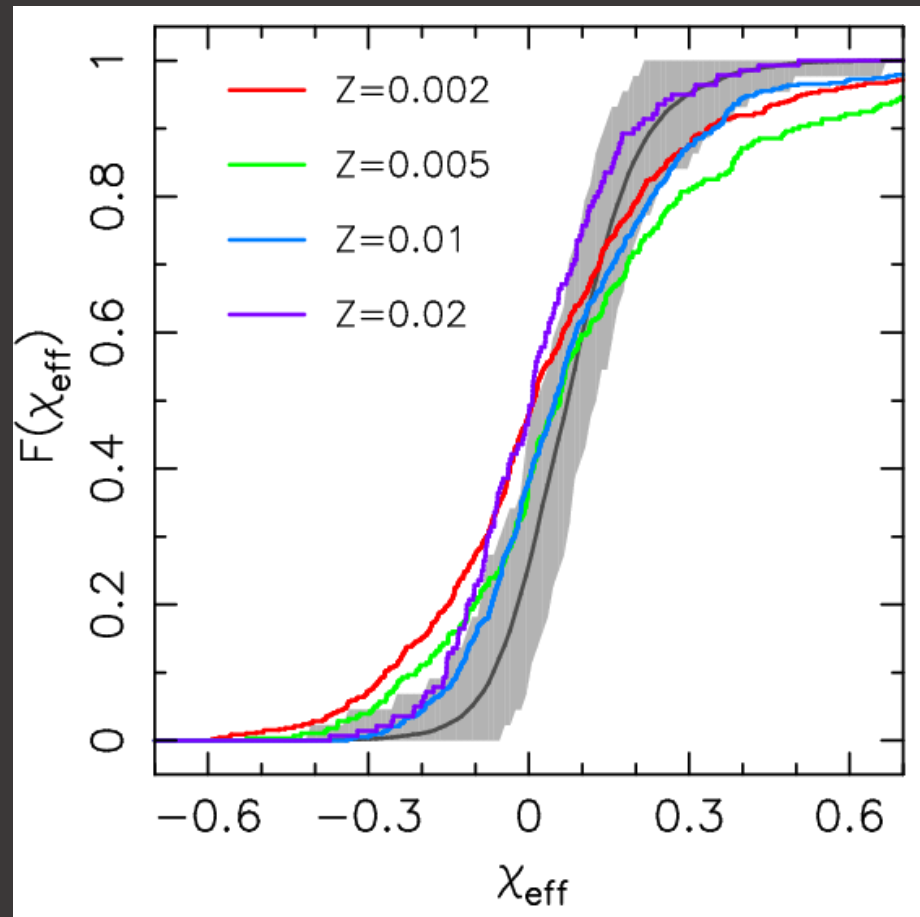


# Spin distribution

Modal 1  
 $S_{1,2}(0) = 0$

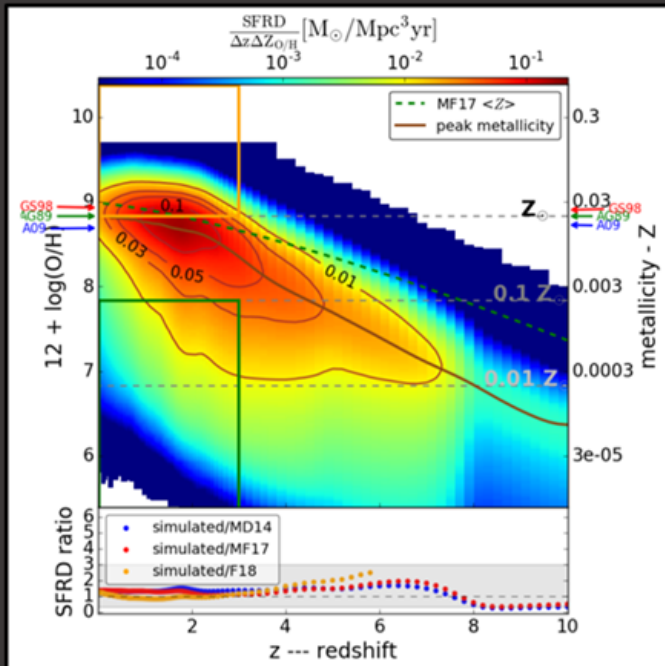


Modal 2  
 $S_{1,2}(0) : \text{flat isotropic}$

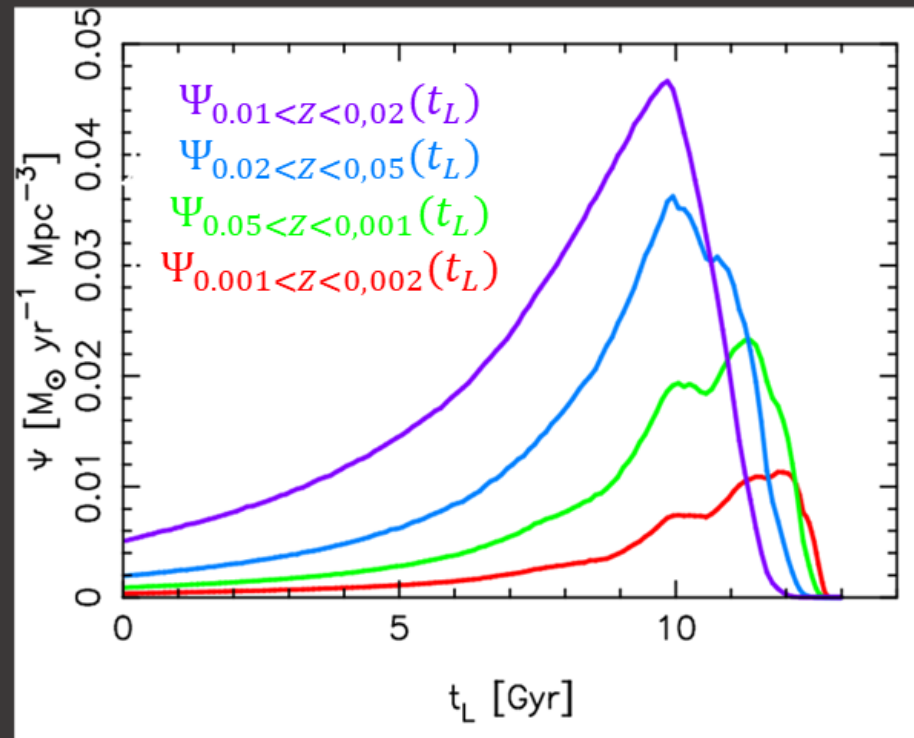


# Star formation history for each metallicity star

SFR( $Z, z$ )

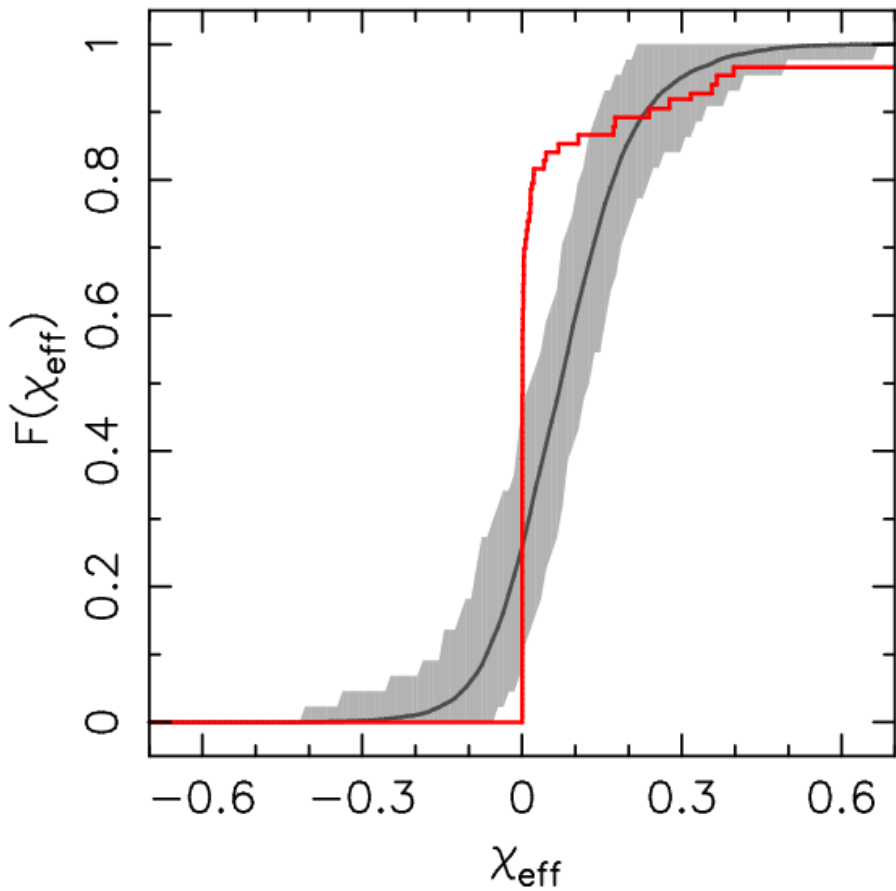


Chruslinska & Nelemans 2019



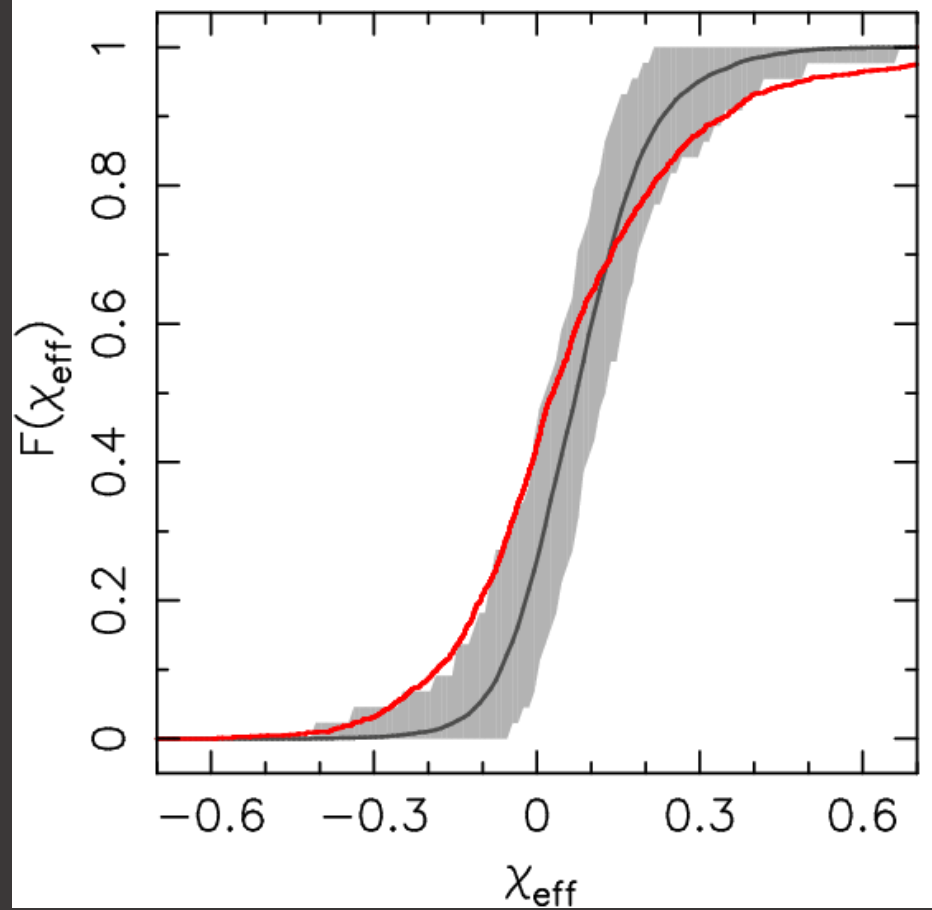
# Spin distribution

Modal 1  
 $S_{1,2}(0) = 0$



$$R_{\chi_{\text{eff}} > 0.1} \sim 11 \text{ yr}^{-1} \text{Gpc}^{-3}$$

Modal 2  
 $S_{1,2}(0)$  : flat isotropic



$$R_{\chi_{\text{eff}} > 0.1} \sim 25 \text{ yr}^{-1} \text{Gpc}^{-3}$$

# Summary

- We perform N-body simulations with a open cluster model and estimate the evolution of the spin parameters of the binary black holes formed in the simulation.
- By considering binary black hole mergers originating from open clusters, we can reproduce the spin parameter distribution as suggested by observations.
- The merger rate density of binary black holes with an effective spin parameter above 0.1 is

$$R_{\chi_{\text{eff}} > 0.1} \sim 11 \text{ yr}^{-1} \text{Gpc}^{-3} \quad (\chi_*(0) = 0 \text{ model})$$

$$R_{\chi_{\text{eff}} > 0.1} \sim 25 \text{ yr}^{-1} \text{Gpc}^{-3} \quad (\text{flat isolated model})$$